



รายงานวิจัยฉบับสมบูรณ์

โครงการ การศึกษาวิวัฒนาการโครงสร้างมหภาคในเอกภพ
Tracing Cosmic Structures Evolution

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คณะผู้วิจัย

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สนับสนุนโดย สำนักงานคณะกรรมการการอุดมศึกษาและสำนักงานกองทุนสนับสนุนการวิจัย
(ความเห็นในรายงานนี้เป็นของผู้วิจัย สำนักงานคณะกรรมการการอุดมศึกษาและ
สำนักงานกองทุนสนับสนุนการวิจัย ไม่จำเป็นต้องเห็นด้วยเสมอไป)

Executive Summary

ในปัจจุบันนักเอกภพวิทยาได้ให้ความสนใจในการศึกษาโครงสร้างเอกภพโดยอาศัยกลุ่มกาแล็กซีเป็นเครื่องมือที่สำคัญที่สุดชิ้นหนึ่ง แต่ยังมีช่องว่างระหว่างแนวคิดทางทฤษฎีที่เกี่ยวข้องกับวัตถุเหล่านี้กับการสังเกตการณ์จริงในเอกภพ โครงการวิจัยที่เคยได้รับการสนับสนุนโดย สกว. นั้น (โครงการ *Investigating the evolution of X-ray properties of galaxy clusters*, สัญญาเลขที่ MRG4680129) ได้ทำการศึกษาวิวัฒนาการของกลุ่มกาแล็กซีในเอกภพจำลอง ซึ่งในขณะนั้นแบบจำลองที่ใช้มีขนาดของกล่องเพียงด้านละ 100 Mpc/h และใช้อนุภาคบาร์ออนและสสารมืดชนิดละจำนวนประมาณ 4 ล้านอนุภาค ข้อดีของการศึกษาในแบบจำลองดังกล่าวนี้คือ จำนวนของกลุ่มกาแล็กซีที่เรดชิฟท์สูงนั้นมีจำนวนกลุ่มตัวอย่างน้อยเกินไป ปัจจุบันนี้กลุ่มความร่วมมือ Virgo Supercomputing Consortium ได้ทำการจำลองแบบด้วยกล่องที่มีขนาดใหญ่ขึ้นมาก เรียกว่า Millennium simulations (<http://www.mpa-garching.mpg.de/galform/millennium/>) ซึ่งเป็นกล่องขนาดด้านละ 500 Mpc/h และใช้อนุภาคจำนวนชนิดละประมาณ 500 ล้านอนุภาค การใช้ข้อมูลใหม่ที่ได้นี้จะทำให้จำนวนกลุ่มกาแล็กซีที่เรดชิฟท์สูงมีจำนวนมากขึ้น และลดความแปรปรวนของการวัดวิวัฒนาการได้ และหลังจากที่ผลการสำรวจกลุ่มกาแล็กซีของโครงการ XMM Cluster Survey (XCS, <http://www.xcs-home.org>) เสร็จสิ้น ความเข้าใจเกี่ยวกับวิวัฒนาการของโครงสร้างเอกภพจะมีความชัดเจนเป็นรูปธรรมมากขึ้น

สำหรับการศึกษาในภาคทฤษฎีนั้น เป็นแนวทางที่จะทำให้ความเข้าใจว่าผลของพลังงานมืด (dark energy) มีต่อโครงสร้างเชิงมหภาคของเอกภพได้อย่างไร ทั้งนี้เนื่องจากพลังงานมืดนั้นมีสัดส่วนประมาณ 70% ของเอกภพ แต่นักเอกภพวิทยายังไม่เข้าใจคุณสมบัติทางฟิสิกส์ที่แท้จริงนัก ประเด็นนี้มีความสำคัญอย่างยิ่งต่องานวิจัยด้านเอกภพวิทยา แต่เป็นงานที่นักฟิสิกส์อนุภาคจะต้องดำเนินต่อไปและไม่ใชขอบเขตของโครงการนี้ สิ่งซึ่งโครงการนี้ต้องการศึกษานั้นเป็นการใช้โครงสร้างเอกภพเพื่อเป็นเครื่องมือในการศึกษาคุณสมบัติของพลังงานมืด โดยการสร้างแบบจำลองทางทฤษฎีให้เกิดองค์ความรู้เกี่ยวกับความสัมพันธ์ระหว่างพลังงานมืดกับโครงสร้างในเอกภพ

1. วัตถุประสงค์ของโครงการ

1. เพื่อศึกษาคุณสมบัติของกลุ่มกาแล็กซีที่เกิดขึ้นในแบบจำลองทางความร้อนต่าง ๆ กัน และตรวจสอบกับผลที่ได้จากการสำรวจกลุ่มกาแล็กซีที่ลำดับวิวัฒนาการต่าง ๆ จากการสังเกตการณ์จริง
2. เพื่อสร้างองค์ความรู้เชิงทฤษฎีเกี่ยวกับเงื่อนไขการเกิดโครงสร้างในเอกภพภายใต้อิทธิพลของพลังงานมืด

2. ระเบียบวิธีวิจัย

โครงการนี้อาศัย 2 แนวทางซึ่งจะดำเนินไปควบคู่กัน ได้แก่การใช้แบบจำลองเอกภพในคอมพิวเตอร์และการศึกษาภาคทฤษฎี สำหรับแนวทางแรกคือการใช้แบบจำลองในคอมพิวเตอร์นั้น จะเป็นการใช้ผลการจำลองเอกภพที่มีความละเอียดและมีขนาดใหญ่ที่สุดในปัจจุบันภายใต้กลุ่มความร่วมมือ Virgo Supercomputing Consortium ซึ่งผู้เสนอโครงการมีสถานภาพเป็นสมาชิก โดยทำการศึกษาคุณสมบัติของกลุ่มกาแล็กซีที่เกิดขึ้นภายในแบบจำลองเพื่อนำไปเปรียบเทียบกับผลการสำรวจกลุ่มกาแล็กซี XMM Cluster Survey (XCS) ซึ่งจะเสร็จสิ้นในอีกสองปีข้างหน้า และจะทำให้สามารถสร้างเข้าใจกระบวนการที่เกิดขึ้นจริงภายในกลุ่มกาแล็กซีได้ โดยการจำลองแบบที่จะนำมาใช้นั้นนับว่าเป็นแบบจำลองที่มีขนาดใหญ่ที่สุดใน

ปัจจุบัน เรียกว่า Millennium simulations (<http://www.mpa-garching.mpg.de/galform/millennium/>) เป็นกล่องขนาดด้านละ 500 Mpc/h และใช้อนุภาคจำนวนชนิดละประมาณ 500 ล้านอนุภาค การใช้ข้อมูลใหม่ที่ได้นี้จะทำให้จำนวนกลุ่มกาแลกซีที่เรดชิฟท์สูงมีจำนวนมากขึ้น และลดความแปรปรวนของการวัดวิวัฒนาการได้

สำหรับแนวทางที่สองคือการศึกษากาแลกซีนั้นจะให้ความสำคัญในการใช้โครงสร้างขนาดใหญ่เป็นเครื่องมือเพื่อศึกษาเอกภพเชิงมหภาค อันได้แก่ เงื่อนไขการเกิดโครงสร้าง (virialisation conditions) ภายใต้อิทธิพลของพลังงานมืด การก่อตัวรวมกันของโครงสร้าง (clustering) ฟังก์ชันมวล (mass function) เป็นต้น เพื่อให้เกิดองค์ความรู้เกี่ยวกับธรรมชาติของพลังงานมืด

3. ผลงานที่คาดว่าจะตีพิมพ์

โครงการวิจัยนี้คาดว่าจะสามารถผลิตผลงานตีพิมพ์ได้อย่างน้อย 1 เรื่อง ในปีที่สองได้แก่บทความที่มีเนื้อหาใกล้เคียงกับ “Evolution of Cluster X-ray Properties in Millennium Gas Project” หรือ “Virialisation in Dark Energy Models” ใน Astrophysical Journal หรือ Monthly Notices of the Royal Astronomical Society

Output

1. Short CJ, Thomas PA, Young O, Pearce FR, Jenkins A, Muanwong O, *The evolution of galaxy cluster X-ray scaling relations*, 2010, Monthly Notices of the Royal Astronomical Society, 408, 2213-2233

วารสารมี JIF(2011) = 4.900

2. การศึกษาส่วนที่ 2 ได้นำไปสู่การเริ่มต้นหัวข้อวิจัยของนักศึกษาปริญญาโท ของนาย สุทธิลักษณ์ โอทาตะวงศ์ ซึ่งจะได้นำเสนอผลงานในส่วนที่ต่อยอดจากโครงการนี้ในการประชุม วทท. ครั้งที่ 38 ระหว่างวันที่ 17-19 ตุลาคม 2555 และคาดว่าจะสามารถตีพิมพ์ผลงานในวารสารระดับนานาชาติได้

บทคัดย่อ

โครงการวิจัยนี้ศึกษาวิวัฒนาการของโครงสร้างในเอกภพจากการจำลองแบบและด้านทฤษฎี ในงานส่วนแรกที่เกี่ยวข้องกับการจำลองแบบ ได้รายงานผลการศึกษาวิวัฒนาการของความสัมพันธ์ของคุณสมบัติในกลุ่มกาแล็กซีย่านเอกซ์เรย์ ซึ่งได้จากการจำลองแบบของ Millennium Gas Simulation ในเอกภพแบบ Λ CDM ด้วยขนาดของกล่องจำลองแบบขนาดใหญ่ (ความยาวด้านละ 500 Mpc/h) ทำให้สามารถศึกษาวิวัฒนาการที่เรดชิฟท์สูงที่ระบบขนาดต่าง ๆ ได้ แบบจำลองที่ศึกษานี้เป็นการเพิ่มอุณหภูมิของอนุภาคก๊าซก่อนการก่อตัวของโครงสร้าง (Preheating model) โดยสามารถสร้างแคตาล็อกของวัตถุและคำนวณคุณสมบัติภายใน r_{500} ที่เรดชิฟท์ 0, 0.5, 1 และ 1.5 เมื่อเปรียบเทียบกับแบบจำลองที่ให้ความร้อนแบบอื่น พบว่าความสัมพันธ์คุณสมบัติในกลุ่มกาแล็กซีย่านเอกซ์เรย์ใน Preheating model มีวิวัฒนาการสอดคล้องกับภาคสังเกตการณ์ที่เรดชิฟท์สูง สำหรับงานในส่วนที่สอง ได้ศึกษาผลการเปลี่ยนแปลงพฤติกรรมของพลังงานมืดที่มีต่อโครงสร้างระดับกาแล็กซีขนาดใหญ่ถึงกลุ่มกาแล็กซี พบว่าการเปลี่ยนแปลงสัดส่วนของพลังงานมืดในโครงสร้างที่ยุบตัวและการเปลี่ยนแปลงระดับความเป็นเอกพันธ์ (degree of homogeneity) ของพลังงานมืดจะมีผลเปลี่ยนแปลงการกำหนดขอบเขตของกลุ่มกาแล็กซี

Abstract

This project aims to investigate the evolution of cosmic structure from the numerical simulation and theoretical approaches. In the first part, the numerical simulation, we report results of the evolution of scaling relations of X-ray galaxy clusters drawn from very large hydrodynamical simulations, the Millennium Gas Simulation, of Λ CDM cosmology. Given the large size of the simulated box (a side of $500 h^{-1}\text{Mpc}$), this allows us to probe the evolution at very high redshift to a great dynamical range. We investigate the evolution in the *Preheating* model where the gas is heated uniformly at a very high redshift prior to cluster formation. We produce catalogues of galaxy clusters and compute their bulk properties within r_{500} at redshifts 0, 0.5, 1 and 1.5. In comparison to other heating models, the evolution of scaling relations of the *Preheating* model is in good agreement with observations at high redshift. For the second part of this work, we are interested in altering the behaviour of dark energy in the scale of large galaxies to clusters. We find that by changing the fraction of dark energy in the collapsed structure and by changing the degree of homogeneity of dark energy, this will alter the definition of the boundary of clusters accordingly.

Acknowledgements

The PI greatly appreciates the support by the Thailand Research Fund and the Commission on Higher Education grant MRG5080314 . The Millennium Gas Simulation described in this report were carried out by the Virgo Supercomputing Consortium at the Nottingham HPC facility. The early part of the homogeneous/inhomogeneous dark energy cosmology was initiated under the Thailand Toray Science Foundation grant where in part it facilitated the PI during her research visit to work in collaboration with Dr. Nelson Nunes at the William I. Fine Theoretical Physics Institute in the University of Minnesota. Their hospitality was greatly appreciated.

On a more personal note, I wish to express my sincere gratitude to my mentor, Prof. Peter A. Thomas, who has been very helpful and supportive throughout the years. His guidance was highly professional and it set an excellent example to follow. Dr. Nelson Nunes, who was so willing to introduce me to the new area of research, was both a great friend and collaborator. Working with him has given me a new horizon in research. I am indebted to their generosity that they reached out to me, with all the opportunities I was kindly given. Although with so much joy this project has enriched my life, sometimes it was not so easy. My strength is restored and reinforced by my loving family, time and time again, for they have been a constant source of support all the way. And for this, I am forever grateful.

1. Part I

Evolution of X-ray clusters in the Millenium Gas Runs

1.1. Introduction

Galaxy clusters play an important role in cosmology as they can give an insight into of the true nature of the universe, particularly in terms of cosmic structure abundance, as they are the largest gravitationally-bound systems. Using their bulk properties such as luminosity, temperature and mass, cosmologists are able to constrain cosmological parameters. However, it has become increasingly interesting in understanding gas physics of the intracluster medium (ICM) which is suggested to be the key to understand manifestations of observed properties where they do not agree well with simple theory of self-similarity as proposed by Kaiser (1982).

Motivated by works, both observational and numerical, where it has been shown that self-similarity is not sufficient to explain observed X-ray properties as the thermodynamics of the ICM requires complicated gas physics than gravitational collapse alone. By including extra gas physics in simulations, we are able to reproduce observed scaling relations of galaxy clusters, at least at redshift zero. In order to discriminate between heating models of the ICM, investigating into the evolution of the scaling relations can assist us as the ICM is highly sensitive to the

thermodynamics. As shown previously in a smaller simulated box in our paper Muanwong et al. (2006) (hereafter MKT06), our results suggested that wide spread heating of the ICM, that is to heat the gas globally in the model called *Preheating* is favoured over one which heats the gas through the star formation, namely the *Feedback* model. Unfortunately, due to the size of the previous simulation box, we were not able to produce enough large systems at high redshifts. In this project, we examine the redshift dependence of scaling relations in the largest homogeneous cosmological simulations with gas particles in to date known as the Millennium Gas Simulation.

The results of the *Preheating* model in the Millennium Gas Simulation are used to make comparisons with other simulations of the same kind where heating processes are different. The PI of this project involves in the analysis of simulated data from the *Preheating* run which will later be called the PC run. For other models, the GO and FO runs, are the works of others. However, data from these models are essentials as they can provide the fuller picture of evolutionary studies than working on one alone. The latter two runs will be briefly described in Section 1.2. Some comments of these two runs will be made while the full descriptions and discussions are elaborated in the publication shown in the appendix.

1.2. The Simulations

We use simulated data from the Millennium Gas Simulations carried out at the Nottingham HPC facility as part of the collaboration of the Virgo Supercomputing Consortium. The cosmological parameters of the simulations are: $\Omega_M = 0.25$, $\Omega_\Lambda = 0.75$, $\Omega_b = 0.045$, $h = 0.73$, $n = 1$ and $\sigma_8 = 0.9$. These parameters are consistent with combined analyses from *WMAP* data (Spergel et al. 2003) and the 2dF galaxy redshift survey (Colless et al. 2001). The simulation box has a comoving volume with a side of $500 h^{-1}\text{Mpc}$. The box contains 500 million gas and 500 million dark matter particles whose masses are $3.12 \times 10^9 h^{-1} \text{M}_\odot$ and $1.422 \times 10^{10} h^{-1} \text{M}_\odot$, respectively, with the initial redshift of 49. In this report, we present results from a particular model, namely the *Preheating* model, where gas particles at redshift 4 are heated to 200 keV/cm^2 as this reproduces the observed luminosity-temperature relation at redshift 0 (Borgani et al. 2004). This model also includes radiative cooling of gas. We will later refer to this run as the PC run. There are two other runs are new members of the Millennium Gas suite. The GO run is a base model where only gravitational heating is incorporated. It should be expected that clusters should behave self-similarly in this case. The FO run is one which incorporates the feedback from supernovae and active galactic nuclei where the energy input into intracluster gas is taken from a semi-analytic model of galaxy formation. This ensures that the source of feedback is a population of galaxies that

closely resembles that found in the real universe. This work is the scheme proposed by Short & Thomas (2009) where full details are described. In our previous paper, MTK06, we have shown that while non-graviational heating models can reproduce the observed relation at redshift 0, we predict strongly positive, mildly positive and mildly negative evolution of the relation for the cases of cooling-only model, preheating and cooling, and the stellar feedback model, respectively. In the new Millennium Gas simulations, the large volume enables us to resolve statistically significant numbers of clusters at all redshifts relevant to cluster formation.

The PC run is a simplistic model where gas particles are heated uniformly at high redshift. Thus, it is interesting to see how the baryon fractions are produced in comparison with observations. As baryons are important constituents in clusters which manifest themselves in observed X-ray properties, we look at their fractions at redshift zero and compare with recent observations of Gonzalez et al. (2007) as shown in Figure 1. We find the overall baryon fraction (star+hot gas) to be in reasonable agreement with the observation, particularly in large systems, while in this *Preheating* model, the amount of stars formed in the simulation is not consistent with real systems.

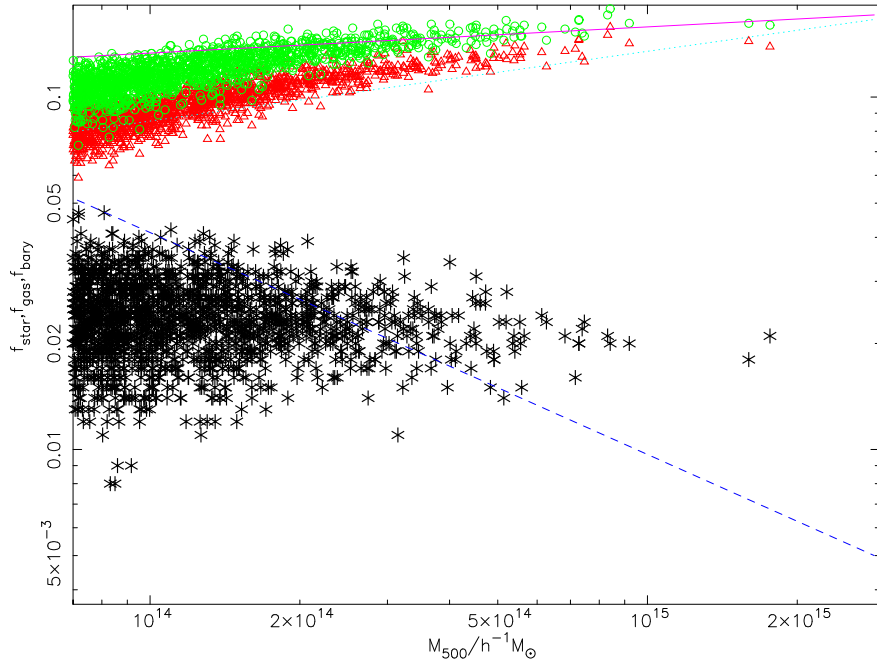


Fig. 1.— Baryon fractions at redshift zero where fraction of stars, hot gas and total baryon is denoted by stars, triangles and circles, respectively. Lines are best fits from observations.

1.3. Cluster catalogues and scaling relations

The simplest model of galaxy cluster formation is that they form via the gravitational collapse of the most overdense regions in the dark matter distribution, and the cluster baryons are heated only by gravitational processes (compression and shock heating) during the collapse. Since non-linear gravitational processes do not introduce any characteristic scale, we would then expect clusters to be self-similar, i.e. scaled versions of each other. With the additional assumptions that clusters are spherically symmetric systems and that the intracluster gas is in hydrostatic

equilibrium with the underlying dark matter potential, it is straightforward to derive simple self-similar scaling relations between cluster properties (Kaiser 1986).

Defining r_Δ as the radius of a spherical volume within which the mean matter density is Δ times the critical density at redshift z , we find that the total enclosed mass, M_Δ ,¹ scales with gas temperature, T_Δ , as

$$E(z)^{-2/3} T_\Delta \propto M_\Delta^{2/3}. \quad (1)$$

Under the further assumption that the X-ray emission of the ICM is primarily thermal Bremsstrahlung radiation (which is valid for $T > 2$ keV), the luminosity, $L_{X,\Delta}$, within r_Δ is given by

$$E(z)^{-1} L_{X,\Delta} \propto T_\Delta^2. \quad (2)$$

The scaling between X-ray luminosity and total mass follows upon combining equations (1) and (2):

$$E(z)^{-7/3} L_{X,\Delta} \propto M_\Delta^{4/3}. \quad (3)$$

The quantity $Y_X = M_{\text{gas}} T$ has recently attracted much attention since it has been shown to be a low-scatter mass proxy, regardless of cluster dynamical state (e.g. Kravtsov et al. 2006). This is primarily because Y_X approximates the total thermal energy of the ICM, which is not strongly affected by cluster mergers (Poole

¹ $M_\Delta = 4\pi r_\Delta^3 \Delta \rho_{\text{cr}}(z)/3$, where $\rho_{\text{cr}}(z) = 3H_0^2 E(z)^2 / 8\pi G$ is the critical density and $E(z)^2 = \Omega_{\text{m},0}(1+z)^3 + \Omega_{\Lambda,0}$ in a spatially-flat cosmological model.

et al. 2007), unlike L_X or T (Ricker & Sarazin 2001). The self-similar scaling of Y_X within r_Δ with total mass is

$$E(z)^{-2/3} Y_{X,\Delta} \propto M_\Delta^{5/3}. \quad (4)$$

The density contrast Δ governs the scale radius within which one measures the mass of a cluster. The most common choice is to set $\Delta = 500$, since r_{500} is the effective limiting radius for reliable observations from *Chandra* and *XMM-Newton*. Throughout this report we will adopt $\Delta = 500$, independent of redshift.

Cluster catalogues are generated at several redshifts for the three Millennium Gas simulations using a procedure similar to that employed by Muanwong et al. (2002), which we now briefly describe.

The first step is to identify gravitationally-bound groups of dark matter particles with the FOF algorithm. This was done on the fly in the FO run, and we have group catalogues stored at all 28 output redshifts between $z = 1.5$ and $z = 0$ for each resimulated cluster. For the GO and PC runs, FOF groups were identified in post-processing, setting the linking length to be 10% of the mean interparticle separation. Only groups with 500 particles or more were kept, corresponding to a minimum halo mass of $7.10 \times 10^{12} h^{-1} M_\odot$. We produced group catalogues for these two simulations at seven different redshifts: $z = 1.5, 1.25, 1, 0.75, 0.5, 0.25, 0$.

The spherical overdensity method is then used to construct cluster catalogues.

Briefly, a sphere is grown about the most gravitationally-bound dark matter particle of each FOF group until radii are found that enclose mean overdensities of $\Delta_{\text{vir}}(z)$, $\Delta = 200$, $\Delta = 500$, $\Delta = 1000$ and $\Delta = 2500$, relative to the critical density $\rho_{\text{cr}}(z)$. In cases where clusters overlap, we only keep the object with the largest mass within r_{2500} . We also discard clusters with fewer than 1000 particles at each overdensity, which corresponds to a minimum cluster mass of $8.61 \times 10^{11} h^{-1} \text{ M}_{\odot}$ in the FO run, and $1.73 \times 10^{13} h^{-1} \text{ M}_{\odot}$ in the GO and PC runs.

During the cluster identification process we compute a variety of cluster properties, averaged within each choice of scale radius. The relevant properties for this work are the total mass, gas mass, temperature and X-ray luminosity. The measure of temperature we adopt is the spectroscopic-like temperature T_{sl} (Mazzotta et al. 2004). In the Bremsstrahlung regime ($T > 2 \text{ keV}$), this temperature estimator has been shown to provide the closest match to the actual spectroscopic temperature, T_{spec} , obtained by fitting X-ray spectra of simulated clusters with a single-temperature plasma model. The X-ray luminosity is approximated by the bolometric emission-weighted luminosity, assuming the cooling function of Sutherland & Dopita (1993) and a fixed metallicity of 0.3. Three-dimensional gas density, spectroscopic-like temperature and entropy profiles are also computed for all our clusters by averaging particle properties within spherical shells, centred on the minimum of the dark matter potential.

For scaling laws involving the total cluster mass (Y_X - M , T_{sl} - M and L_X - M), we then impose a mass cut of $M_{500} \geq 10^{14} h^{-1} \text{M}_{\odot}$ at all redshifts of interest. For the L_X - T_{sl} relation, a cut is made in T_{sl} instead to ensure completeness in T_{sl} ; only clusters with a spectroscopic-like temperature greater than that corresponding to a mass of $M_{500} = 10^{14} h^{-1} \text{M}_{\odot}$ on the mean T_{sl} - M relation are kept. Table 1 lists the number of clusters in our final samples as a function of redshift for each of the Millennium Gas simulations.

1.4. Results

Radial cluster profiles are more sensitive to the precise manner in which non-gravitational cooling and heating processes are implemented in numerical simulations than X-ray scaling laws. Therefore, we start by examining whether our model for feedback from galaxies is able to explain the temperature and entropy profiles of observed low-redshift clusters. The observational dataset we use is REXCESS (Böhringer et al. 2007), a representative sample of 33 local ($z < 0.2$) clusters drawn from the REFLEX catalogue (Böhringer et al. 2004), all of which have been observed with *XMM-Newton*. Temperature profiles for the REXCESS clusters are presented in Arnaud et al. (2010), and entropy profiles in Pratt et al. (2010, hereafter PAP10). We choose to compare with REXCESS for three reasons. First, REXCESS clusters were selected in luminosity only, thus ensuring

Table 1: Number of clusters in each of the Millennium Gas simulations as a function of redshift, once the mass/temperature cut appropriate for each scaling relation has been made (see text).

Relation	Redshift			
	1.5	1	0.5	0
GO simulation				
Y_X - M , T_{sl} - M , L_X - M	25	145	549	1109
L_X - T_{sl}	15	107	441	946
PC simulation				
Y_X - M , T_{sl} - M , L_X - M	14	102	410	881
L_X - T_{sl}	13	93	376	838
FO simulation				
Y_X - M , T_{sl} - M , L_X - M	18	75	148	187
L_X - T_{sl}	15	67	139	186

no morphological bias, in such a way as to sample the X-ray cluster luminosity function in an optimal manner. Second, distances were optimised in REXCESS so that r_{500} falls well within the *XMM-Newton* field-of-view, increasing the precision of measurements at large radii. Third, the same definition of r_{500} is used as in this work.

To facilitate a fair comparison with our simulated data, we only consider observed clusters with a mass $M_{500} \geq 10^{14} h^{-1} M_{\odot}$. We have also rescaled the observational data to account for the fact that Arnaud et al. (2010) and PAP10 assumed a slightly different cosmological model in their analysis.

In the following, it will prove useful to divide the REXCESS sample into CC and non-cool-core (NCC) systems. As in Pratt et al. (2009, hereafter PCA09), clusters are classified as CC systems if they have a central gas density $E(z)^{-2} n_e(0) > 4.8 \times 10^{-2} h^{1/2} \text{cm}^{-3}$.

In Figure 2 we display the average spectroscopic-like temperature profile of clusters in the FO simulation. For comparison, we also show average profiles obtained from the reference GO and PC simulations and the observational data of Arnaud et al. (2010). We discard profile data at radii less than the gravitational softening length and only plot the average profile if there are 10 or more clusters in a given radial bin. All profiles have been normalised to the characteristic halo

temperature, T_{500} , computed from the self-similar model:

$$T_{500} = \frac{G}{2} \frac{\mu m_{\text{H}}}{k_{\text{B}}} \frac{M_{500}}{r_{500}}, \quad (5)$$

where $\mu = 0.59$ is the mean molecular weight for a fully ionised gas of primordial composition and m_{H} is the mass of a hydrogen atom. In the case of the observed profiles, T_{500} is calculated at the redshift of each individual cluster. With this scaling we would expect cluster profiles to coincide in the pure gravitational heating scenario.

Clusters formed in the GO simulation are clearly cooler than observed. This is because the spectroscopic-like temperature estimate is biased low by the cool, low-entropy cores of accreted subhaloes that are prevalent in GO cluster haloes (e.g. Mathiesen & Evrard 2001). The temperature profiles of individual clusters are flat in core regions, but we see a slight decline in the average scaled profile at small radii, $r \lesssim 0.1r_{500}$. This is because we are only averaging over the profiles of the most massive clusters at such radii, since the gravitational softening length is a smaller fraction of r_{500} for these objects, and the normalisation of the scaled temperature profiles decreases with increasing mass. In the self-similar model the normalisation of the scaled profiles should not depend on mass; the reason for the mass-dependence in our GO simulation is that more massive clusters are less concentrated than their low-mass counterparts, i.e. even the dark matter is not truly self-similar.

In the PC and FO runs the source of non-gravitational heating is completely different, but the net effect of the entropy injection is the same: cool subclumps are erased and the average temperature of the intracluster gas increases. Both simulations lead to temperature profiles that provide a good overall match to the observed profiles of NCC clusters, being nearly isothermal in core regions $r \lesssim 0.15r_{500}$. Again, the down-turn in the average scaled profiles visible in core regions arises because, for small values of r/r_{500} , we are taking an average of the scaled temperature profiles of the most massive objects only, which have a lower normalisation than those of less massive systems.

The entropy of intracluster gas increases when heat energy is introduced, and decreases when radiative cooling carries heat energy away. Entropy profiles thus preserve a record of the physical processes responsible for similarity breaking in clusters (e.g. Voit et al. 2002, 2003).

If shock heating were the only mechanism acting to raise the entropy of the gas, then analytical models based on spherical collapse predict that entropy scales with radius as $K \propto r^{1.1}$ outside of central cluster regions (Tozzi & Norman 2001). Cosmological simulations that only include gravitational heating give rise to slightly steeper entropy profiles in cluster outskirts: $K \propto r^{1.2}$ (e.g. Voit et al. 2005; Nagai et al. 2007).

Observed profiles are also typically found to scale as $K \propto r^{1.1}$ at large

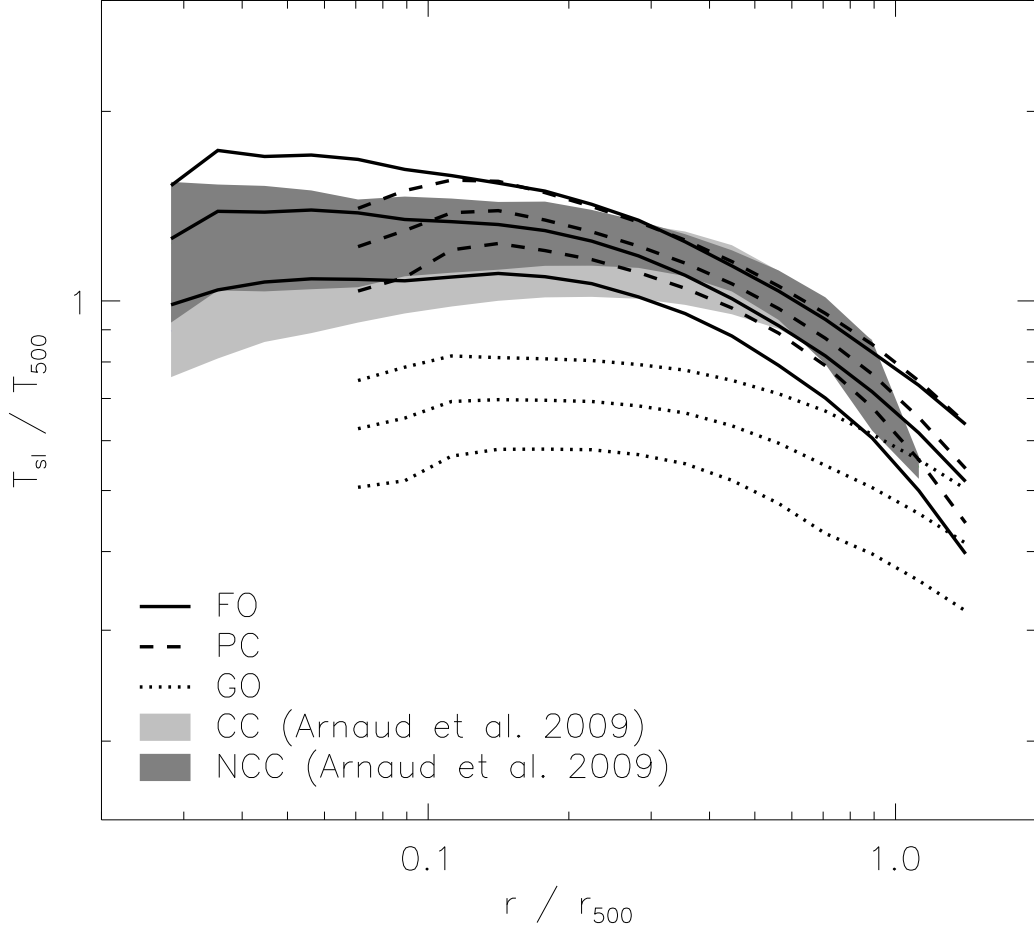


Fig. 2.— Mean spectroscopic-like temperature profiles, with 1σ scatter, obtained from the Millennium Gas simulations. The light and dark shaded regions enclose the mean profiles, plus 1σ scatter, of CC and NCC clusters in the REXCESS sample (Arnaud et al. 2010), respectively. Only clusters with a mass $M_{500} \geq 10^{14} h^{-1} M_{\odot}$ are considered.

cluster-centric radii, flattening in central regions (e.g. Ponman et al. 2003; Sun et al. 2009; Cavagnolo et al. 2009; Sanderson et al. 2009, PAP10). However, the precise radius at which this flattening occurs varies considerably, depending on such factors as the temperature (mass) of the system and whether it has a CC or a NCC. In particular, hotter, more massive objects have a higher mean core entropy (e.g. Cavagnolo et al. 2009), and the profiles of NCC clusters flatten off at significantly larger radii than those of CC clusters (e.g. Sanderson et al. 2009, PAP10).

Figure 3 compares the entropy profiles obtained from each of our three simulations with observational data from REXCESS (PAP10). For illustrative purposes, we also show the power-laws $K \propto r^{1.1}$ and $K \propto r^{1.2}$, assuming an arbitrary normalisation in both cases. We have scaled all entropy profiles by the ‘virial’ entropy, K_{500} , defined as

$$K_{500} = \frac{k_B T_{500}}{n_{e,500}^{\gamma-1}}, \quad (6)$$

where $n_{e,500}$ is the average electron density within r_{500} , given by

$$n_{e,500} = \frac{500 f_b E(z)^2 \rho_{cr,0}}{\mu_e m_H}, \quad (7)$$

and $\mu_e = 1.14$ is the mean molecular weight per free electron. Note that K_{500} depends only on the total halo mass, so is independent of the thermodynamic state of the gas.

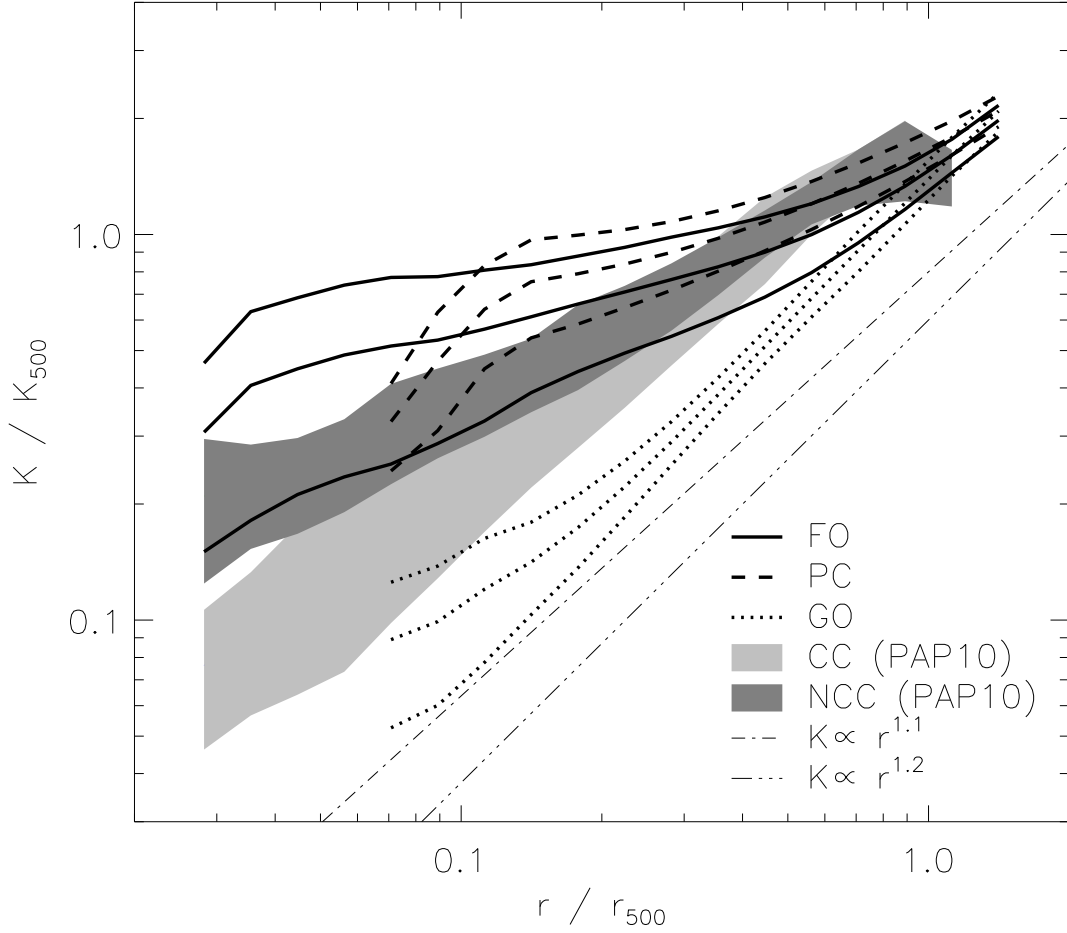


Fig. 3.— Mean entropy profiles, with 1σ scatter, obtained from the Millennium Gas simulations. The light and dark shaded regions enclose the mean profiles, plus 1σ scatter, of observed CC and NCC clusters from REXCESS (PAP10), respectively.

We only consider clusters with a mass $M_{500} \geq 10^{14} h^{-1} M_{\odot}$.

The entropy profiles of clusters extracted from the GO run are indeed well described by the power-law $K \propto r^{1.2}$ for $r \gtrsim 0.15r_{500}$, agreeing with the results of previous studies. There is also very little scatter about the mean, indicating self-similar scaling. For radii interior to $0.15r_{500}$ there is more diversity; some of the clusters have nearly isentropic cores while others show no signs of flattening. Compared to the observed entropy profiles of CC clusters, the profiles of objects in the GO run have a similar slope, at least for $r \gtrsim 0.15r_{500}$, but the normalisation is systematically too low. In the case of NCC clusters, it is evident that the GO model cannot explain the shallow profiles characteristic of these systems.

Clusters formed in the PC and FO simulations have entropy profiles that are broadly consistent with the theoretical scaling $K \propto r^{1.1}$ at large radii $r \gtrsim r_{500}$. This supports the idea that gravity dominates the ICM thermodynamics in the outer regions of clusters. As we move in towards the core from r_{500} , the slope decreases and the profiles flatten off, providing a fair match to the observed entropy profiles of NCC clusters. However, on average, both the PC and FO models predict entropy profiles with a shallower slope than those of NCC clusters in central regions, resulting in an overestimate of the core entropy. Note that the FO run yields entropy profiles that are slightly closer to the observed NCC cluster profiles than the PC run.

In both the PC and FO runs, we see a drop in the average scaled entropy

profiles at small values of r/r_{500} , where we are averaging over the profiles of just the most massive systems. This is because the normalisation of cluster entropy profiles decreases with mass in these simulations. To demonstrate this, in Figure 4 we plot the scaled entropy at r_{500} as a function of M_{500} for each of our simulations, along with observational data from REXCESS (PAP10). For clarity, we do not plot individual points for the GO simulation, but instead show the best-fit relation in log-log space, and the typical dispersion about this relation. The gradient of the best-fit line is very close to zero, so the normalisation of the scaled entropy profiles is independent of mass for GO clusters, as in the self-similar model. By contrast, our PC and FO models predict that the scaled entropy at r_{500} is a decreasing function of mass, implying that non-gravitational heating affects the entropy structure of the ICM out to larger radii in lower-mass systems. This is consistent with the expectation that non-gravitational processes are more influential at the low-mass end of the cluster population. Massive clusters in the PC and FO runs have a similar entropy at r_{500} to their GO counterparts. Note that the observational data points also appear to suggest that the scaled entropy at r_{500} decreases with increasing mass, being scattered about the PC and FO model predictions.

The mass-dependence of the normalisation of scaled cluster entropy profiles in the PC and FO runs explains why we see a larger scatter about the average profile than in the GO run. The scatter about the mean profile in the PC run is similar to

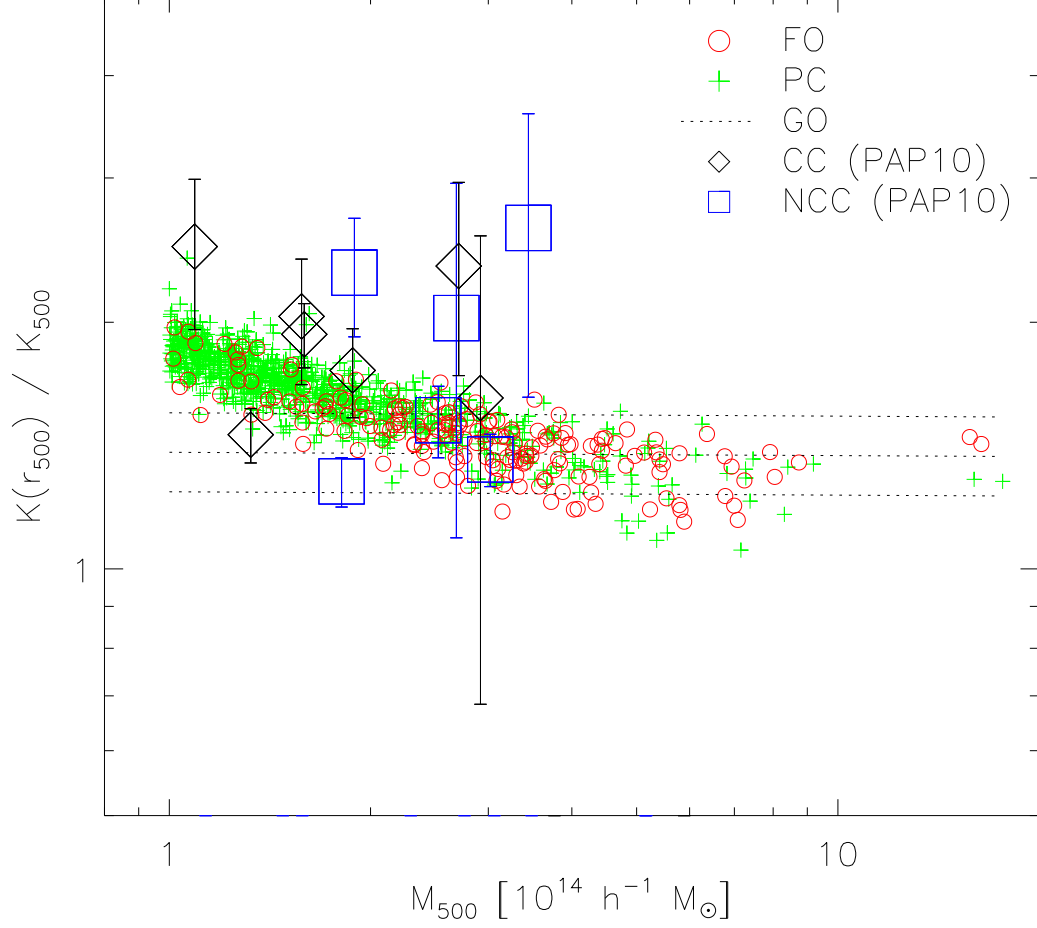


Fig. 4.— Scaled entropy at r_{500} as a function of total mass within r_{500} for clusters in the Millennium Gas simulations. For clarity, we do not display individual data points for the GO run, but instead show the best-fit relation and the typical dispersion about this relation. Observational data for CC and NCC clusters in the REXCESS sample (PAP10) are also shown for comparison, along with 1σ error bars. Only clusters with $M_{500} \geq 10^{14} h^{-1} M_{\odot}$ are considered.

that found in observed profiles of NCC systems, but the FO run generates clusters with a wider range of entropy profiles, leading to a larger scatter than is observed.

Neither the PC or the FO models are capable of reproducing the steeply declining entropy profiles seen in CC clusters. In the case of the FO run, this problem could potentially be overcome by including radiative cooling in our model, since cooling acts to lower the entropy in dense central regions where the gas cooling time is short. As we have said, cooling is included in the PC run, but it is curtailed at high redshift by the preheating.

Self-consistent N -body/SPH simulations that incorporate cooling, star formation and associated feedback are able to produce entropy profiles that resemble those of CC clusters, with a normalisation in the outer parts of clusters that is higher than predicted by pure gravitational heating, and a steep slope that remains roughly constant all the way into the core (e.g. Borgani et al. 2002, 2004; Kay et al. 2004; Kay 2004; Kay et al. 2007). However, this success is usually achieved at the expense of excessive star formation. Furthermore, such simulations fail to reproduce the observed entropy profiles of NCC systems.

We now discuss whether our feedback model generates local X-ray scaling laws that are compatible with observations, focusing on the Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} relations. In each case, we compare with the corresponding relation derived from the low-redshift REXCESS data by PCA09. Wherever possible, we

explain any differences that arise using the knowledge gleaned from our discussion of cluster profiles. The data of PCA09 are particularly suitable for a comparison with our simulated cluster samples because they tabulate spectral temperatures and luminosities within r_{500} (where r_{500} is defined as in this work), and their luminosities are bolometric. Note that we have rescaled the observational data to allow for the slightly different choice of cosmological parameters adopted by PCA09.

For each set of cluster properties, $(X, Y) = (M, Y_X), (M, T_{\text{sl}}), (M, L_X)$ and (T_{sl}, L_X) , we fit a power-law scaling relation of the form

$$E(z)^n Y = C_0 \left(\frac{X}{X_0} \right)^\alpha, \quad (8)$$

to our simulated data points by minimising χ^2 in log space. Here $X_0 = 5 \times 10^{14} h^{-1} \text{ M}_\odot$ if $X = M$ and $X_0 = 6 \text{ keV}$ if $X = T_{\text{sl}}$. The normalisation C_0 has units of $10^{14} \text{ M}_\odot \text{ keV}$, keV and $10^{44} h^{-2} \text{ erg s}^{-1}$ for $Y = Y_X, T_{\text{sl}}$ and L_X , respectively. Best-fitting parameters α and C_0 for each relation are summarised in Table 2. The factor $E(z)^n$ is included to remove the self-similar evolution predicted by equations (1)–(4), where the index $n = -2/3, -2/3, -7/3$ and -1 for the Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} relations, respectively. We include this scaling factor simply to ‘adjust’ observational data to $z = 0$ for comparison with our $z = 0$ simulated clusters. This will only be a small effect for the redshift range ($z < 0.2$) probed by the REXCESS sample.

Scatter in the relations, $\sigma_{\log_{10} Y}$, is quantified via the rms deviation of $\log_{10} Y$ from the mean relation:

$$\sigma_{\log_{10} Y}^2 = \frac{1}{N-2} \sum_{i=1}^N \left[\log_{10} Y_i - \alpha \log_{10} \left(\frac{X}{X_0} \right) - \log_{10} C_0 \right]^2, \quad (9)$$

where N is the number of individual data points (X_i, Y_i) . The scatter about each relation is also listed in Table 2.

We have demonstrated that the feedback model can reproduce the observed properties of massive low-redshift clusters reasonably well, apart from those with a CC. We have also seen that the $z = 0$ properties of clusters formed in the feedback run can be replicated almost exactly with a simplistic preheating model, where the entropy of the ICM is raised impulsively at $z = 4$, rather than by continual heating from SNe and AGN. Consequently, we cannot discriminate between these two models using data from local observations.

In Figure 9 we show the evolution of gas density, spectroscopic-like temperature and entropy profiles for clusters in the PC run. In the top row, we plot the profiles of the 10 hottest systems (i.e. the most massive objects) at each redshift and, in the bottom row, profiles for clusters in a narrow temperature range $3 \text{ keV} \leq T_{\text{sl}} \leq 4 \text{ keV}$. Again, we only keep profile data at radii greater than the gravitational softening length. We scale the density, temperature and entropy profiles by $n_{\text{e},500}$, T_{500} and K_{500} , respectively; see equations (5)–(7). With this

Table 2: Best-fit parameters (with 1σ errors) for the $z = 0$ X-ray scaling relations obtained from the Millennium Gas simulations.

Relation	C_0	α	$\sigma_{\log_{10} Y}$
GO simulation			
Y_X-M	4.202 ± 0.070	1.547 ± 0.014	0.087
$T_{\text{sl}}-M$	3.931 ± 0.057	0.554 ± 0.012	0.076
L_X-M	18.58 ± 0.53	1.203 ± 0.024	0.148
L_X-T_{sl}	37.6 ± 1.5	2.004 ± 0.040	0.137
PC simulation			
Y_X-M	5.622 ± 0.052	1.7805 ± 0.0079	0.045
$T_{\text{sl}}-M$	6.310 ± 0.031	0.5512 ± 0.0042	0.024
L_X-M	5.549 ± 0.088	1.842 ± 0.013	0.076
L_X-T_{sl}	4.563 ± 0.055	3.297 ± 0.020	0.063
FO simulation			
Y_X-M	5.757 ± 0.069	1.692 ± 0.016	0.048
$T_{\text{sl}}-M$	6.333 ± 0.049	0.521 ± 0.010	0.031
L_X-M	6.17 ± 0.15	1.777 ± 0.033	0.098
L_X-T_{sl}	4.99 ± 0.12	3.296 ± 0.065	0.104

C_0 is the best-fitting normalisation of the relations, and α is the best-fitting slope;

see equation (8). $\sigma_{\log_{10} Y}$ is the scatter about the mean relation as defined by

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equation (9).

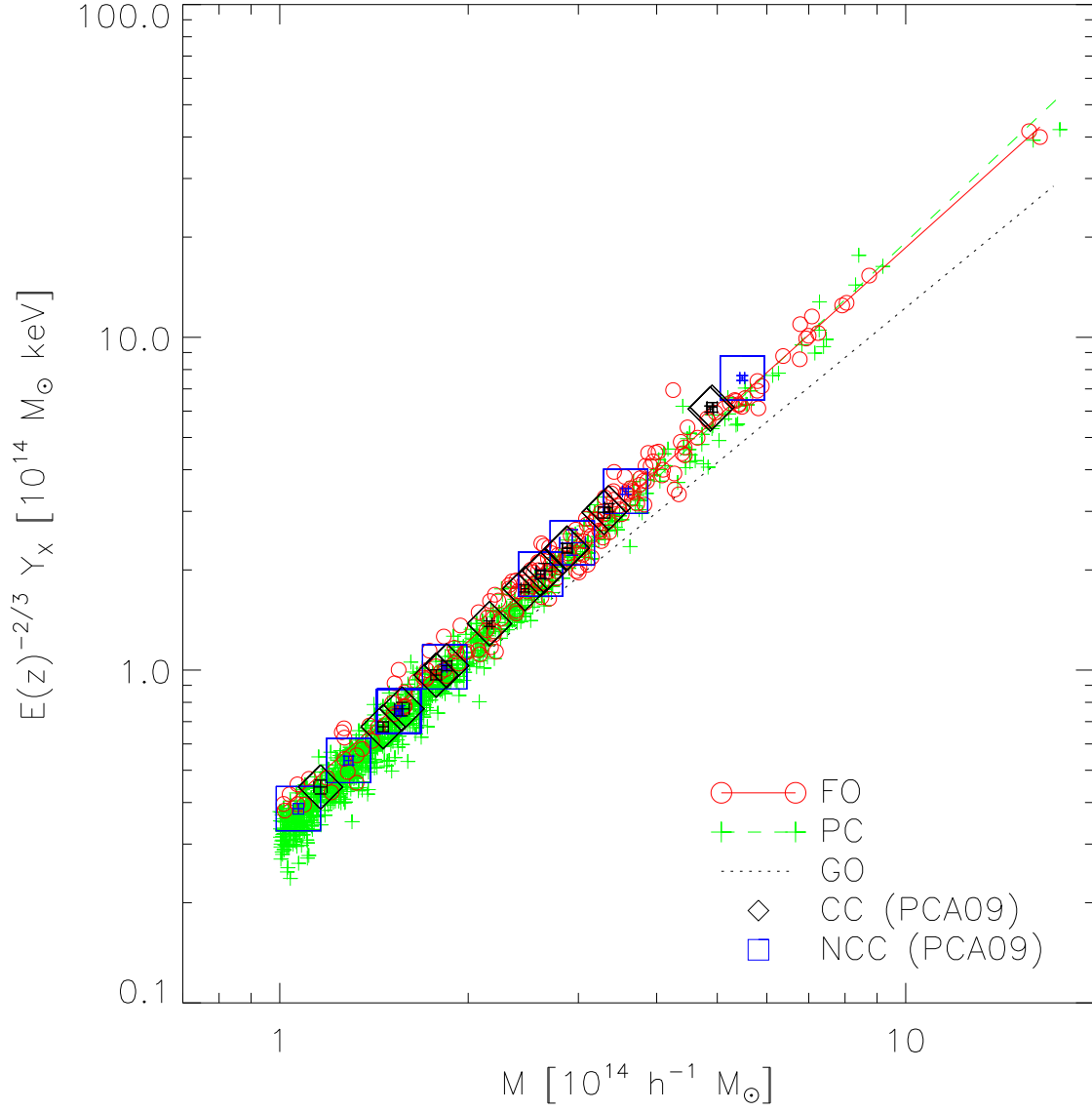


Fig. 5.— Y_X as a function of total mass within r_{500} for $z = 0$ clusters in the Millennium Gas simulations. We do not display data points from the GO run for clarity. Observational data for CC and NCC clusters from REXCESS (PCA09) is shown for comparison, along with 1σ error bars.

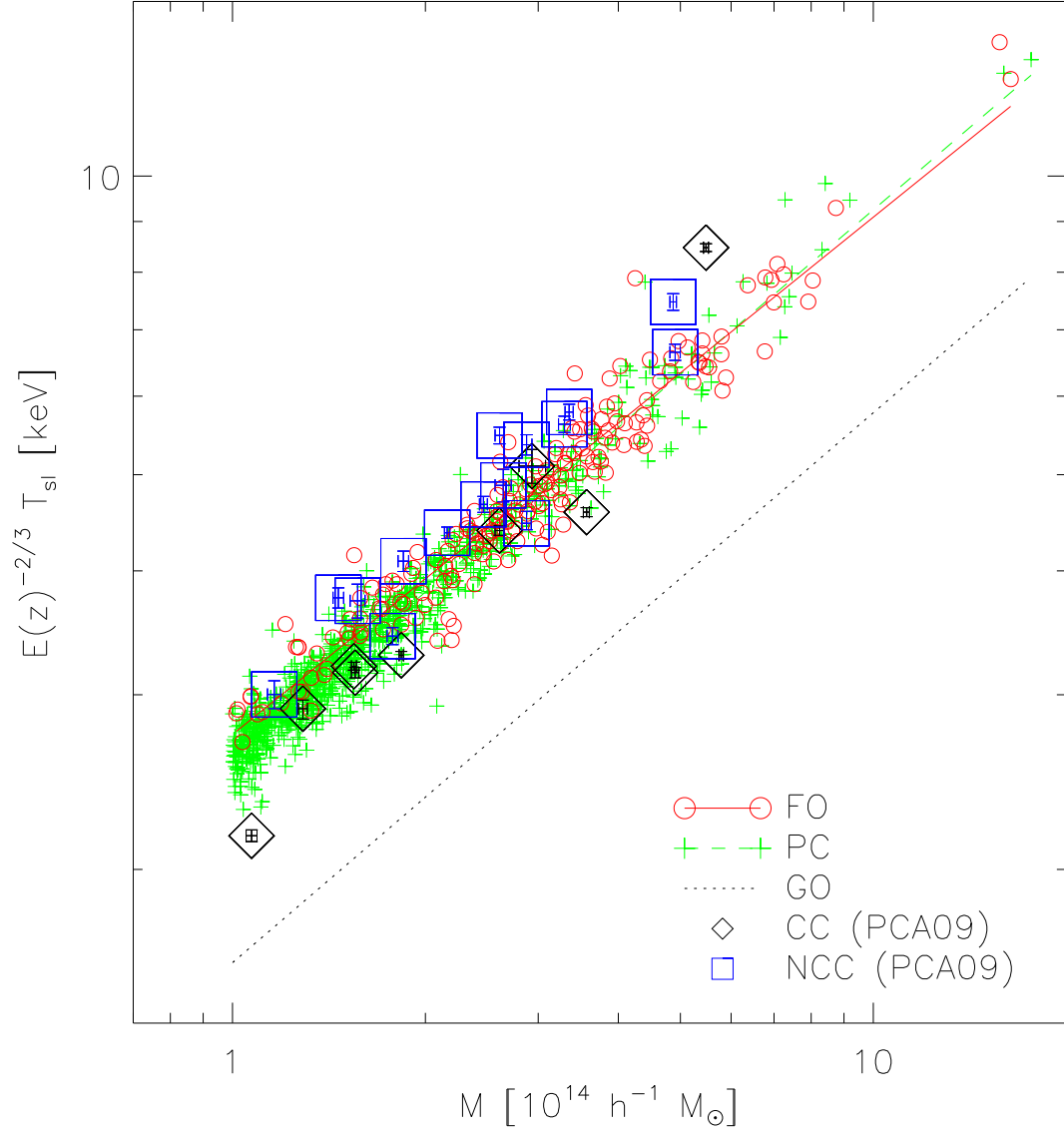


Fig. 6.— Spectroscopic-like temperature as a function of total mass within r_{500} for $z = 0$ clusters in the Millennium Gas simulations. We also display observational data for CC and NCC clusters in the REXCESS sample (PCA09).

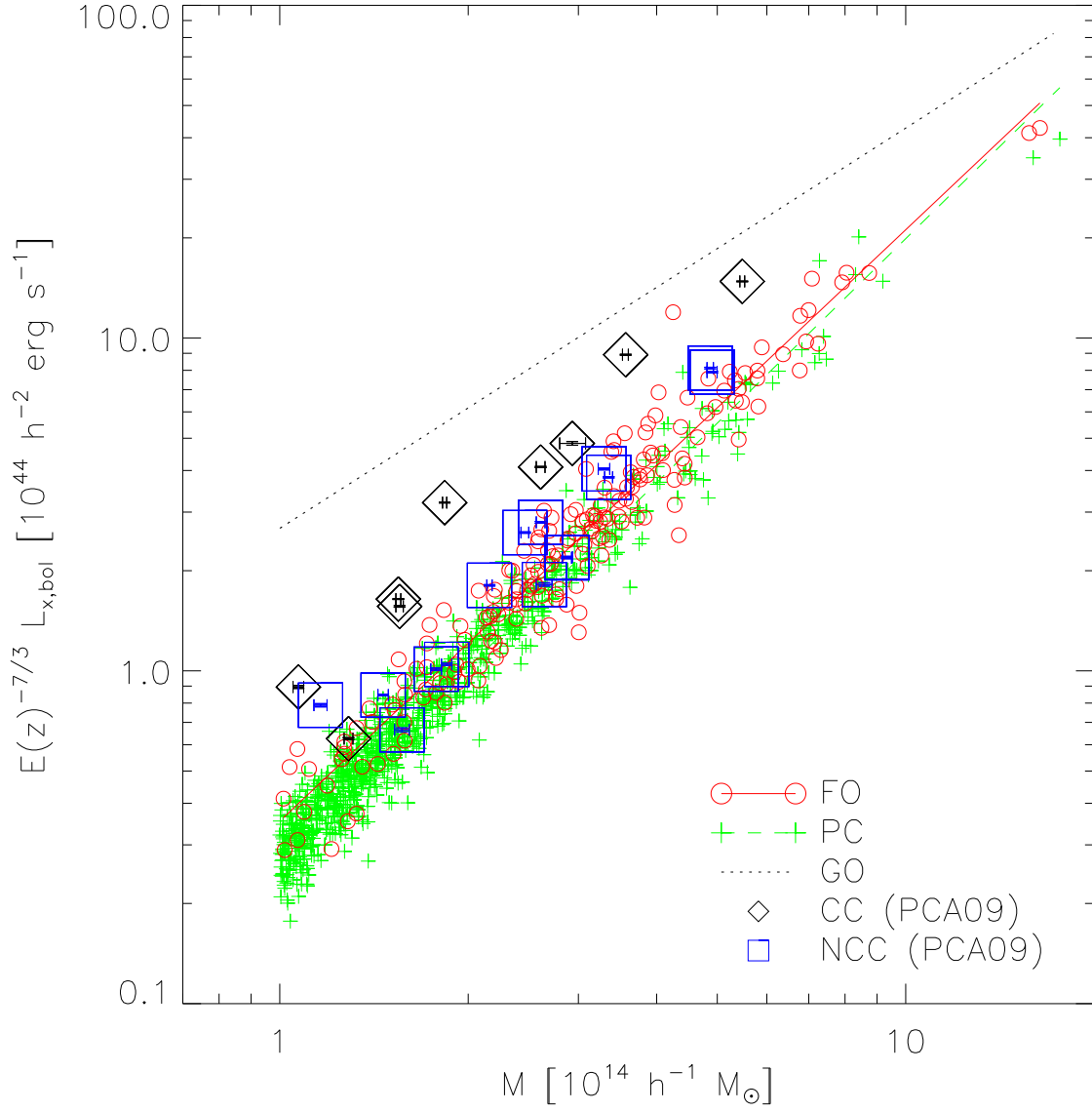


Fig. 7.— Bolometric X-ray luminosity as a function of total mass within r_{500} for $z = 0$ clusters in the Millennium Gas simulations. Observational data for CC and NCC clusters from REXCESS (PCA09) is also shown.

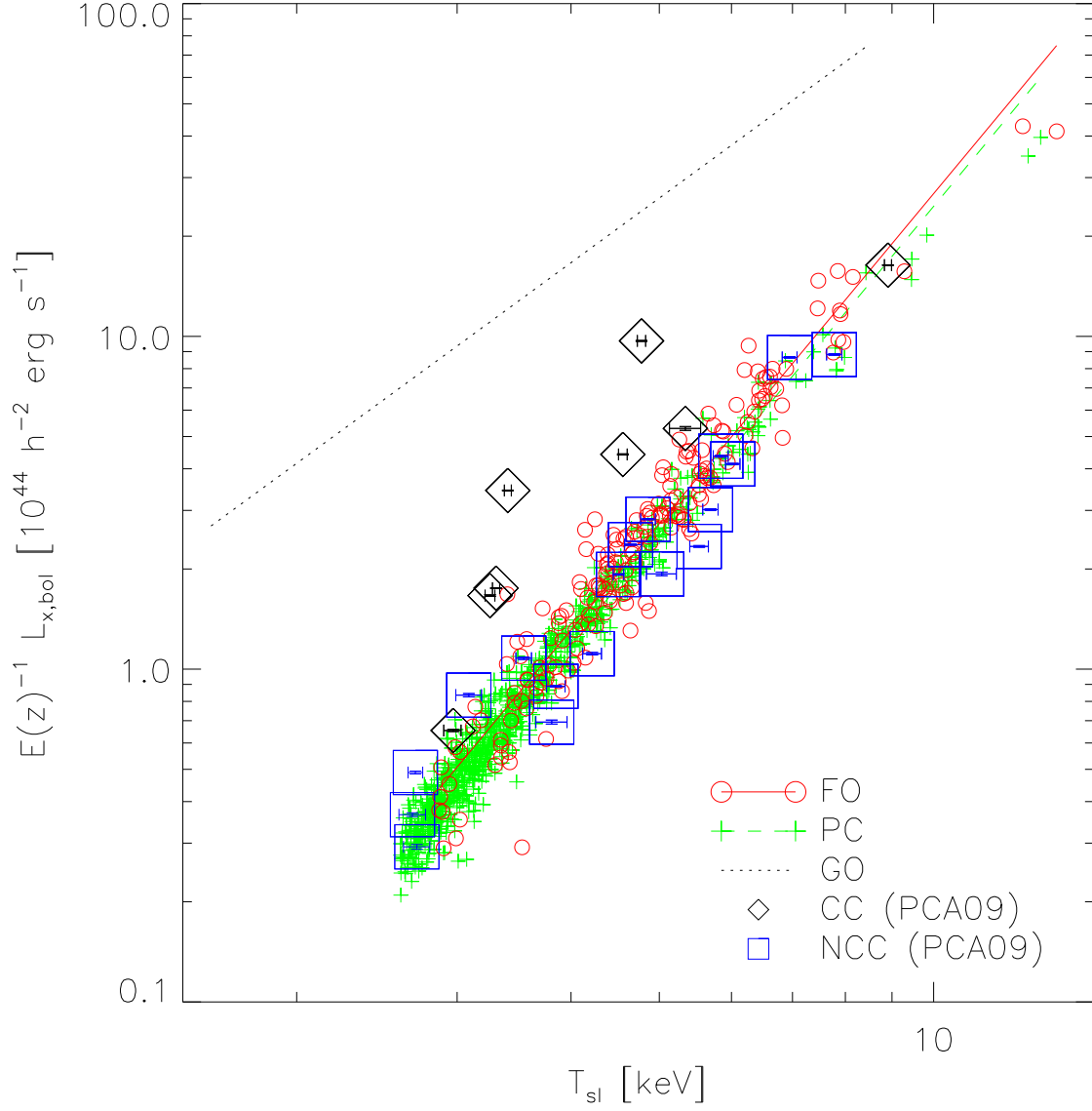


Fig. 8.— Bolometric X-ray luminosity as a function of spectroscopic-like temperature for $z = 0$ clusters in the Millennium Gas simulations. X-ray properties are calculated within r_{500} . For comparative purposes, we plot observational data for CC and NCC clusters in the REXCESS sample (PCA09).

scaling we would expect to see no evolution of cluster profiles in the self-similar model, where the ICM is only heated by gravitational processes. We have confirmed that this is indeed the case in our GO run.

Focusing on the profiles of the hottest clusters, we see clear signs of evolution beyond the self-similar prediction, which can be understood as follows. Imposing a uniform entropy floor at $z = 4$ boosts the entropy of the ICM more in core regions than at large radii. Gas is driven out from central cluster regions, flattening the density profile and increasing the normalisation of the temperature profile, relative to the prediction from gravitational heating alone. Note that the temperature must increase if the slope of the density profile decreases to maintain pressure support.

After preheating, ejected gas is gradually reincorporated into descendant haloes as hierarchical growth proceeds. Since the gas density has already been lowered by the preheating, it does not decrease as rapidly as in the gravitational heating scenario, so we see an increase relative to the average gas density $n_{e,500}$ as $z \rightarrow 0$. Likewise, the preheated gas has a higher temperature and entropy than if the only source of heating was gravity. Therefore, as gas is accreted back onto descendant haloes, compression and shock heating raise its temperature and entropy at a lesser rate than in the gravitational heating model. This explains why we see a drop in gas temperature and entropy with redshift relative to T_{500} and K_{500} , respectively. Given that there is no further non-gravitational heating

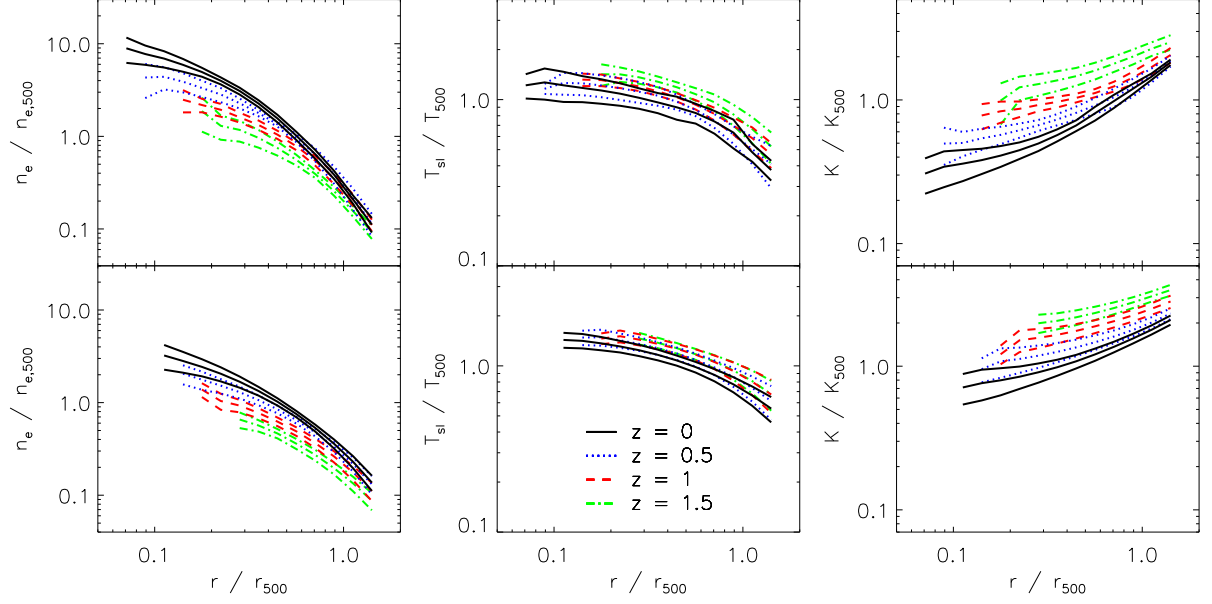


Fig. 9.— Evolution of gas density (first column), spectroscopic-like temperature (second column) and entropy (third column) profiles for clusters in the Millennium Gas PC run. The top row shows the evolution of the ten hottest systems, while the bottom row shows the evolution of clusters with a temperature in the range $3 \text{ keV} \leq T_{\text{sl}} \leq 4 \text{ keV}$.

of intracluster gas in the PC run, the high-redshift entropy injection will become increasingly ‘diluted’ with time, and cluster profiles will eventually resemble those obtained from a simulation with gravitational heating only.

At any given redshift, several of the 10 hottest objects are likely to have undergone a recent major merger, which could potentially affect the shape, dispersion and evolution of cluster profiles. To investigate this, we first compute the substructure statistic

$$S = \frac{|\mathbf{x}_{\text{com}} - \mathbf{x}_c|}{r_{500}}, \quad (10)$$

for each of the 10 most massive clusters at each redshift of interest. Here, $\mathbf{x}_c$ is the location of the dark matter potential minimum, which we take to be the cluster centre, and $\mathbf{x}_{\text{com}}$ is the centre of mass of the cluster gas, defined by

$$\mathbf{x}_{\text{com}} = \mathbf{x}_c + \frac{\sum_i m_i (\mathbf{x}_i - \mathbf{x}_c)}{\sum_i m_i}, \quad (11)$$

where the sums are over all gas particles within r_{500} . Systems undergoing a major merger will be dynamically disturbed and will thus have a larger value of S .

Following Kay et al. (2007), we say that a cluster is disturbed if $S > 0.1$, and relaxed otherwise. At each redshift, we have found that the shape and dispersion of the radial profiles shown in the top row of Figure 9 remain almost unchanged if we only consider relaxed clusters in the sample of the 10 hottest systems. This signifies that our results are not affected by cluster mergers.

The scaled profiles of clusters with $3 \text{ keV} \leq T_{\text{sl}} \leq 4 \text{ keV}$ evolve in similar

way to those of the most massive objects, but their shape is different at each redshift. In particular, their density and entropy profiles are flatter. The reason for these differences is that we are now considering lower-mass clusters. Consequently, preheating is more effective at removing gas from their shallower potential wells, modifying their thermodynamic properties out to larger radii.

We have seen that feedback from galaxy formation leads to dramatically different evolution of cluster profiles than high-redshift preheating. It follows that we should see differences in the evolution of X-ray scaling laws too. We now examine whether the evolution of the Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} relations predicted by our FO simulation is compatible with observational data, and whether the data prefers this model over simple preheating. The datasets we use are the low-redshift REXCESS sample of PCA09, and the high-redshift sample of Maughan et al. (2008a, hereafter MJF08). We choose to compare with the data of MJF08 for several reasons. First, this dataset is one of the largest high-redshift X-ray-selected cluster samples currently available, consisting of 115 clusters observed with *Chandra*. Second, it covers a broader redshift range ($0.1 < z < 1.3$) than any other existing large sample. Third, temperatures and bolometric luminosities were derived in the aperture $0 < r \leq r_{500}$, using the same definition of r_{500} as in this work. This agrees with the way in which these properties were calculated for our simulated clusters. Nevertheless, we must be careful not to over-interpret any

comparison of our simulated data with observations since strong selection biases limit our ability to perform a statistically meaningful comparison.

To account for the evolution of X-ray observables, we define scaling relations by

$$E(z)^n Y = C(z) \left(\frac{X}{X_0} \right)^\alpha, \quad (12)$$

where all quantities are as in equation (8), except that the normalisation is now a function of redshift. For each relation, we fix the slope α to the $z = 0$ value found previously (see Table 2), and compute the normalisation at each redshift by minimising χ^2 in log space. The self-similar model predicts that the slope of each relation will be independent of redshift. In our simulations, we see small fluctuations in the slope with redshift, but there is no systematic variation, justifying our assumption of a fixed slope.

A power-law of the form

$$C(z) = C_0(1+z)^\beta, \quad (13)$$

is then fit to the normalisation data to determine the parameters C_0 and β (note that this may cause C_0 to change slightly from the $z = 0$ value given in Table 2). Best-fitting parameters for each relation are listed in Table 3. Since we have included the $E(z)^n$ factor in equation (12), then we would expect the slope β to be zero if clusters do indeed evolve self-similarly. If $\beta < 0$ or $\beta > 0$, then we say there is negative or positive evolution, respectively. Note that some authors do not scale

out the expected self-similar behaviour first, so their definition of negative/positive evolution has a different meaning to ours. This is one reason why care must be taken when comparing the results of different studies.

The PC run predicts negative evolution of the L_X - T_{sl} relation as well, which is more pronounced than for the L_X - M relation. This is because the temperature increases relative to the self-similar prediction with redshift (Figure 9), whereas the total mass decreases at a similar rate. Over a given redshift interval, the normalisation of the L_X - T_{sl} relation decreases more than that of the L_X - M relation, so we see a larger drop in normalisation relative to the self-similar model, implying stronger negative evolution. As before, the evolution of the PC L_X - T_{sl} relation will have been tempered somewhat, because the slope is steeper than the self-similar value. Energy feedback from galaxies leads to substantially different evolution of the Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} relations than uniform preheating. We now discuss which of the PC and FO models, if either, is preferred by the high-redshift data of MJF08.

We begin by noting that, as in REXCESS, the masses of clusters in the sample of MJF08 were estimated from a Y_X - M relation. Since this relation was calibrated using clusters with hydrostatic mass estimates, the masses of their high-redshift clusters are also likely to be biased low by $\sim 10 - 20\%$. Therefore, the observational data points shown in Figures 11 and 12 should all be shifted down by $\sim 5 - 10\%$

Table 3: Best-fit parameters (with 1σ errors) for the evolution of the normalisation of the X-ray scaling relations predicted by each Millennium Gas simulation.

Relation	C_0	β
GO simulation		
Y_X - M	4.222 ± 0.028	-0.267 ± 0.011
T_{sl} - M	3.941 ± 0.031	-0.335 ± 0.013
L_X - M	19.53 ± 0.65	-0.243 ± 0.055
L_X - T_{sl}	39.4 ± 1.4	0.370 ± 0.058
PC simulation		
Y_X - M	5.96 ± 0.23	-0.330 ± 0.066
T_{sl} - M	6.317 ± 0.025	0.0423 ± 0.0065
L_X - M	6.18 ± 0.42	-0.90 ± 0.11
L_X - T_{sl}	5.34 ± 0.52	-1.77 ± 0.16
FO simulation		
Y_X - M	5.683 ± 0.038	0.054 ± 0.014
T_{sl} - M	6.180 ± 0.042	-0.249 ± 0.014
L_X - M	6.334 ± 0.046	0.748 ± 0.015
L_X - T_{sl}	5.85 ± 0.14	0.760 ± 0.050

C_0 is the best-fitting normalisation, and β is the best-fitting slope. β characterises

the evolution of the normalisation; see equations (12) and (13).

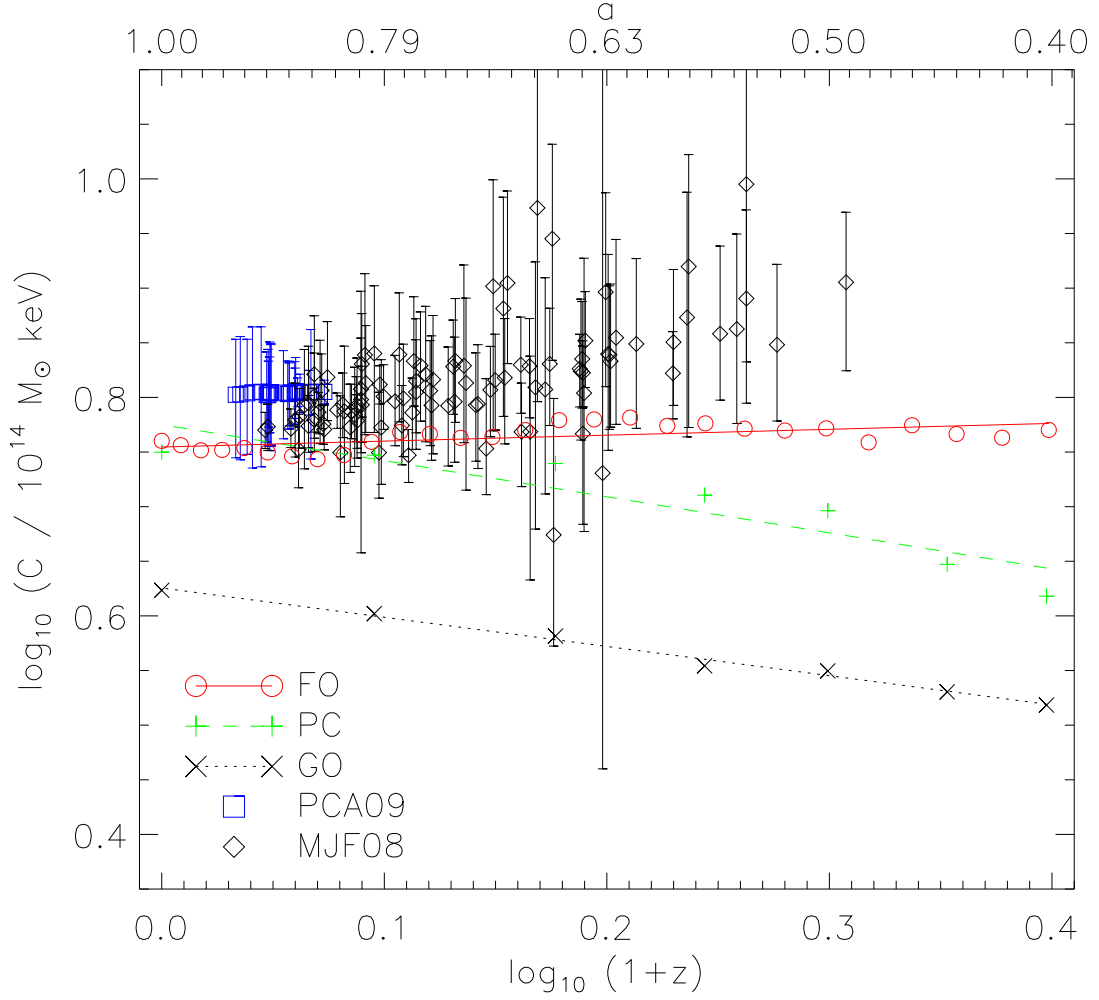


Fig. 10.— Normalisation of the Y_X - M scaling relation as a function of redshift for each of the Millennium Gas simulations. Low-redshift observational data from REXCESS (PCA09) and the high-redshift data of MJF08 is shown for comparison. 1σ error bars are also plotted for the observational data.

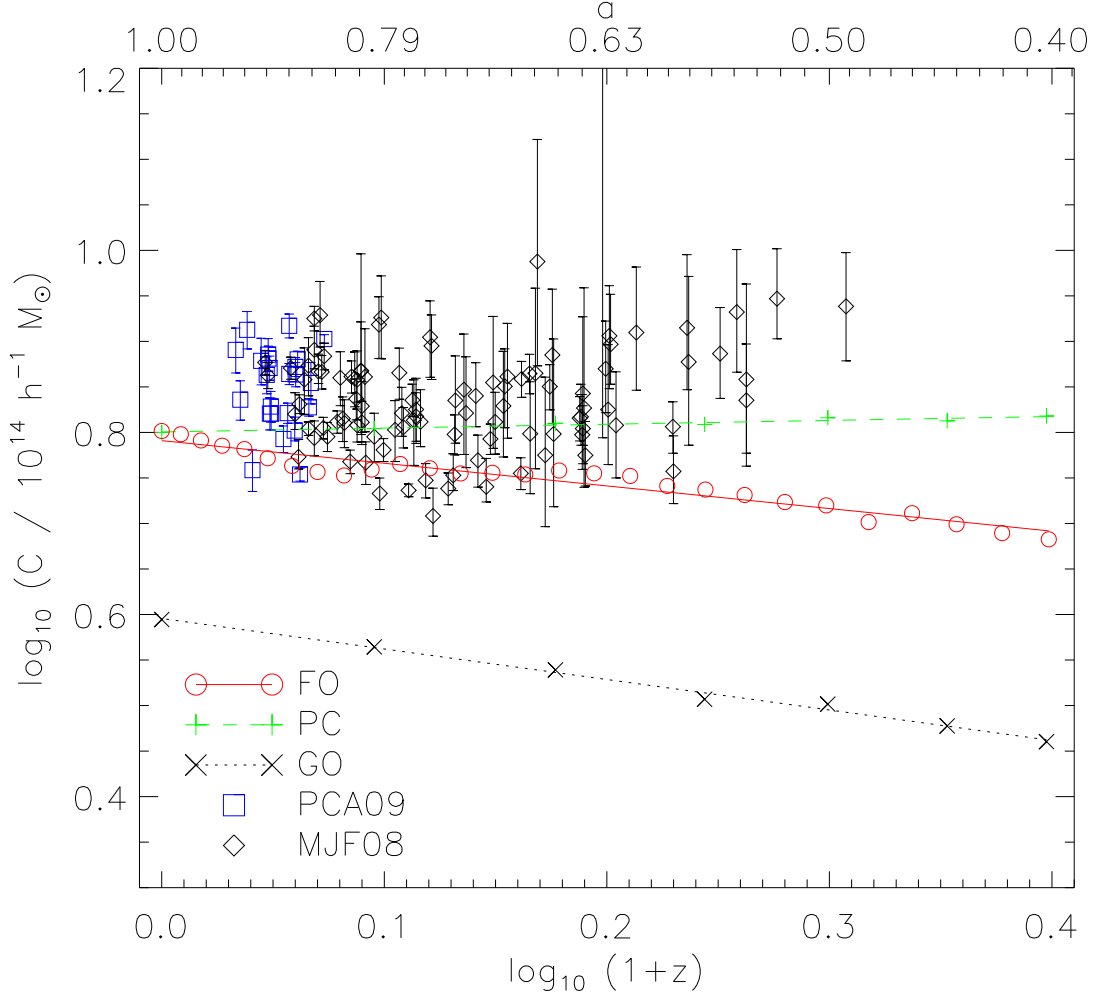


Fig. 11.— Normalisation of the $T_{\text{sI}}\text{-}M$ scaling relation as a function of redshift for each of the Millennium Gas simulations. We also display observational data from PCA09 and MJF08.

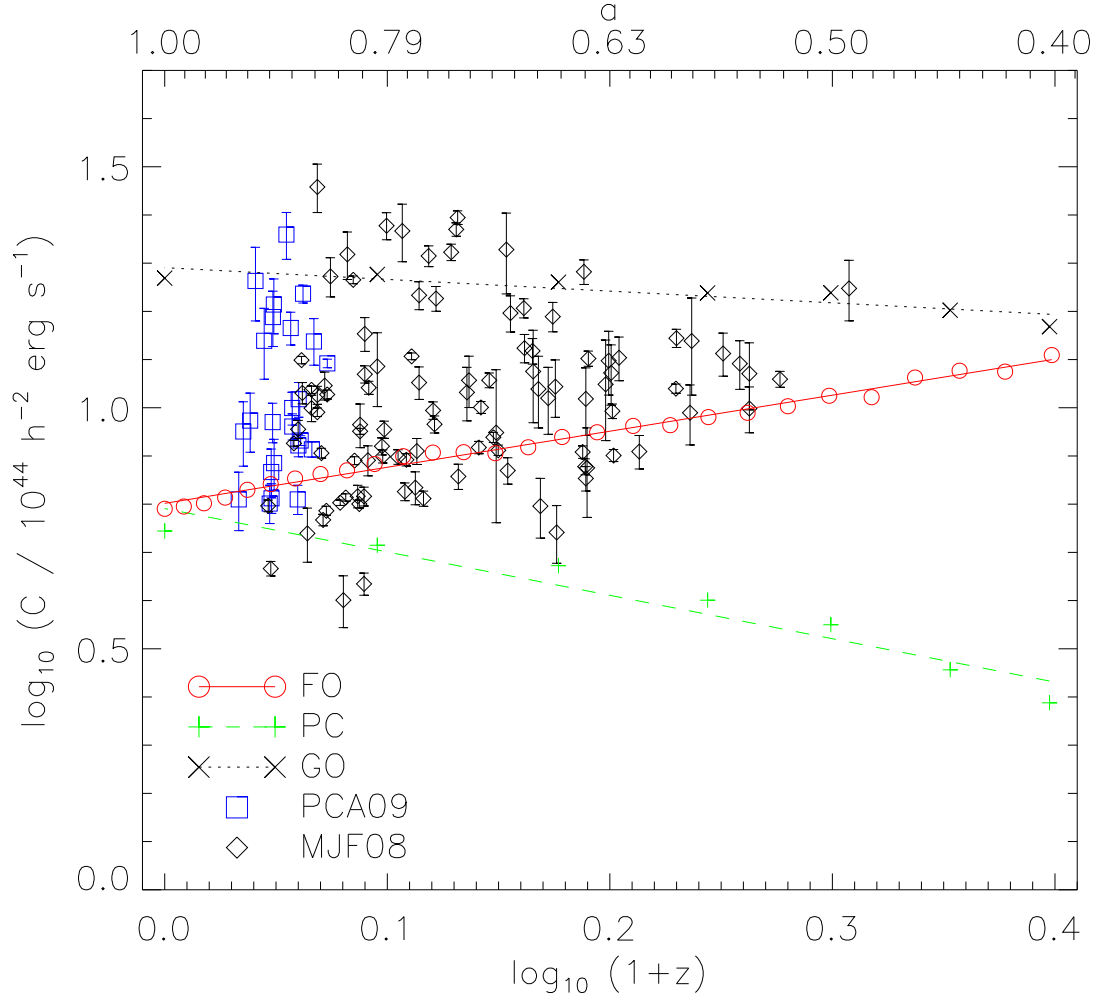


Fig. 12.— Normalisation of the L_X - M scaling relation as a function of redshift for each of the Millennium Gas simulations. For comparative purposes, we plot low and high-redshift observational data from PCA09 and MJF08, respectively.

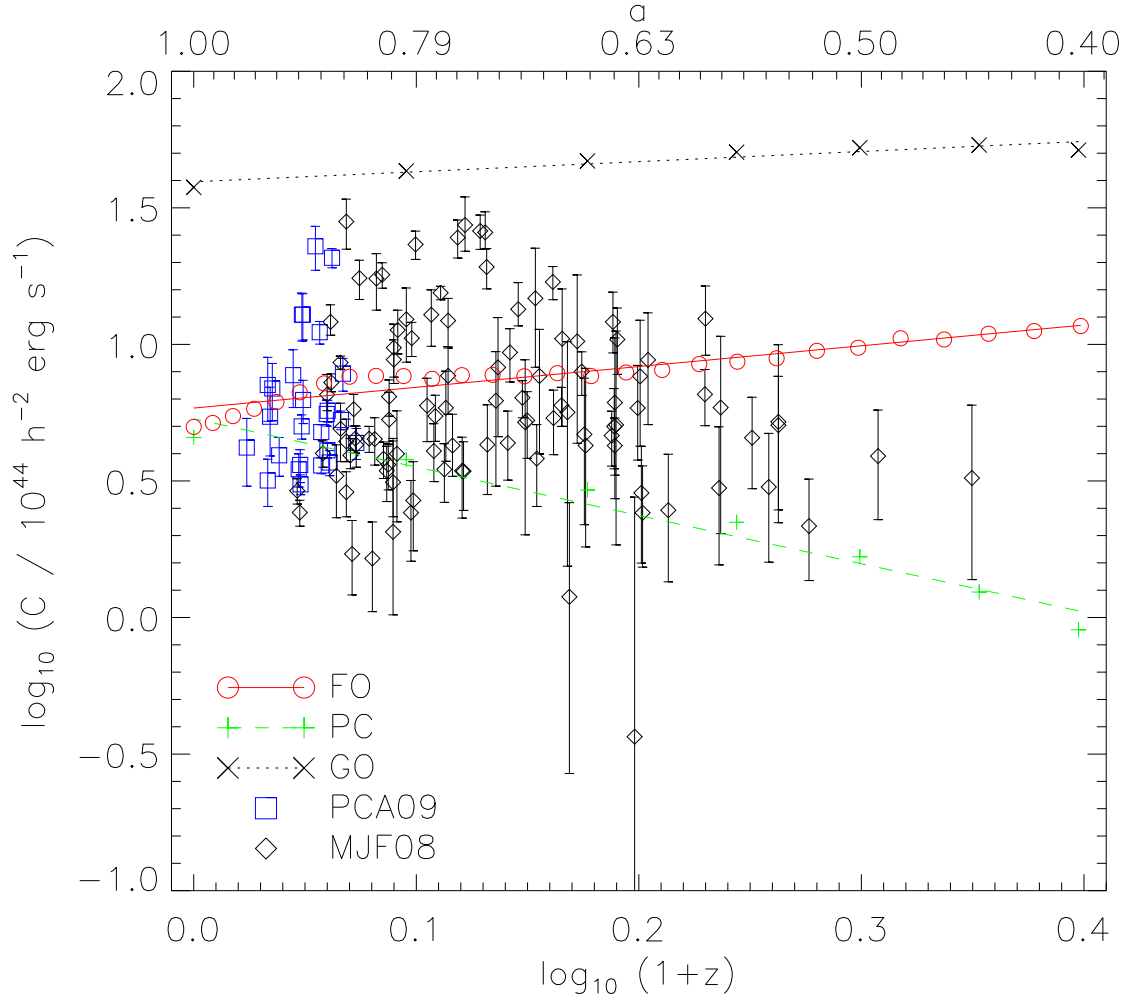


Fig. 13.— Normalisation of the L_X - T_{sl} scaling relation as a function of redshift for each of the Millennium Gas simulations. Data from the observational studies of PCA09 and MJF08 is also shown.

and $\sim 20 - 30\%$, respectively.

Once we have applied this correction, we find that all four scaling relations obtained from the FO run evolve in a manner broadly consistent with the observational data at low to moderate redshifts, $z \lesssim 0.5$. In the case of the L_X - M and L_X - T_{sl} relations, there are hints that the positive evolution predicted by our feedback model provides a better match to the data at these redshifts than the PC model, although the observed scatter is large. Both the PC and FO runs predict similar results for the Y_X - M and T_{sl} - M relations at $z \lesssim 0.5$, and it is not possible to distinguish between the two models with the observational data.

At higher redshift, $z \gtrsim 0.5$, the observational data for the Y_X - M and L_X - M relations seems to follow an upward trend, consistent with the positive evolution expected from our feedback model. The data also suggests that the T_{spec} - M relation evolves in a positive sense at these redshifts, but in this case the PC model provides a better description of the observed evolution than the FO model. The PC model also predicts negative evolution of the L_X - T_{sl} relation for $z \gtrsim 0.5$, consistent with the observational data.

1.5. Conclusions and Discussions

In this report, we set out to investigate the evolution of galaxy cluster X-ray scaling relations using numerical simulations. The evolution of scaling laws is

crucial for constraining cosmological parameters with clusters surveys, and also offers a potentially powerful probe of the cooling and heating processes operating in clusters. Our main objective was to determine how including additional feedback from AGN in simulations affects the predicted evolution, and whether this is consistent with observations. Given that there is a substantial body of observational and theoretical evidence indicating that AGN are key in shaping the properties of galaxy clusters, it is clearly important to address this issue. However, all evolution studies to date have been based on simulations that only incorporate feedback from star formation. Our main conclusions can be summarised as follows.

1. Non-gravitational heating from SNe and AGN in the FO run produces a $z = 0$ cluster population whose radial temperature and entropy profiles broadly agree with those of NCC clusters in the REXCESS sample (PAP10). In particular, the temperature profiles are close to isothermal in the core, and the entropy profiles are significantly flatter in central regions than the theoretical $K \propto r^{1.1}$ scaling observed in cluster outskirts. However, it seems that the entropy of the gas has been raised too much in the core, compared to the observational data. None of our clusters exhibit a gentle drop in temperature at small cluster-centric radii or a steadily declining entropy profile, both of which are characteristic of CC systems. This is because gas cannot lose entropy via radiative cooling in our simulation. We note that fully

self-consistent hydrodynamical simulations tend to suffer from the opposite problem, in the sense that radiative cooling leads to the over-production of cool cores.

2. The Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} scaling relations obtained from the FO run at $z = 0$ generally match the local REXCESS relations (PCA09), once we have accounted for the fact that the observed masses are likely to be biased low by $\sim 10 - 20\%$ due to the assumption of hydrostatic equilibrium. The exception is that we cannot explain the large scatter above the mean L_X - M and L_X - T_{spec} relations seen in the observational data. This is because the source of this scatter is highly X-ray luminous CC systems which are not formed in our simulation.
3. A crude model of non-gravitational heating from astrophysical sources in which the ICM is preheated at $z = 4$, rather than in response to galaxy formation, can produce a population of clusters whose $z = 0$ properties closely resemble those of objects formed in the FO run. In fact, the two model predictions are so similar that they cannot be distinguished using high-quality local observations.
4. Density, temperature and entropy profiles of individual clusters in the FO run all evolve in a self-similar fashion from $z = 1.5$ to $z = 0$, although feedback from galaxies has modified their shape compared to that expected from pure

gravitational heating. We suspect this is linked to the self-regulation of cooling and heating in the underlying model of galaxy formation.

5. The profiles of preheated clusters do not scale self-similarly. This is because the injection of entropy at high-redshift acts to remove gas from central cluster regions, lowering the gas density and increasing its temperature. Following preheating, the properties of the ICM can only be modified by gravitational processes, so the effect of the preheating is gradually erased and cluster profiles will eventually resemble those of clusters that have been subject to gravitational heating only. This ‘recovery’ from preheating is what drives the apparent evolution of cluster profiles relative to the self-similar model.
6. Feedback from galaxy formation in our FO model leads to positive evolution of the Y_X - M , L_X - M and L_X - T_{sl} relations, and negative evolution of the T_{sl} - M relation. By contrast, preheating leads to scaling relations that evolve in the opposite sense. Kay et al. (2007) also reported negative evolution of the L_X - T_{sl} relation using a simulation with a self-consistent stellar feedback scheme. This suggests that additional heating from AGN feedback changes the way in which scaling laws evolve, possibly because AGN heating is still important in cluster cores at low-redshift, long after the peak of star formation. We have investigated whether the evolution predicted by our feedback model is

consistent with X-ray observations of high-redshift clusters. Unfortunately, the large samples of high-redshift clusters currently available are not cleanly selected, which is problematic since it may generate spurious evolution (e.g. Pacaud et al. 2007). This is possibly why different observational studies give contradictory results. Consequently, we have not been able to decide whether our FO model provides a better description of reality than simple preheating. However, it is encouraging that the evolutionary behaviour predicted by the two models is distinct, particularly in the case of the L_X - M and L_X - T_{sl} relations, so that we could potentially distinguish between them, and also other models (such as that of Kay et al. 2007), when higher-quality data becomes available. As an example, the XCS will soon provide the largest ever sample of X-ray clusters selected with well-defined criteria, extending out to $z \approx 1.5$. Likewise, large high-redshift cluster samples are expected from SZ surveys currently underway. With such datasets, a rigorous comparison between theory and observation will become possible, so that we will be able to use the evolution of cluster scaling laws as an additional constraint on models of non-gravitational heating in clusters.

2. Part II

Clusters in homogeneous and inhomogeneous dark energy

It has been almost a decade since cosmologists find some evidence of the existence of dark energy, the most abundant component in the universe. Yet, we do not fully understand what it actually is or how it interacts with matter. The standard scenario is that when cosmic structures are formed, they decouple from the general expansion of the universe and hence excluding from the dark energy component. However, recently cosmologists start to look into how dark energy plays a role in formation of structures. There are many questions of the mysterious dark energy to be answered still. Currently, what theorists like to do now is to explore possibilities of how to identify the most probable model of what dark energy could be. Studies of structure formation are one of those possibilities.

In this report, we will present what has been studied on the formation of structures under the influence of dark energy. We initially focus on the work by Maor and Lahav (2005), Percival (2005) and Wang (2006), and we extend further. The report is structured as followed. We first discuss virialisation conditions in general by forming necessary equations. Then we look into how including the dark energy component affects the virialisation of halos in comparison to what is expected in Einstein-de Sitter universe. The parts previously described were conducted under the support of the Toray Thailand Science Foundation (TTSF), a

year prior to the support of the TRF and the CHE. The work forms the foundation of the current project and it is essential to reiterate here in order to fully describe the work homogeneously. Towards the end of this part, we will show the effect of dark energy in clustering has on cluster scales. However, some more work is required in the future to have a consistent conclusion.

2.1. Potential energy

We will start with discussing Poisson equation. In Newtonian physics, the Poisson equation is

$$-\nabla^2\Phi = 4\pi G\rho, \quad (14)$$

where Φ is the potential, G is the universal gravitational constant and ρ is the matter density. The potential within a radius of R as felt by a particle at a distance r is

$$\Phi = -2\pi G\rho(R^2 - \frac{r^2}{3}). \quad (15)$$

In the relativistic case, however, the potential at r within a radius R encompassing the energy component x , whose density and pressure are ρ_x and p_x , respectively, can be written as

$$\Phi_x(r) = -2\pi G\rho_x(1 + 3w)(R^2 - \frac{r^2}{3}), \quad (16)$$

where w is the equation of state, $w = p_x/\rho_x$. The term $1 + 3w$ comes from the consideration from energy-momentum tensor as in Copeland et. al. (2006). The

potential energy of this energy component, U_x is the integral over volume

$$U_x = \frac{1}{2} \int \rho_{\text{tot}} \Phi_x dV, \quad (17)$$

$$= 2\pi\rho_{\text{tot}} \int_0^R \Phi_x r^2 dr, \quad (18)$$

where ρ_{tot} is the density of all components. Thus, we can substitute Φ_x of equation 16 in equation 18 and obtain that

$$U_x = -\frac{4}{5}\pi G\rho_x MR^2(1+3w), \quad (19)$$

where the mass, M , is $(4/3)\pi\rho_{\text{tot}}R^3$. If one considers matter alone, $w = 0$, the potential energy is $-(3/5)GM^2/R$.

2.2. Virialisation conditions

2.2.1. Single component system

To investigate virialisation, we consider a spherical collapse. We start with a collapse of a single component, that is matter, first. Once a halo decouples from general evolution of the universe, it expands to reach a turnaround and then collapses to the point that the halo becomes virialised and stable. From virial theorem, a structure is virialised under this condition

$$T_{\text{vir}} = \frac{1}{2}R \left. \frac{\partial U}{\partial R} \right|_{\text{vir}}, \quad (20)$$

where T_{vir} is the kinetic energy. At turnaround, the kinetic energy is zero, $T_{ta} = 0$, thus from energy conservation we can obtain that the potential energy at turnaround, U_{ta} , is

$$U_{ta} = \left[U + \frac{1}{2} R \frac{\partial U}{\partial R} \right]_{vir}. \quad (21)$$

In an Einstein-de Sitter universe, $U = -(3/5)GM^2/R$, thus

$$\begin{aligned} \left[U + \frac{1}{2} R \frac{\partial U}{\partial R} \right]_{vir} &= -\frac{3}{5} G \frac{M}{R_{vir}} + \left[\frac{1}{2} R \left(-\frac{3}{5} GM \right) \left(\frac{-1}{R^2} \right) \right]_{vir} \\ -\frac{3}{5} G \frac{M}{R_{ta}} &= -\frac{3}{5} GM \left(\frac{1}{R_{vir}} - \frac{1}{2R_{vir}} \right) \\ \frac{R_{vir}}{R_{ta}} &= \frac{1}{2}, \end{aligned} \quad (22)$$

where R_{vir} and R_{ta} are virial and turnaround radius, respectively. We shall see later how this ratio changes when we include dark energy component in the collapse.

2.3. Two-component system

We will now allow the dark energy component to play a role in virialisation of structures. We will call this component Q , for quintessence. Before working out the virialisation condition, let us now determine evolution of density components, starting with continuity equation,

$$\dot{\rho} + 3(1+w)\frac{\dot{r}}{r}\rho = 0. \quad (23)$$

For a homogeneous Q -component,

$$\rho_{Qc} \dot{a} + 3(1+w)\frac{\dot{a}}{a}\rho_{Qc} = 0, \quad (24)$$

where ρ_{Qc} and a are the dark energy density in a cluster and global scale factor, respectively. For clustering dark energy,

$$\rho_{\dot{Q}c} + 3(1+w)\frac{\dot{r}}{r}\rho_{Qc} = 0, \quad (25)$$

where r is the local scale factor. In order to control the clustering, Mota and van de Bruck (2004) suggest there is a clustering parameter γ which can be incorporated in the continuity equation as

$$\rho_{\dot{Q}c} + 3(1+w)\frac{\dot{r}}{r}\rho_{Qc} = \gamma\Gamma, \quad (26)$$

where

$$\Gamma = 3(1+3w)\left[\frac{\dot{r}}{r} - \frac{\dot{a}}{a}\right]\rho_{Qc}, \quad (27)$$

where the clustering parameter is between zero and 1, dark energy component being clustered and homogeneous, respectively. As for the density evolution of matter component in a cluster, it is obviously

$$\rho_{\dot{m}c} + 3\frac{\dot{r}}{r}\rho_{mc} = 0, \quad (28)$$

and the acceleration equation of the two components is

$$\frac{\ddot{r}}{r} = -\frac{4}{3}\pi G(\rho_{mc} + (1+3w)\rho_{Qc}). \quad (29)$$

We have now formed all equations required to work out the virialisation condition for structures in dark energy cosmology. The potential energy contributed by the

two components is,

$$U_{\text{tot}} = \frac{1}{2} \int \rho_{\text{tot}} \Phi_{\text{tot}} dV \quad (30)$$

$$= \frac{1}{2} \int (\rho_m + \rho_Q)(\Phi_m + \Phi_Q) dV, \quad (31)$$

where the potentials of the matter and dark energy component are Φ_m and Φ_Q ,

repsectively, are

$$\Phi_m = -2\pi G \rho_m (R^2 - \frac{r^2}{3}), \quad (32)$$

$$\Phi_Q = -2\pi G (1 + 3w) \rho_Q (R^2 - \frac{r^2}{3}). \quad (33)$$

Substitute the potentials in equation 31 and we can obtain,

$$U_{\text{tot}} = -\frac{16}{15} \pi^2 G R^5 (\rho_m^2 + (2 + 3w) \rho_m \rho_Q + (1 + 3w) \rho_Q^2). \quad (34)$$

For clustered quintessence, the continuity equations for matter and dark energy

components in cluster are,

$$\dot{\rho}_{mc} + 3 \frac{\dot{r}}{r} \rho_{mc} = 0, \quad (35)$$

$$\dot{\rho}_{Qc} + 3 \frac{\dot{r}}{r} \rho_{Qc} = 0, \quad (36)$$

and we can obtain that $\rho_{mc} = \tilde{\rho}_{mc} r^{-3}$, $\rho_{Qc} = \tilde{\rho}_{Qc} r^{-3(1+w)}$, where $\tilde{\rho}_{mc}$ and $\tilde{\rho}_{Qc}$ are

constants. From the total potential energy and virialisation condition, we have

$$\begin{aligned} U_{\text{vir}} + T_{\text{vir}} &= -\frac{16}{15} \pi^2 G \left(\frac{\tilde{\rho}_{mc}^2}{2r_{\text{vir}}} + (2 + 3w)(1 - 3w) \tilde{\rho}_{mc} \tilde{\rho}_{Qc} \frac{1}{2r_{\text{vir}}^{(1+3w)}} \right. \\ &\quad \left. + (1 + 3w)(1 - 6w) \tilde{\rho}_{Qc}^2 \frac{1}{2r_{\text{vir}}^{(1+6w)}} \right), \end{aligned} \quad (37)$$

$$\begin{aligned}
U_{ta} = & -\frac{16}{15}\pi^2 G \left(\frac{\tilde{\rho}_{mc}^2}{r_{ta}} + (2+3w)\tilde{\rho}_{mc}\tilde{\rho}_{Qc} \frac{1}{r_{ta}^{(1+3w)}} \right. \\
& \left. + (1+3w)\tilde{\rho}_{Qc}^2 \frac{1}{2r_{vir}^{(1+6w)}} \right). \tag{38}
\end{aligned}$$

At turnaround, let $q = \rho_{Qc}/\rho_{mc}$ and $x = r_{vir}/r_{ta}$, thus we can rewrite equations 37 and 38 as

$$\begin{aligned}
U_{vir} + T_{vir} = & -\frac{16}{15}\pi^2 G \frac{\rho_{mc}^2}{2r_{vir}} (1 + (2+3w)(1-3w)qx^{-3w} + \\
& (1+3w)(1-6w)q^2x^{-6w}) \tag{39}
\end{aligned}$$

$$\begin{aligned}
U_{ta} = & -\frac{16}{15}\pi^2 G \frac{\rho_{mc}^2}{r_{ta}} (1 + (2+3w)(1-3w)qx^{(-3w)} \\
& + (1+3w)(1-6w)q^2x^{-6w}). \tag{40}
\end{aligned}$$

From the energy conservation, equating the two equations above and one obtains,

$$\frac{1}{2} = (1+(2+3w)q+(1+3w)q^2)x - \frac{1}{2}(2+3w)(1-3w)qx^{-3w} - \frac{1}{2}(1+3w)(1-6w)q^2x^{-6w} \tag{41}$$

For matter only to virialise, we can repeat the above procedure and obtain the following,

$$U = \frac{1}{2} \int (\rho_m + \rho_Q) \Phi_m dV \tag{42}$$

$$= -\frac{16}{15}\pi^2 G \tilde{\rho}_{mc}^2 (r^{-1} + \frac{\tilde{\rho}_{Qc}}{\tilde{\rho}_{mc}} r^{-(1+3w)}) \tag{43}$$

$$U_{ta} = -\frac{16}{15}\pi^2 G \frac{\tilde{\rho}_{mc}^2}{r_{ta}} (1 + qr_{ta}^{-3w}) \tag{44}$$

$$T_{vir} + U_{vir} = -\frac{16}{15}\pi^2 G \frac{\tilde{\rho}_{mc}^2}{r_{vir}} \left(\frac{1}{2} + \frac{(1-3w)}{2} qx^{-3w} \right) \tag{45}$$

$$(1+q)x - \frac{q}{2}(1-3w)x^{-3w} = \frac{1}{2}. \tag{46}$$

In Figure 14, we show that for the case of fully clustered quintessence ($\gamma = 0$) with $w = -0.8$, the ratio between turnaround and virial radii as a function of ρ_{Qc}/ρ_{mc} starts off at 0.5, the standard value in Einstein-de Sitter universe, and decreases when we allow only matter to virialise (solid line), while when both components are allowed to virialise the radii ratio increases. Thus, this contrasting behavior is indeed very interesting to help one discriminate one scenario from the other, given that we know how to obtain the turnaround radii in real observation. In the favoured model, if we concentrate on only virialising matter, the ratio of the radii in a universe with a cosmological constant ($w = -1$) is even less than that with $w = -0.8$, as in Figure 15.

In the case of unclustered quintessence, $\gamma \neq 0$, one can obtain the generalised form for the above equation as,

$$\begin{aligned}
& \frac{1}{2}(1 - 2x + q(2 + 3w)) \left(\frac{1}{x}\right)^{-3(w(-1+\gamma)+\gamma)} \left(-\left(\frac{a_{ta}}{a_{vir}}\right)^{3(1+w)\gamma} + 2\left(\frac{1}{x}\right)^{3(1+w)\gamma}\right. \\
& - 2\left(\frac{1}{x}\right)^{-1+3w(-1+\gamma)+3\gamma} + 3\left(\frac{a_{ta}}{a_{vir}}\right)^{3(1+w)\gamma} w(-1 + \gamma) + 3\left(\frac{a_{ta}}{a_{vir}}\right)^{3(1+w)\gamma} \gamma) \\
& + q^2(1 + 3w) \left(\frac{1}{x}\right)^{-6(w(-1+\gamma)+\gamma)} \left(-\left(\frac{a_{ta}}{a_{vir}}\right)^{6(1+w)\gamma} + 2\left(\frac{1}{x}\right)^{6(1+w)\gamma}\right. \\
& - 2\left(\frac{1}{x}\right)^{-1+6w(-1+\gamma)+6\gamma} + 6\left(\frac{a_{ta}}{a_{vir}}\right)^{6(1+w)\gamma} w(-1 + \gamma) + \\
& \left. 6\left(\frac{a_{ta}}{a_{vir}}\right)^{6(1+w)\gamma} \gamma\right) = 0
\end{aligned}$$

In Figure 16, we demonstrate how the radii ratio relates to the degree of quintessence clustering at different values of q or ρ_{Qc}/ρ_{mc} at turnaround.

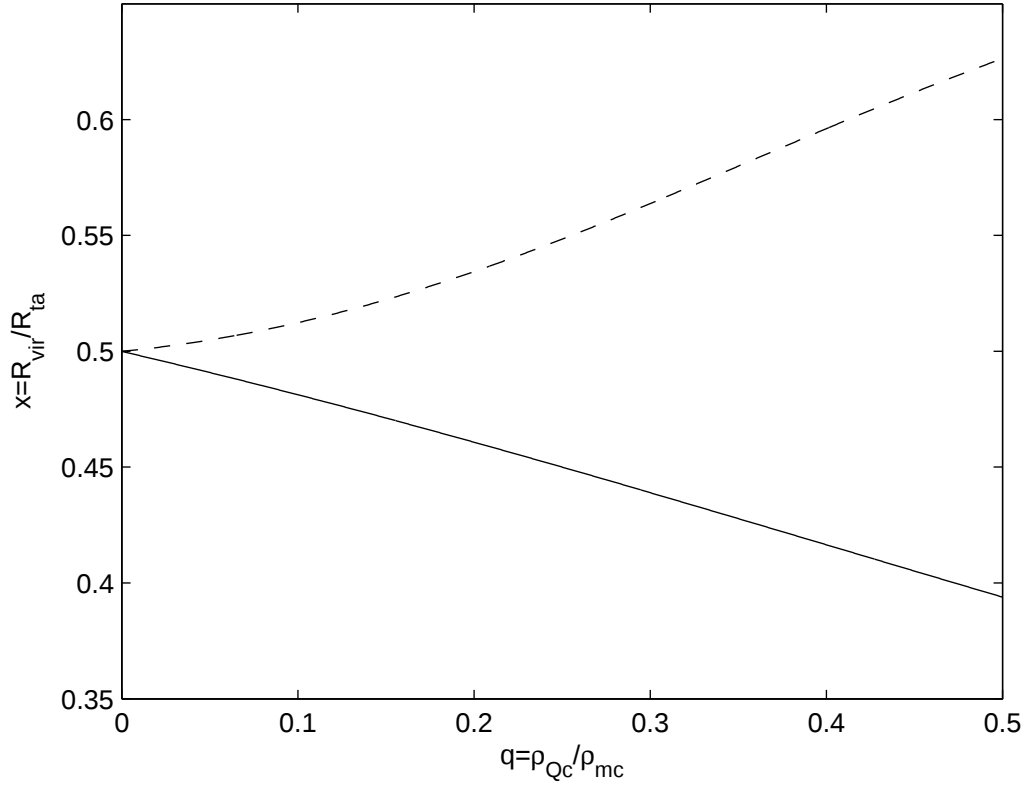


Fig. 14.— The ratio between turnaround and virial radii as a function of ρ_{Qc}/ρ_{mc} when we allow only matter the virialise (solid line) and both components to virialise (dashed line) with a constant equation of state $w = -0.8$.

2.4. Results/Discussions

The main interest of this project concerns exploiting observable properties of galaxy clusters to study their manifestations due to a range dark energy models, in particular, when one considers the possibility of the dark energy being

inhomogeneous, as well as the usual homogeneous model. One parameter which is of interest for both observation and theoretical aspects is the NFW concentration parameter. This parameter is proposed by Navarro et al. (1997), hence the name NFW. The concentration parameter c_{vir} is defined as $c_{vir} = r_{vir}/r_s$ where r_{vir} is the virial radius and r_s is the characteristic radius, and this is a parameter in the NFW dark matter halo profile given as :

$$\rho_{NFW}(r) = \frac{\rho_s}{(r/r_s)(1 + r/r_s)^2}, \quad (47)$$

where ρ_s is the characteristic density. These parameters in observed clusters will rely on assuming models relating observable hot plasma and dark matter distribution. Following the method proposed by Eke et al (2000), one can calculate c_{vir} , which is the NFW concentration parameter and is defined as

$$c_{vir}^3 = \frac{\Delta_{vir}(z_c)\Omega_m(z_o)(1 + z_c)^3}{\Delta_{vir}(z_o)\Omega_m(z_c)(1 + z_o)^3}, \quad (48)$$

where z_c, z_o are collapsed and observed redshift, Δ_{vir} is the density contrast of matter density with respect to the critical density. In our analytical work, we are able to calculate the overdensity where we define it to be the ratio between the matter density with respect to the background matter density. To avoid confusion, we define this parameter as Δ_{vir*} and we can theoretically calculate this as follows

$$\Delta_{vir*} = \frac{\zeta}{x^3} \left(\frac{a_c}{a_{ta}} \right)^3, \quad (49)$$

where ζ is the ratio between the densities of matter in the cluster and background matter at turnaround. The parameter ζ can be calculated directly as in Wang

(2006)

$$\zeta = \frac{\Omega_{Q,0}(1+z_{ta})^{3w}}{q\Omega_{m,0}}, \quad (50)$$

while this parameter was also given a fitting formula by it Wang & Steinhardt (1998) for constant equation of state as,

$$\zeta = \left(\frac{3\pi}{4}\right)^2 \Omega_{m,ta}^{-0.79+0.26\Omega_{m,ta}-0.06w}. \quad (51)$$

While the density contrast, Δ_{vir} , and overdensity, Δ_{vir*} , are reasonable (as shown in Figure 17), the calculated NFW concentration from both equations 50 and 51, show significant discrepancy as in Figure 18. The values given from ζ as calculated in equation 50 are far too low than from equation 51. This must be investigated further as the concentration parameter can provide a base test to see how dark matter is distributed in the clusters. No work in the literature to date has shown the results of varying γ or the strength of clustering γ of the corresponding cluster global parameters. This is the first attempt which remains to be explored in the hope that one can relate this theoretical picture of dark energy behaviour in cluster scale to real observations. The current implication at this time is that the behaviour of dark energy will alter the definition of the boundary of clusters. If this is to be true, then it will have strong impact on the use of clusters of galaxies as a tool to constrain cosmological model.

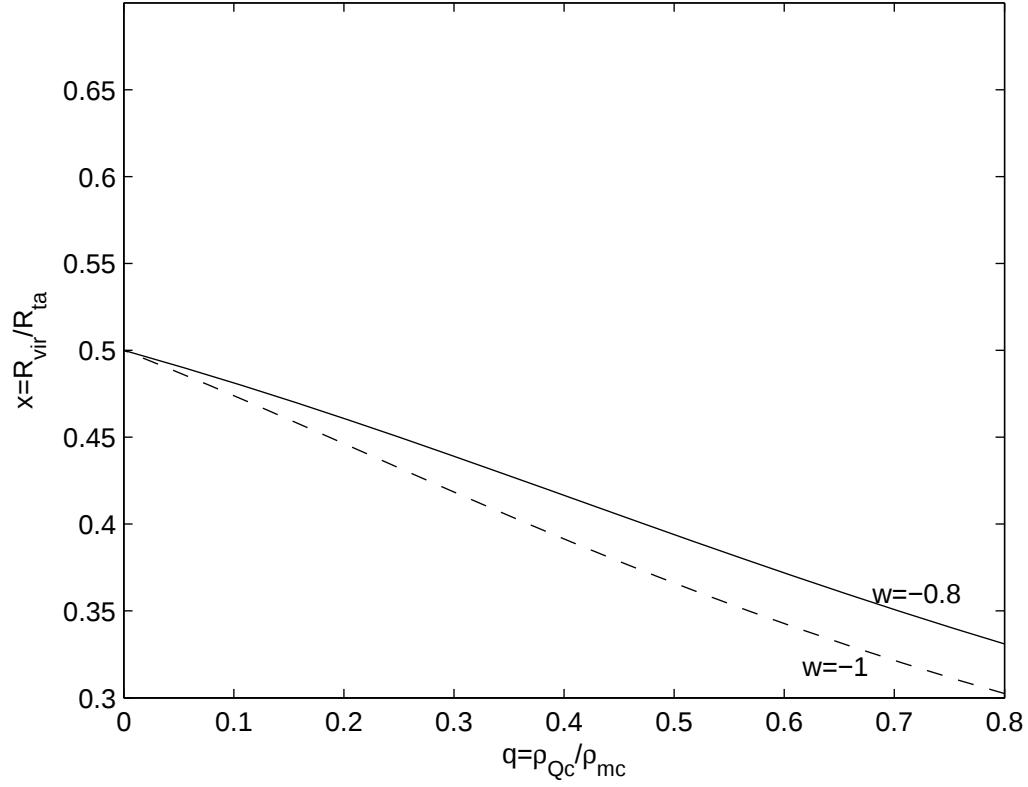


Fig. 15.— The ratio between turnaround and virial radii as a function of ρ_{Qc}/ρ_{mc} when we allow only matter the virialise with constant equation of states being $w = -0.8$ (solid line) and -1 (dashed line).

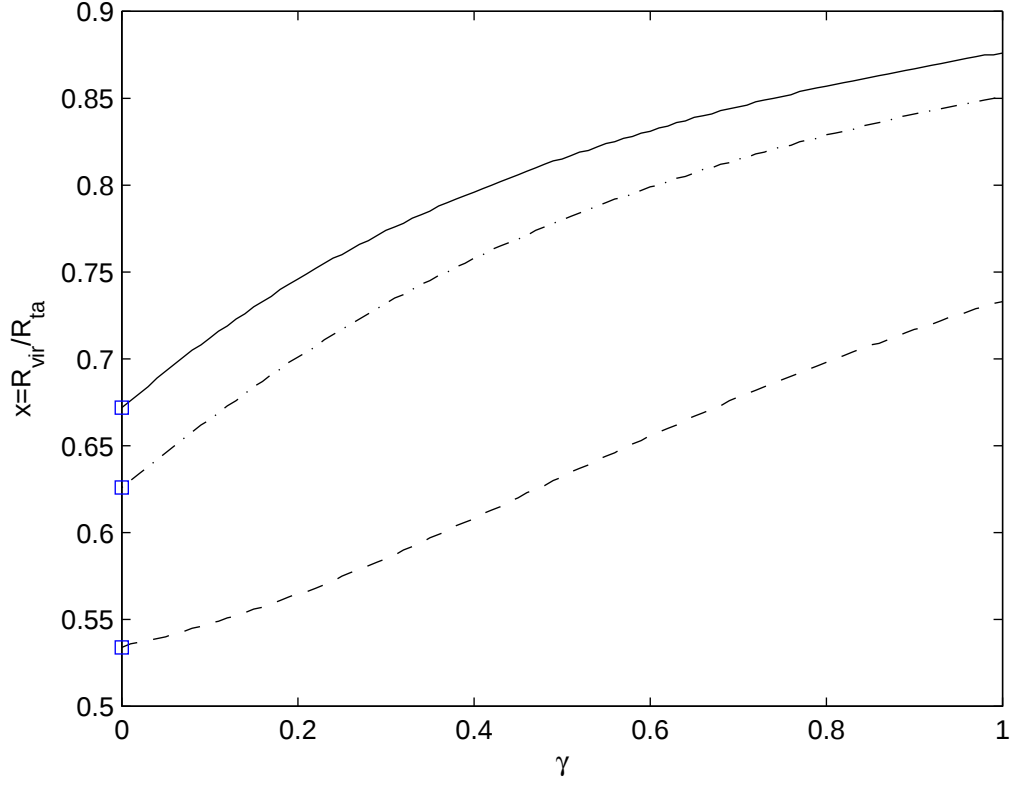


Fig. 16.— Ratio between turnaround and virial radii as a function of γ , ranging from clustered to unclustered quintessence ($\gamma = 0 \rightarrow 1$) for $\rho_{Qc}/\rho_{mc} = 0.2, 0.5$ and 0.7 (dotted, dotted-dash and solid line, respectively), assuming $a_{ta}/a_{vir} = 0.67$. Boxes show values that agree with Maor & Lahav (2005) results.

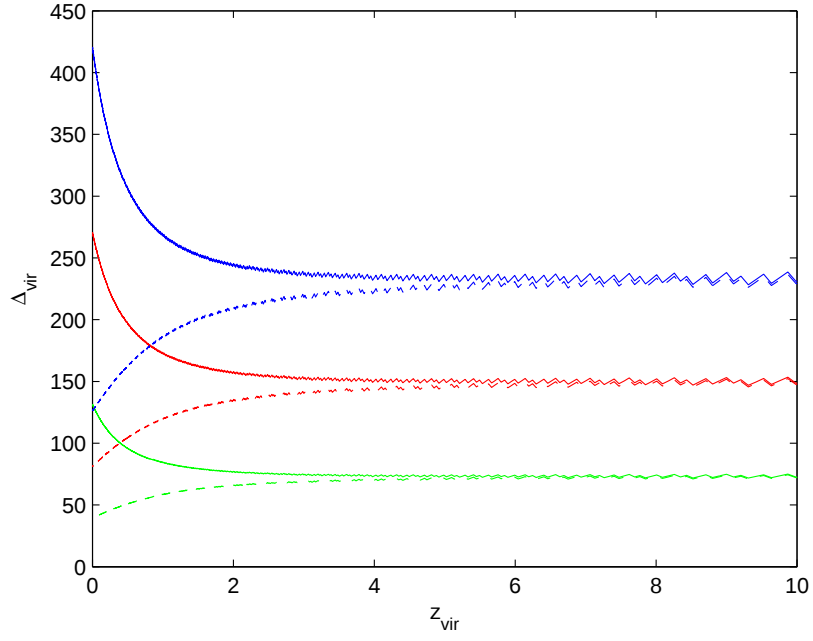


Fig. 17.— Various Δ for only matter virialises (top pair), for $\gamma = 0.7$ with $q = 0.2$ (middle pair) and for $\gamma = 0$ (bottom pair). Dashed lines are those of NFW definition, solid of the analytic solution.

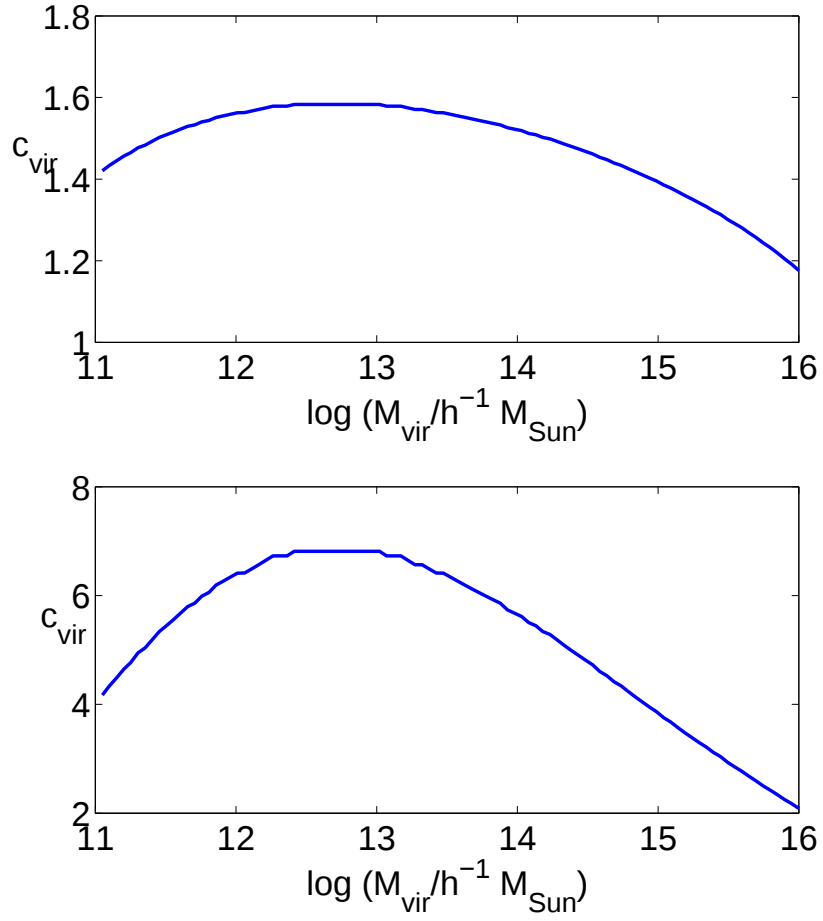


Fig. 18.— The concentration parameters calculated from equation 50 (top panel) and equation 51 (bottom panel). The clusters are observed at $z = 0$.

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The evolution of galaxy cluster X-ray scaling relations

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ABSTRACT

We use numerical simulations to investigate, for the first time, the joint effect of feedback from supernovae (SNe) and active galactic nuclei (AGN) on the evolution of galaxy cluster X-ray scaling relations. Our simulations are drawn from the Millennium Gas Project and are some of the largest hydrodynamical N -body simulations ever carried out. Feedback is implemented using a hybrid scheme, where the energy input into intracluster gas by SNe and AGN is taken from a semi-analytic model of galaxy formation. This ensures that the source of feedback is a population of galaxies that closely resembles that found in the real Universe. We show that our feedback model is capable of reproducing observed local X-ray scaling laws, at least for non-cool-core clusters, but that almost identical results can be obtained with a simplistic preheating model. However, we demonstrate that the two models predict opposing evolutionary behaviour. We have examined whether the evolution predicted by our feedback model is compatible with observations of high-redshift clusters. Broadly speaking, we find that the data seem to favour the feedback model for $z \lesssim 0.5$, and the preheating model at higher redshift. However, a statistically meaningful comparison with observations is impossible, because the large samples of high-redshift clusters currently available are prone to strong selection biases. As the observational picture becomes clearer in the near future, it should be possible to place tight constraints on the evolution of the scaling laws, providing us with an invaluable probe of the physical processes operating in galaxy clusters.

Key words: hydrodynamics – methods: numerical – galaxies: clusters: general – galaxies: clusters: intracluster medium – X-rays: galaxies: clusters.

1 INTRODUCTION

Galaxy cluster surveys are a potentially powerful means of placing tight constraints on key cosmological parameters, independent of other methods such as the measurement of cosmic microwave background anisotropies. This is primarily because the mass function of galaxy clusters is highly sensitive to different choices of model parameters. It is therefore essential to determine how the mass function varies with redshift if we are to exploit clusters as a cosmological probe. This is not trivial since the total masses of galaxy clusters must first be inferred from their observable properties.

Mass estimates can be derived from X-ray observations of the hot, diffuse intracluster medium (ICM) by assuming that the gas is in hydrostatic equilibrium within the cluster gravitational potential well (e.g. Sarazin 1988). However, this requires the accurate determination of gas density and temperature profiles out to large radii.

Although this has become common practice for low-redshift clusters with the advent of the *Chandra* and *XMM-Newton* satellites, measuring high-quality profiles of distant clusters requires long observation times, so hydrostatic mass estimates have only been made for a small number of high-redshift clusters. Furthermore, the assumption of hydrostatic equilibrium only applies to dynamically relaxed systems, so this technique cannot be applied to unbiased cluster samples.

In cases where a hydrostatic estimate is not possible, cluster masses can be inferred from the relationships that exist between X-ray observables, like luminosity, L_X , temperature, T , and the total mass, M . These scaling relations are predicted by the simple self-similar model of cluster formation, where the ICM is heated solely by gravitational processes, such as adiabatic compression and shocks induced by supersonic accretion (Kaiser 1986). However, the observed L_X – M relation is steeper than expected from gravitational heating alone (e.g. Reiprich & Böhringer 2002; Chen et al. 2007; Vikhlinin et al. 2009; Pratt et al. 2009, hereafter PCA09), as is the L_X – T relation (e.g. Markevitch 1998; Arnaud & Evrard 1999; Wu,

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Xue & Fang 1999; Ettori, De Grandi & Molendi 2002; PCA09). This departure from self-similarity is due to an excess of entropy¹ in cluster cores (Ponman, Cannon & Navarro 1999; Lloyd-Davies, Ponman & Cannon 2000; Finoguenov et al. 2002). This extra entropy prevents gas from being compressed to high densities, reducing its X-ray emissivity compared to the self-similar prediction. The effect will be more pronounced in galaxy groups since they have shallower potential wells, leading to a steepening of the L_X – M relation (and L_X – T relation) as desired. The main physical processes thought to be responsible for boosting the entropy of the ICM are heating from astrophysical sources, such as supernovae (SNe) and active galactic nuclei (AGN), and the removal of low-entropy gas via radiative cooling (see Voit 2005 for a review).

Unfortunately, scaling relations are not a perfect means of converting from X-ray observables to mass because of their intrinsic scatter. The dominant source of scatter about relations involving L_X is the dense, highly X-ray luminous central regions of cool-core (CC) clusters (e.g. O’Hara et al. 2006; Chen et al. 2007). One way of reducing this scatter is simply to exclude the core region from the measurements (e.g. Markevitch 1998). Another source of scatter is cluster mergers, which can cause clusters to shift (approximately) along the L_X – T relation, but away from the M – T relation (Rowley, Thomas & Kay 2004; Kravtsov, Vikhlinin & Nagai 2006). However, Kravtsov et al. (2006) recently demonstrated that the quantity Y_X , defined as the product of the gas mass M_{gas} and the X-ray temperature, is extremely tightly correlated with total mass and is insensitive to cluster mergers. This result has been confirmed by independent numerical simulations (Poole et al. 2007) and several observational studies (Arnaud, Pointecouteau & Pratt 2007; Maughan 2007; Vikhlinin et al. 2009), suggesting that reliable cluster mass estimates can indeed be derived from simple observables.

Given that scaling relations enable us to estimate the masses of clusters with poor quality X-ray data, it is clearly vital to ensure that they are well calibrated over a wide redshift range, so we can improve cosmological constraints derived from the mass function. Furthermore, measuring the evolution of X-ray scaling laws should reveal information on the nature of the non-gravitational heating and cooling processes responsible for shaping galaxy clusters (Muanwong, Kay & Thomas 2006).

At low redshift, scaling relations are reasonably well calibrated, at least for relaxed clusters, since reliable hydrostatic mass estimates are readily available. Measuring these relations at high redshift is considerably more challenging, with fewer results available in the literature. As will become clear from the following brief review, the observational picture is far from settled at present.

Ettori et al. (2004a) used a sample of 28 galaxy clusters with $0.4 < z < 1.3$ to measure the M – T , L_X – M and L_X – T relations. Upon comparing their high-redshift M – T relation with local counterparts, they found that the normalization evolved in a manner well described by the self-similar model. By contrast, the normalization of both the high-redshift L_X – M and L_X – T relations was lower than expected from self-similar scaling arguments. Negative evolution² of the L_X – T relation was also reported by Hilton et al. (2007), based on

XMM-Newton observations of a single cluster at $z = 1.457$. Another study was performed by Maughan et al. (2006) who used a sample of 11 clusters in the redshift range $0.6 < z < 1$. They concluded that there is no evidence for any evolution of the M – T , L_X – M and L_X – T relations beyond that anticipated from self-similar theory. Similar results for the L_X – T relation were also found by Vikhlinin et al. (2002) and Lumb et al. (2004). However, such analyses often rely on simplifying assumptions, like isothermal temperature profiles and β -model profiles for the gas density, which can lead to large biases in the mass determination (e.g. Markevitch & Vikhlinin 1997).

A different approach was adopted by Morandi, Ettori & Moscardini (2007), whose sample consisted of 24 clusters in the redshift range $0.14 < z < 0.82$. For each object in their sample, they used the measured gas density profile and the equation of hydrostatic equilibrium to determine the best-fitting temperature profile by varying the free parameters in the assumed model for the dark matter density profile. In conflict with most of the results discussed above, they reported slight negative evolution of the M – T and L_X – M relations, and positive evolution of the L_X – T relation.

More recently, small samples of distant clusters (~ 10 objects) with hydrostatic mass estimates have been used to measure the Y_X – M (Maughan 2007), M – T (Kotov & Vikhlinin 2005, 2006) and L_X – T (Kotov & Vikhlinin 2005) relations at high-redshift ($z \sim 0.7$). The evolution of the normalization of the Y_X – M and M – T relations was again found to be consistent with the self-similar model. On the other hand, the L_X – T relation exhibited positive evolution, consistent with the results of Morandi et al. (2007), but not the negative evolution measured by Ettori et al. (2004a) and Hilton et al. (2007). Beyond $z \sim 0.7$, there are very few clusters with a hydrostatic mass estimate; a notable exception is the $z = 1.05$ object discovered by Maughan et al. (2008a), who demonstrated that the position of this cluster on the high-redshift Y_X – M , M – T and L_X – M relations can be explained by self-similar scaling arguments.

Although several observational studies indicate that the self-similar model provides an adequate description of the evolution of X-ray scaling relations, Voit (2005) suggests that self-similar evolution cannot persist to arbitrarily high redshift, because of the increasing importance of radiative cooling and feedback from galaxy formation. An example of an observational result that supports this argument is that of Branchesi et al. (2007). Using a sample of 39 distant clusters ($0.25 < z < 1.3$), they found that the evolution of the L_X – T relation is comparable with the self-similar prediction for $0 < z < 0.3$, but negative at higher redshifts.

One reason for the lack of concordance between different observational studies is inconsistent cluster selection. With current heterogeneous archival cluster samples, it is very difficult to account for selection biases, which may vary from sample to sample and can mimic evolution. An attempt to quantify the impact of selection effects on the evolution of scaling relations was made by Pacaud et al. (2007), who focused on the L_X – T relation. From an analysis of their raw data, they found evidence for non-monotonic evolution, at odds with the self-similar prediction. However, after taking selection effects into account, they found that the evolution of the L_X – T relation was consistent with self-similar scaling, although this was a tentative result because of poor statistics. Nevertheless, the salient point to take from their work is that modelling the full source-selection process can drastically alter the measured evolution, so we must seriously question any attempt to assess the evolution of X-ray scaling laws that does not attempt to do this. In more recent work, Mantz et al. (2010a,b) have developed a method

¹ We define entropy as $K = k_B T / n_e^{\gamma-1}$, where k_B is Boltzmann’s constant, n_e is the electron number density and $\gamma = 5/3$ is the ratio of specific heats for a monoatomic ideal gas.

² Throughout this work, we consider the evolution of scaling relations relative to that predicted by the self-similar model. Given a particular scaling law, we say there is negative (positive) evolution if the normalization at high redshift is lower (higher) than anticipated from self-similar scaling.

for rigorously accounting for selection effects in order to constrain the scaling relations at low and high redshifts, including their evolution. They concluded that the T – M and L_X – M relations both show no departures from self-similar evolution up to $z \approx 0.5$.

In the near future, the *XMM Cluster Survey* (XCS; Romer et al. 2001) will provide a complete sample of clusters spanning a broad redshift range, $0 < z \lesssim 1.5$, all coming from the same survey and selected with well-defined criteria. Since the survey selection function will be known, the evolution of X-ray scaling relations will be measured with unprecedented accuracy out to high-redshift. Cluster surveys based on the Sunyaev–Zel’dovich (SZ) effect, such as those being conducted with the *South Pole Telescope* (Vanderlinde et al. 2010) and the *Atacama Cosmology Telescope* (Hincks et al. 2009), are also expected to produce large catalogues of clusters covering a wide redshift range with a well-defined mass threshold. Like XCS, these samples will be ideal for studying the evolution of cluster scaling relations.

There are also several other reasons why results from different studies may appear to be contradictory. For example, the measured evolution can be affected by: poor statistics due to small sample sizes; the local scaling relation chosen to compare high-redshift data with; different definitions of evolution (i.e. whether the expected self-similar behaviour is scaled out first or not); different choices of scale radius used to define a cluster (i.e. redshift-dependent or not) and whether the core region is excised or not (and the size of the core region). In short, extreme care is required when comparing observational results with each other, and with theoretical results from numerical simulations.

Theoretical studies of cluster formation have mainly concentrated on explaining the lack of self-similarity inherent in low-redshift scaling relations, rather than the evolution of scaling laws. To this end, numerous mechanisms for raising the entropy of the intracluster gas have been implemented in hydrodynamical N -body simulations, such as radiative cooling (e.g. Bryan 2000; Pearce et al. 2000; Muanwong et al. 2001, 2002; Davé, Katz & Weinberg 2002; Voit et al. 2002; Wu & Xue 2002), preheating (e.g. Bialek, Evrard & Mohr 2001; Brighenti & Mathews 2001; Muanwong et al. 2002; Borgani et al. 2002; Tornatore et al. 2003; Borgani et al. 2005), star formation and associated feedback from SNe (e.g. Valdarnini 2003; Kay 2004; Kay et al. 2004, 2007; Borgani et al. 2004, 2005; Romeo et al. 2006; Nagai, Kravtsov & Vikhlinin 2007) and black hole growth with associated feedback from AGN (e.g. Puchwein, Sijacki & Springel 2008; McCarthy et al. 2010; Fabjan et al. 2010).

Simulations employing such models have indeed proved capable of successfully reproducing the observed scaling relations for local clusters, at least on average, although often at the expense of excessive star formation. However, we would not expect the thermal history of the ICM to be the same in each case, so we should see differences in evolutionary behaviour. This was first demonstrated by Muanwong et al. (2006) who traced the evolution of the cluster population to $z = 1.5$ using three different models: a cooling-only model, a model with preheating and cooling, and a stellar feedback model that self-consistently heats cold gas in proportion to the local star formation rate. While all three schemes produce indistinguishable L_X – T relations at $z = 0$, they predict strongly positive, mildly positive and mildly negative evolution of the L_X – T relation, respectively. Therefore, given observational data of sufficient quality, it should be possible to rule out unsuitable theoretical models of non-gravitational heating. This emphasizes the importance of accurately measuring cluster scaling relations over a range of redshifts.

Other attempts to study the evolution of X-ray scaling laws with numerical simulations are scarce. Ettori et al. (2004b) used a simulation including radiative cooling, star formation and supernova feedback to follow the evolution of the cluster population between $z = 1$ and $z = 0.5$. They measured a small, but significant, negative evolution in the normalization of the L_X – M and L_X – T relations, and a marginally negative evolution of the M – T relation. These results were found to be consistent with the observational data of Ettori et al. (2004a). Kay et al. (2007) used a similar simulation, but with a different prescription for cooling and stellar feedback, to investigate the evolution of the M – T and L_X – T relations in the redshift interval $0 < z < 1$. The results they obtained are qualitatively the same as those of Ettori et al. (2004b). However, we note that a rigorous comparison between the results of Ettori et al. (2004b), Muanwong et al. (2006) and Kay et al. (2007) is not possible owing to differences in their data analysis procedures (different definitions of cluster scale radii, etc.).

In this paper, we reconsider the evolution of cluster scaling relations from a theoretical perspective. Our basic goal is to investigate how scaling laws evolve when feedback from AGN is included in numerical simulations, in addition to stellar feedback. As far as we are aware, this is the first time this has been attempted.

The simulation we use is drawn from the Millennium Gas Project, a series of hydrodynamical N -body simulations with the same volume ($500^3 h^{-3} \text{ Mpc}^3$) and the same initial perturbation amplitudes and phases as the Millennium Simulation (Springel et al. 2005). Feedback from galaxies is incorporated in our simulation via the hybrid approach of Short & Thomas (2009), where the energy imparted to the ICM by SNe and AGN is computed from a semi-analytic model (SAM) of galaxy formation. Since SAMs are tuned to reproduce the properties of observed galaxies, the source of feedback in our simulation is guaranteed to be a realistic galaxy population. By contrast, fully self-consistent simulations with radiative cooling, star formation and supernova feedback typically predict that too much gas cools and forms stars (e.g. Borgani et al. 2004; Kay et al. 2007). We assess how feedback from galaxy formation affects the evolution of scaling relations by comparing our results with those obtained from two other Millennium Gas simulations. The first of these is a control model, where the gas is heated by gravitational processes only. The second includes additional radiative cooling and uniform preheating at high redshift as a simple model of non-gravitational heating from astrophysical sources.

The large volume of the Millennium Gas simulations enables us to resolve statistically significant numbers of clusters at all redshifts relevant to cluster formation. In fact, our cluster samples are some of the largest ever extracted from numerical simulations. For example, in the preheating plus cooling run we have over 20 times more objects with $T > 2 \text{ keV}$ at $z = 0$ and $z = 1$ than Kay et al. (2007). Furthermore, we can capture the formation of the richest systems, allowing us to probe the same dynamic range as the observations. The Millennium Gas simulations thus provide an ideal tool for studying the evolution of the cluster population.

The layout of this paper is as follows. In Section 2 we briefly review the self-similar model of cluster formation. The three Millennium Gas simulations are discussed in Section 3, along with a description of our method for generating cluster catalogues and profiles. In Section 4, we compare results for our three models, starting with a discussion of cluster profiles and X-ray scaling relations at $z = 0$, and then investigate how profiles and scaling laws evolve from $z = 1.5$ to $z = 0$. Wherever possible we attempt to place observational constraints on our models. We summarize our results and conclude in Section 5.

2 CLUSTER SCALING THEORY

The simplest model of galaxy cluster formation is that they form via the gravitational collapse of the most overdense regions in the dark matter distribution, and the cluster baryons are heated only by gravitational processes (compression and shock heating) during the collapse. Since non-linear gravitational processes do not introduce any characteristic scale, we would then expect clusters to be self-similar, i.e. scaled versions of each other. With the additional assumptions that clusters are spherically symmetric systems and that the intracluster gas is in hydrostatic equilibrium with the underlying dark matter potential, it is straightforward to derive simple self-similar scaling relations between cluster properties (Kaiser 1986).

Defining r_Δ as the radius of a spherical volume within which the mean matter density is Δ times the critical density at redshift z , we find that the total enclosed mass, M_Δ ,³ scales with gas temperature, T_Δ , as

$$E(z)^{-2/3} T_\Delta \propto M_\Delta^{2/3}. \quad (1)$$

Under the further assumption that the X-ray emission of the ICM is primarily thermal bremsstrahlung radiation (which is valid for $T > 2$ keV), the luminosity, $L_{X,\Delta}$, within r_Δ is given by

$$E(z)^{-1} L_{X,\Delta} \propto T_\Delta^2. \quad (2)$$

The scaling between X-ray luminosity and total mass follows upon combining equations (1) and (2):

$$E(z)^{-7/3} L_{X,\Delta} \propto M_\Delta^{4/3}. \quad (3)$$

The quantity $Y_X = M_{\text{gas}} T$ has recently attracted much attention since it has been shown to be a low-scatter mass proxy, regardless of cluster dynamical state (e.g. Kravtsov et al. 2006). This is primarily because Y_X approximates the total thermal energy of the ICM, which is not strongly affected by cluster mergers (Poole et al. 2007), unlike L_X or T (Ricker & Sarazin 2001). The self-similar scaling of Y_X within r_Δ with total mass is

$$E(z)^{-2/3} Y_{X,\Delta} \propto M_\Delta^{5/3}. \quad (4)$$

The density contrast Δ governs the scale radius within which one measures the mass of a cluster. The most common choice is to set $\Delta = 500$, since r_{500} is the effective limiting radius for reliable observations from *Chandra* and *XMM-Newton*. Throughout this paper we will adopt $\Delta = 500$, independent of redshift.

Note that there are other ways in which the scale radius of a cluster can be defined. In the original model of Kaiser (1986), clusters were assumed to be self-similar with respect to the mean matter density of the Universe, rather than the critical density. In this case, the $E(z)$ factors in equations (1)–(4) are replaced by $(1+z)$. Another possibility is to assume a redshift-dependent density contrast $\Delta(z)$ that is proportional to $\Delta_{\text{vir}}(z)$, where $\Delta_{\text{vir}}(z)\rho_{\text{cr}}(z)$ is the mean density within the cluster virial radius (e.g. Ettori et al. 2004a; Maughan et al. 2006; Branchesi et al. 2007). The value of $\Delta_{\text{vir}}(z)$ is taken from the analytical solution for the collapse of a spherical top-hat perturbation, under the assumption that the cluster has just virialized at that redshift (e.g. Peebles 1980). With this choice of density contrast, the $E(z)$ factors in equations (1)–(4) become $E(z)\Delta(z)^{1/2}$ instead. Therefore, predictions for the evolution

of the cluster population clearly depend on how the scale radius is defined, so caution must be exercised when comparing the results of different observational and theoretical studies.

Observations of clusters in the local Universe have established that scaling relations between cluster properties do indeed exist, but their form is found to be different to the self-similar predictions. This is because non-gravitational effects, such as radiative cooling and feedback from galaxy formation, modify the entropy structure of the ICM. Lower-mass systems are affected more than massive objects, breaking the self-similarity of the scaling laws. Departures from self-similarity thus provide us with a probe of the non-gravitational processes operating in clusters. Although the self-similar model cannot explain the observed form of scaling relations, there is some observational evidence that it is capable of describing their evolution.

3 SIMULATIONS: THE MILLENNIUM GAS PROJECT

In this work we use simulations taken from the Millennium Gas Project, a programme to add gas to the dark matter-only Millennium Simulation (Springel et al. 2005). We present a new addition to the Millennium Gas suite in which feedback is directly tied to galaxy formation, enabling us to investigate how energy input from both SNe and AGN affects the evolution of cluster scaling relations. Hereafter, we refer to this simulation as the FO run. The feedback model adopted is the hybrid scheme of Short & Thomas (2009), where a SAM is used to calculate the energy transferred to the intracluster gas by SNe and AGN. An immediate benefit of this approach is that feedback is guaranteed to originate from a galaxy population whose observational properties agree well with those of real galaxies. This is generally not the case in fully self-consistent hydrodynamical simulations that include radiative cooling and stellar feedback because too much gas cools out of the hot phase, leading to excessive star formation (e.g. Borgani et al. 2004; Kay et al. 2007). It is widely thought that additional heating from AGN is the natural solution to this overcooling problem. Indeed, McCarthy et al. (2010) and Fabjan et al. (2010) have demonstrated that including AGN feedback in hydrodynamical simulations can successfully balance radiative cooling in galaxy groups. However, the stellar fraction is still found to be nearly two to three times larger than observed in massive clusters (Fabjan et al. 2010).

By coupling an SAM to a hydrodynamical simulation, Short & Thomas (2009) were able to reproduce the observed mean L_X – T relation for groups and poor clusters, provided there was a large energy input into the ICM from AGN over the entire formation history of haloes. The AGN heating is more efficient at driving X-ray emitting gas from the central regions of lower-mass haloes, reducing their luminosity and steepening the L_X – T relation as desired. Their model was also able to account for some of the increased scatter about the mean relation seen for temperatures $T \lesssim 3$ keV, attributable to the varied merger histories of groups.

A limitation of the method of Short & Thomas (2009) is that radiative cooling is not incorporated in their hydrodynamical simulations. Instead, their model relies on the simplistic treatment of the distribution and cooling of gas employed in existing SAMs. Note, however, that gas particles are still converted to dissipationless ‘star’ particles as dictated by the SAM. While cooling is relatively unimportant for the majority of the ICM, the low central entropy found in CC clusters cannot be reproduced in their simulations, so the large scatter towards the upper-luminosity edge of the observed

³ $M_\Delta = 4\pi r_\Delta^3 \Delta \rho_{\text{cr}}(z)/3$, where $\rho_{\text{cr}}(z) = 3H_0^2 E(z)^2/8\pi G$ is the critical density and $E(z)^2 = \Omega_{\text{m},0}(1+z)^3 + \Omega_{\Lambda,0}$ in a spatially flat Λ -cold dark matter (Λ CDM) cosmological model.

local L_X - T relation is not recovered. This will be less of an issue at high redshift since only a small fraction of clusters have CCs at $z \gtrsim 0.5$ (e.g. Vikhlinin et al. 2007), due to the higher rate of major mergers (e.g. Jeltema et al. 2005).

A more self-consistent approach would be to fully couple a SAM to a radiative simulation, so that the gas distribution in the simulation is used to inform the SAM. This extension of the semi-analytic technique would require the simulation and the SAM to be coupled in such a way that both can be undertaken simultaneously. Extensive testing would be necessary to ensure that such a model was as successful as current SAMs in reproducing observed galaxy properties. Such a scheme is a long-term goal of our work but is beyond the scope of this paper.

In order to elucidate the effect of feedback from galaxy formation on the evolution of scaling laws, we compare the predictions of our feedback model with those of two other models in the Millennium Gas series. The first of these simulations incorporates gravitational heating only and is thus referred to as the GO run. This is useful as a base model. Given that the only source of gas entropy changes in the GO run is gravity, we would expect a self-similar cluster population to be formed. This is generally found to be the case in such simulations (e.g. Navarro, Frenk & White 1995; Eke, Navarro & Frenk 1998; Voit, Kay & Bryan 2005; Ascasibar et al. 2006; Stanek et al. 2010).

The second reference simulation includes high-redshift preheating and radiative cooling, in addition to shock heating. We name this the PC run. Preheating raises the entropy of the ICM before gravitational collapse, preventing gas from reaching high densities in central cluster regions and thus reducing its X-ray emissivity. This effect is greater in lower-mass systems, breaking the self-similarity of the cluster scaling relations in a way that resembles observations (Bialek et al. 2001; Brighenti & Mathews 2001; Muanwong et al. 2002; Borgani et al. 2002; Tornatore et al. 2003; Borgani et al. 2005; Hartley et al. 2008; Stanek et al. 2010). However, preheating fails to account for the observed scatter about the mean relations, particularly on group scales, and generates overly large isentropic cores in low-mass systems (e.g. Ponman, Sanderson & Finoguenov 2003; Pratt, Arnaud & Pointecouteau 2006).

The cosmological model adopted in all three Millennium Gas simulations is a spatially flat Λ CDM model with parameters $\Omega_{m,0} = 0.25$, $\Omega_{b,0} = 0.045$, $\Omega_{\Lambda,0} = 0.75$, $h = 0.73$, $n_s = 1$ and $\sigma_{8,0} = 0.9$. Here $\Omega_{b,0}$ is the baryon density parameter, h is the Hubble parameter H_0 in units of $100 \text{ km s}^{-1} \text{ Mpc}^{-1}$, n_s is the spectral index of primordial density perturbations and $\sigma_{8,0}$ is the rms linear density fluctuation within a sphere of comoving radius $8 h^{-1} \text{ Mpc}$. These cosmological parameters are the same as those used in the original Millennium Simulation and are consistent with a combined analysis of the first-year *Wilkinson Microwave Anisotropy Probe* (WMAP) data (Spergel et al. 2003) and data from the *Two-degree-Field Galaxy Redshift Survey* (Colless et al. 2001). However, there is some tension between the chosen parameter values, particularly n_s and $\sigma_{8,0}$, and those derived from the seven-year WMAP data (Komatsu et al. 2010).

We now describe further details of our simulations. The GO and PC runs have already been discussed elsewhere (Hartley et al. 2008; Stanek et al. 2010), so here we only briefly summarize their properties, focusing our attention mainly on the new FO run.

3.1 The GO and PC simulations

Initial conditions for the GO and PC runs were created at a redshift $z_i = 49$ by displacing particles from a glass-like distribu-

tion, so as to form a random realization of a density field with a Λ CDM linear power spectrum obtained from CMBFAST (Seljak & Zaldarriaga 1996). The amplitudes and phases of the initial perturbations were chosen to match those of the Millennium Simulation. In both cases, the simulation volume is a comoving cube of side length $L = 500 h^{-1} \text{ Mpc}$, as in the Millennium Simulation, containing 5×10^8 dark matter particles of mass $m_{\text{DM}} = 1.42 \times 10^{10} h^{-1} M_\odot$, and 5×10^8 gas particles of mass $m_{\text{gas}} = 3.12 \times 10^9 h^{-1} M_\odot$. These are some of the largest hydrodynamical N -body simulations ever carried out. Although the mass resolution is approximately 20 times coarser than the Millennium Simulation, over 95 per cent of haloes formed with a mass greater than $10^{13} h^{-1} M_\odot$ are within $100 h^{-1} \text{ kpc}$ and 5 per cent of their original position and mass, respectively.

The massively parallel TreePM N -body/SPH code GADGET-2 (Springel 2005) was used to evolve both sets of initial conditions to $z = 0$, with full particle data stored at 160 output redshifts. The Plummer-equivalent gravitational softening length was fixed at $\epsilon = 100 h^{-1} \text{ kpc}$ in comoving coordinates until $z = 3$, then fixed in physical coordinates thereafter. The softening is thus approximately 4 per cent of the mean interparticle spacing, which has been shown to be the optimal choice for hydrodynamical simulations (Thomas & Couchman 1992; Borgani et al. 2006).

The simple model of preheating employed in the PC simulation is similar to that of Borgani et al. (2002). Briefly, the entropy of every particle is raised to 200 keV cm^2 at $z = 4$, thus creating an entropy ‘floor’. In addition to preheating, there is also radiative cooling based on the cooling function of Sutherland & Dopita (1993), assuming a fixed metallicity of $0.3 Z_\odot$ (a good approximation to the mean metallicity of the ICM out to at least $z = 1$; Tozzi et al. 2003). Once the temperature of a gas particle drops below $2 \times 10^4 \text{ K}$, the hydrogen density exceeds $\rho_{\text{H}} = 4.2 \times 10^{-27} \text{ g cm}^{-3}$ and the density contrast is greater than 100, then it is converted to a collisionless star particle. However, the preheating is so extreme that star formation is effectively terminated at $z = 4$, so that less than 2 per cent of the baryons are locked-up in stars at $z = 0$.

3.2 The FO simulation

We have adopted a different approach for the FO simulation than for the other two Millennium Gas runs. Rather than simulating the entire Millennium volume, we decided instead to resimulate a sample of several hundred galaxy groups and clusters extracted from the original Millennium Simulation. In this way, it will be less time/resource consuming to develop and test future extensions of the model of Short & Thomas (2009).

There are three distinct components of the FO run: a dark matter-only resimulation of each region containing a cluster from our sample, semi-analytic galaxy catalogues built on the halo merger trees of these resimulations and hydrodynamical resimulations of the same regions to track the energy injection from model galaxies. We now discuss each stage of the modelling process in turn.

3.2.1 Dark matter cluster resimulations

Our cluster sample consists of 337 objects identified in the $z = 0$ output of the Millennium Simulation, spanning a broad mass range: $1.7 \times 10^{13} h^{-1} M_\odot \leq M_{\text{vir}} \leq 2.9 \times 10^{15} h^{-1} M_\odot$. The sample was constructed as follows. All clusters with $M_{\text{vir}} > 5 \times 10^{14} h^{-1} M_\odot$ were selected while, at lower masses, a fixed number of clusters were chosen at random per logarithmic interval in virial mass. For each cluster in the sample, we extract a spherical region from the

$z = 0$ Millennium snapshot that is centred on the object in question and has a radius equal to twice the cluster virial radius. The particles contained within this sphere are traced back to $z_i = 127$ (the initial redshift of the Millennium Simulation) to identify the Lagrangian region from which the object formed. Multi-mass initial conditions (Tormen, Bouchet & White 1997) are then made by following a procedure similar to that of Springel et al. (2008), but with one major difference: we do not increase the mass resolution in the Lagrangian region of interest, but degrade the resolution exterior to this region instead. Particles in the ‘high-resolution’ region then have (approximately) the same mass as in the parent Millennium Simulation, $m_{\text{DM}} = 8.61 \times 10^8 h^{-1} M_{\odot}$, but more distant regions are sampled with progressively more massive particles. Our resimulations can thus be thought of as ‘desimulations’. A glass-like configuration was used for the unperturbed particle distribution in the high-resolution regions of all our initial conditions, and the initial particle displacements were imprinted using the Zel’dovich approximation. The amplitudes and phases of the initial perturbations again match those of the Millennium Simulation.

We adopt the same mass resolution as the Millennium Simulation in the high-resolution regions of our initial conditions for two reasons. First, the properties of our resimulated clusters should then agree well with those of their counterparts in the original Millennium Simulation, except for small perturbations induced by different representations of the tidal field. Secondly, we will be able to construct more comprehensive galaxy catalogues, and thus a more detailed model for feedback from galaxies, than if we had used the coarser mass resolution of the other Millennium Gas runs.

The initial conditions for each cluster in our sample are then evolved to the present day with GADGET-2. Raw particle data are stored at the 64 output redshifts of the Millennium Simulation. At each output time, dark matter haloes are identified as virialized groups of high-resolution particles using a parallel friends-of-friends (FOF) algorithm. We adopt a standard FOF linking length of 20 per cent of the mean particle separation (Davis et al. 1985), and only save groups that contain at least 20 particles, so that the minimum halo mass is $1.7 \times 10^{10} h^{-1} M_{\odot}$. Gravitationally bound substructures orbiting within these FOF haloes are then found with a parallel version of the SUBFIND algorithm (Springel et al. 2001). The resulting catalogues of groups and subgroups are written out alongside the snapshot data.

In the Millennium Simulation, the gravitational force law was softened isotropically on a fixed comoving scale of $\epsilon = 5 h^{-1} \text{ kpc}$ (Plummer-equivalent), corresponding to approximately 2 per cent of the mean interparticle spacing. We employ a different softening scheme in our cluster resimulations. The Plummer-equivalent gravitational softening length is fixed to $\epsilon = 9.2 h^{-1} \text{ kpc}$ in physical coordinates below $z = 3$, and to $\epsilon = 36.8 h^{-1} \text{ kpc}$ in comoving coordinates at higher redshifts (for the high-resolution particles). The $z = 0$ softening length is thus 4 per cent of the mean particle separation. Our choice of a larger softening scale allows us to resolve more low-mass subhaloes, because two-body heating effects are less important, so we can construct more detailed semi-analytic galaxy catalogues.

It is important that the high-resolution region remains free from contamination by more massive boundary particles during the course of a resimulation. Since we are interested in the evolution of cluster properties within r_{500} , we have checked whether there are any boundary particles in this region for every cluster used in this study (see Section 3.3 for a description of how we construct cluster samples from our resimulations). Only three objects were found to contain boundary particles interior to r_{500} , of which two were sig-

nificantly contaminated. We discarded these two objects from our cluster samples.

3.2.2 Feedback from a galaxy formation model

Dark matter halo merger trees are constructed in post-processing for each resimulated region using the stored subhalo catalogues. This is done by exploiting the fact that each halo will have a unique descendant in a hierarchical scenario of structure formation [see Springel et al. (2005) for details of the procedure]. Using these merger trees, we have generated galaxy catalogues for all our resimulations by applying the Munich L-GALAXIES SAM of De Lucia & Blaizot (2007). Galaxy properties are saved at the same 64 redshifts as the simulation data. We adopted the same set of model parameters as De Lucia & Blaizot (2007). For a full description of the physical processes incorporated in L-GALAXIES, we refer the reader to Croton et al. (2006) and De Lucia & Blaizot (2007).

The information contained within the semi-analytic galaxy catalogues enables us to calculate energy feedback from galaxies into the ICM. We only give an outline the procedure here, since a complete account is given in Short & Thomas (2009).

For each cluster in our sample, we first identify all model galaxies that lie within a distance r_{vir} of the centre of the cluster halo at $z = 0$, then use the galaxy merger trees to find all their progenitors. We only consider feedback from this subset of galaxies since this is sufficient to correctly determine the properties of the ICM within r_{500} , the region we are interested in. For each of these galaxies, we use its merger tree to compute the change in stellar mass, ΔM_* , and mass accreted by the central black hole, ΔM_{BH} , over the time interval Δt between successive model outputs. Knowledge of ΔM_* enables us to incorporate star formation in our simulations as described in the following section.

We compute the energy imparted to intracluster gas by Type II SNe using the L-GALAXIES supernova feedback model. In this model, the total amount of energy released by SNe in a time Δt is proportional to ΔM_* . However, some of this energy is assumed to be used up reheating cold gas in the galactic disc. Any energy remaining after reheating is used to eject gas from the halo into the surrounding medium, heating the ICM (see equation 20 of Croton et al. 2006).

The model of AGN feedback we employ is that of Bower, McCarthy & Benson (2008). In this scheme, the heat energy input into the ICM by AGN over a time period Δt is the minimum of

$$\Delta E_{\text{heat}} = \epsilon_r \Delta M_{\text{BH}} c^2 \quad (5)$$

and

$$\Delta E_{\text{heat}} = \epsilon_{\text{SMBH}} \Delta E_{\text{Edd}}, \quad (6)$$

where c is the speed of light, ΔE_{Edd} is the energy released by a black hole accreting at the Eddington rate in a time Δt and ϵ_r is the efficiency with which matter can be converted to energy near the event horizon. Following convention, we set $\epsilon_r = 0.1$, which is appropriate for radiatively efficient accretion on to a non-rapidly spinning black hole (Shakura & Sunyaev 1973). The parameter ϵ_{SMBH} is related to the structure of the accretion disc itself. At low accretion rates, the accretion disc is expected to be geometrically thick and advection dominated, enabling efficient jet production and effective radio mode feedback. As the accretion rate is increased, it is thought that the vertical height of the disc eventually collapses, so much more of the accretion energy is radiated away. Bower et al. (2008) assume that this change in disc structure occurs once the accretion rate reaches $\dot{M}_{\text{BH}} = \epsilon_{\text{SMBH}} \dot{M}_{\text{Edd}}$, where $\epsilon_{\text{SMBH}} = 0.02$,

leading to an upper limit on the amount of energy available for heating intracluster gas (equation 6).

3.2.3 Hydrodynamical cluster resimulations

To track the effect of energy feedback from galaxies on the thermodynamical properties of the ICM, we couple the L-GALAXIES SAM to hydrodynamical resimulations of our clusters. We use the same multi-mass initial conditions for these resimulations as described above, but we add gas particles with zero gravitational mass. This ensures that the dark matter distribution remains undisturbed by the inclusion of baryons, so that the halo merger trees used to generate the semi-analytic galaxy catalogues will be the same. Although baryons can influence the structure and merger histories of dark haloes (Saro et al. 2008; Stanek, Rudd & Evrard 2009; Romano-Díaz et al. 2009; Pedrosa, Tissera & Scannapieco 2010; Duffy et al. 2010), such effects are neglected in all modern SAMs, which are founded on merger trees derived from the dark matter distribution. We are forced to follow this route so that we can use SAM input into our simulations. This approximation is unlikely to have any significant impact on the results presented in this paper.

The number of gas particles added to each set of initial conditions is chosen in such a way that their true mass would be the same as in the other two Millennium Gas runs. Note that gas particles are only added to the high-resolution region. We include gas at a lower resolution than the dark matter simply to ease the computational cost of our simulations. The resolution we have adopted is sufficient to obtain numerically converged estimates of bulk cluster properties for systems with $T \gtrsim 2$ keV (Short & Thomas 2009).

Each set of initial conditions is evolved from $z_i = 127$ to $z = 0$ with a version of GADGET-2 that has been modified to accommodate gas particles with zero gravitational mass. As in Short & Thomas (2009), cooling processes are neglected. The same softening scheme as used in the dark matter resimulations is applied to the gas particles since they do not influence the gravitational dynamics. Whenever an SPH calculation is required, we assign gas particles their true mass, so that gas properties are computed correctly. Gas particles are also given their true mass for simulation data dumps, with the mass of the dark matter particles accordingly reduced to $(1 - f_b)m_{\text{DM}} = 7.06 \times 10^8 h^{-1} M_\odot$, where $f_b = \Omega_{\text{b},0}/\Omega_{\text{m},0} = 0.18$ is the mean cosmic baryon fraction in our cosmological model.

Once an output redshift is reached, temporary ‘galaxy’ particles are introduced throughout the high-resolution region at positions specified by the SAM galaxy catalogue. For each galaxy, we know the increase in stellar mass and energy released by SNe and AGN since the last output (see above). We use this information to form stars and heat gas in the vicinity of model galaxies as detailed in Short & Thomas (2009). Briefly, the $\Delta N_{\text{star}} = \Delta M_*/m_{\text{gas}}$ gas particles nearest to each galaxy are converted into collisionless star particles, where a stochastic method is used to ensure ΔN_{star} is an integer. Once star formation is complete, the heat energy available from SNe and AGN is distributed amongst all gas particles contained within a sphere of radius r_{200} centred on the galaxy, in such a way that each particle receives an equal entropy boost. If the galaxy is not the central galaxy of a FOF group, then L-GALAXIES approximates r_{200} by the radius of a sphere enclosing a mass equal to the product of the number of particles in the host subhalo and the particle mass. In this case, we distribute the available heat energy within this radius instead. The total energy contributed by such galaxies is about an order of magnitude less than for central galaxies anyway. Following the injection of entropy, the galaxy particles are removed and the

simulation continues until the next output time, when the process is repeated. Note that increasing the frequency with which energy is injected into ICM has a negligible impact on our results, because the time interval between our chosen 64 model outputs is always less than the galaxy halo dynamical time.

3.3 Constructing cluster catalogues and profiles

Cluster catalogues are generated at several redshifts for the three Millennium Gas simulations using a procedure similar to that employed by Muanwong et al. (2002), which we now briefly describe.

The first step is to identify gravitationally bound groups of dark matter particles with the FOF algorithm. This was done on the fly in the FO run, and we have group catalogues stored at all 28 output redshifts between $z = 1.5$ and $z = 0$ for each resimulated cluster. For the GO and PC runs, FOF groups were identified in post-processing, setting the linking length to be 10 per cent of the mean interparticle separation. Only groups with 500 particles or more were kept, corresponding to a minimum halo mass of $7.10 \times 10^{12} h^{-1} M_\odot$. We produced group catalogues for these two simulations at seven different redshifts: $z = 1.5, 1.25, 1, 0.75, 0.5, 0.25, 0$.

The spherical overdensity method is then used to construct cluster catalogues. Briefly, a sphere is grown about the most gravitationally bound dark matter particle of each FOF group until radii are found that enclose mean overdensities of $\Delta_{\text{vir}}(z)$, $\Delta = 200$, $\Delta = 500$, $\Delta = 1000$ and $\Delta = 2500$, relative to the critical density $\rho_{\text{cr}}(z)$. In cases where clusters overlap, we only keep the object with the largest mass within r_{2500} . We also discard clusters with fewer than 1000 particles at each overdensity, which corresponds to a minimum cluster mass of $8.61 \times 10^{11} h^{-1} M_\odot$ in the FO run, and $1.73 \times 10^{13} h^{-1} M_\odot$ in the GO and PC runs.

During the cluster identification process we compute a variety of cluster properties, averaged within each choice of scale radius. The relevant properties for this work are the total mass, gas mass, temperature and X-ray luminosity. The measure of temperature we adopt is the spectroscopic-like temperature T_{sl} (Mazzotta et al. 2004). In the bremsstrahlung regime ($T > 2$ keV), this temperature estimator has been shown to provide the closest match to the actual spectroscopic temperature, T_{spec} , obtained by fitting X-ray spectra of simulated clusters with a single-temperature plasma model. The X-ray luminosity is approximated by the bolometric emission-weighted luminosity, assuming the cooling function of Sutherland & Dopita (1993) and a fixed metallicity of $0.3 Z_\odot$. Three-dimensional gas density, spectroscopic-like temperature and entropy profiles are also computed for all our clusters by averaging particle properties within spherical shells, centred on the minimum of the dark matter potential.

In this paper, we focus our attention on the evolution of X-ray scaling relations for massive clusters only, since it is the most massive objects that are observed at high redshift. Previous numerical studies that use a smaller simulation volume than the Millennium volume have been unable to resolve sufficiently large numbers of massive clusters to investigate this in detail. Limiting our scope in this way has two additional benefits. First, the cooling times are longer in the central regions of massive clusters than in groups, so the lack of self-consistent cooling in our feedback model is less of an issue. Secondly, the X-ray emission will be predominantly thermal bremsstrahlung, so the spectroscopic-like temperature provides an accurate estimate of the spectral temperature.

We construct samples of massive clusters for our study from the cluster catalogues as follows. The starting point is to discard all clusters whose average density is too low for r_{2500} to be defined.

Table 1. Number of clusters in each of the Millennium Gas simulations as a function of redshift, once the mass/temperature cut appropriate for each scaling relation has been made (see text).

Relation	Redshift			
	1.5	1	0.5	0
GO simulation				
$Y_X-M, T_{\text{sl}}-M, L_X-M$	25	145	549	1109
L_X-T_{sl}	15	107	441	946
PC simulation				
$Y_X-M, T_{\text{sl}}-M, L_X-M$	14	102	410	881
L_X-T_{sl}	13	93	376	838
FO simulation				
$Y_X-M, T_{\text{sl}}-M, L_X-M$	18	75	148	187
L_X-T_{sl}	15	67	139	186

We do this to remove any low-mass objects that may have erroneous properties due to being subclumps falling into more massive neighbouring systems. For scaling laws involving the total cluster mass (Y_X-M , $T_{\text{sl}}-M$ and L_X-M), we then impose a mass cut of $M_{500} \geq 10^{14} h^{-1} M_{\odot}$ at all redshifts of interest. For the L_X-T_{sl} relation, a cut is made in T_{sl} instead to ensure completeness in T_{sl} ; only clusters with a spectroscopic-like temperature greater than that corresponding to a mass of $M_{500} = 10^{14} h^{-1} M_{\odot}$ on the mean $T_{\text{sl}}-M$ relation is kept. Table 1 lists the number of clusters in our final samples as a function of redshift for each of the Millennium Gas simulations.

4 RESULTS AND DISCUSSION

We now use the samples of massive clusters extracted from our three simulations to investigate differences in evolutionary behaviour that arise from adopting a plausible model for feedback from SNe and AGN, rather than simple preheating or gravitational heating. We first present results at $z = 0$ as they will form the basis for measuring the evolution of the thermal properties of the ICM with redshift.

Throughout the remainder of this work, all uncertainties are quoted at the 68 per cent confidence level.

4.1 Cluster profiles at $z = 0$

Radial cluster profiles are more sensitive to the precise manner in which non-gravitational cooling and heating processes are implemented in numerical simulations than X-ray scaling laws. Therefore, we start by examining whether our model for feedback from galaxies is able to explain the temperature and entropy profiles of observed low-redshift clusters. The observational data set we use is REXCESS (Böhringer et al. 2007), a representative sample of 33 local ($z < 0.2$) clusters drawn from the REFLEX catalogue (Böhringer et al. 2004), all of which have been observed with *XMM-Newton*. Temperature profiles for the REXCESS clusters are presented in Arnaud et al. (2009), and entropy profiles in Pratt et al. (2010, hereafter PAP10). We choose to compare with REXCESS for three reasons. First, REXCESS clusters were selected in luminosity only, thus ensuring no morphological bias, in such a way as to sample the X-ray cluster luminosity function in an optimal manner. Secondly, distances were optimized in REXCESS so that r_{500} falls well within the *XMM-Newton* field-of-view, increasing the precision of measurements at large radii. Thirdly, the same definition of r_{500} is used as in this work.

To facilitate a fair comparison with our simulated data, we only consider observed clusters with a mass $M_{500} \geq 10^{14} h^{-1} M_{\odot}$. We have also rescaled the observational data to account for the fact that Arnaud et al. (2009) and PAP10 assumed a slightly different cosmological model in their analysis.

In the following, it will prove useful to divide the REXCESS sample into CC and non-cool-core (NCC) systems. As in PCA09, clusters are classified as CC systems if they have a central gas density $E(z)^{-2} n_e(0) > 4.8 \times 10^{-2} h^{1/2} \text{ cm}^{-3}$.

4.1.1 Temperature profiles

In Fig. 1, we display the average spectroscopic-like temperature profile of clusters in the FO simulation. For comparison, we also show average profiles obtained from the reference GO and PC simulations and the observational data of Arnaud et al. (2009). We discard profile data at radii less than the gravitational softening length and only plot the average profile if there are 10 or more clusters in a given radial bin. All profiles have been normalized to the characteristic halo temperature, T_{500} , computed from the self-similar model:

$$T_{500} = \frac{G \mu m_H}{2 k_B} \frac{M_{500}}{r_{500}}, \quad (7)$$

where $\mu = 0.59$ is the mean molecular weight for a fully ionized gas of primordial composition and m_H is the mass of a hydrogen atom. In the case of the observed profiles, T_{500} is calculated at the redshift of each individual cluster. With this scaling we would expect cluster profiles to coincide in the pure gravitational heating scenario.

Clusters formed in the GO simulation are clearly cooler than observed. This is because the spectroscopic-like temperature estimate is biased low by the cool, low-entropy cores of accreted subhaloes that are prevalent in GO cluster haloes (e.g. Mathiesen & Evrard 2001). The temperature profiles of individual clusters are flat in core regions, but we see a slight decline in the average scaled profile at small radii, $r \lesssim 0.1 r_{500}$. This is because we are only averaging over the profiles of the most massive clusters at such radii, since the gravitational softening length is a smaller fraction of r_{500} for these objects, and the normalization of the scaled temperature

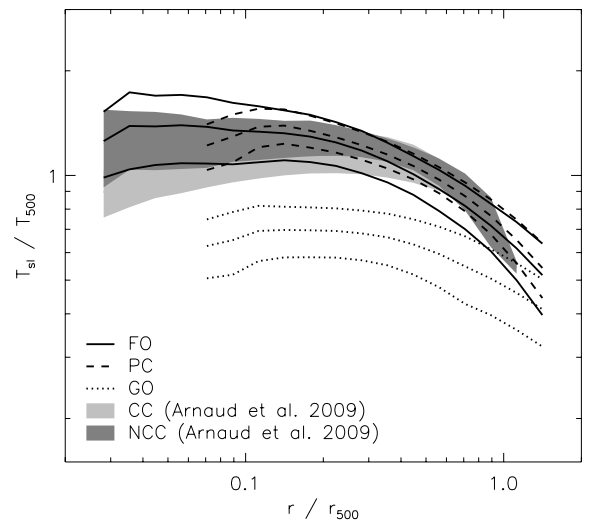


Figure 1. Mean spectroscopic-like temperature profiles, with 1σ scatter, obtained from the Millennium Gas simulations. The light- and dark shaded regions enclose the mean profiles, plus 1σ scatter, of CC and NCC clusters in the REXCESS sample (Arnaud et al. 2009), respectively. Only clusters with a mass $M_{500} \geq 10^{14} h^{-1} M_{\odot}$ are considered.

profiles decreases with increasing mass. In the self-similar model the normalization of the scaled profiles should not depend on mass; the reason for the mass-dependence in our GO simulation is that more massive clusters are less concentrated than their low-mass counterparts, i.e. even the dark matter is not truly self-similar.

In the PC and FO runs the source of non-gravitational heating is completely different, but the net effect of the entropy injection is the same: cool subclumps are erased and the average temperature of the intracluster gas increases. Both simulations lead to temperature profiles that provide a good overall match to the observed profiles of NCC clusters, being nearly isothermal in core regions $r \lesssim 0.15r_{500}$. Again, the down-turn in the average scaled profiles visible in core regions arises because, for small values of r/r_{500} , we are taking an average of the scaled temperature profiles of the most massive objects only, which have a lower normalization than those of less massive systems.

Recall that we have chosen to neglect gas cooling processes in our FO simulation, so it is not surprising that we do not reproduce the gradual decline in temperature seen in the central parts of CC clusters, where the cooling time is short. Although the PC run does incorporate radiative cooling, it has a negligible effect on the gas temperature since the entropy of the ICM is raised before structure formation commences, preventing gas from reaching high densities in cluster cores and cooling efficiently.

Fully self-consistent simulations with radiative cooling and stellar feedback typically predict temperature profiles with a sharp spike at small cluster-centric radii, followed by a rapid drop in temperature moving further into the core (e.g. Borgani et al. 2004; Nagai et al. 2007; Sijacki et al. 2007). This is due to the adiabatic compression of gas flowing in from cluster outskirts to compensate for the lack of pressure support caused by too much gas cooling out of the hot phase. Temperature profiles of this form clearly conflict with the smoothly declining (flat) profiles of observed CC (NCC) clusters (e.g. Sanderson, Ponman & O’Sullivan 2006; Vikhlinin et al. 2006; Arnaud et al. 2009).

Even if a feedback mechanism is able to reproduce observed temperature profiles, this does not guarantee that radiative cooling has been balanced. For example, the stellar feedback scheme employed by Kay et al. (2007) is capable of producing temperature profiles that are in reasonable agreement with observational data. However, the resulting stellar fraction within clusters was found to be ~ 25 per cent, far in excess of the observed value of ~ 10 per cent (Balogh et al. 2001; Lin, Mohr & Stanford 2003; Balogh et al. 2008).

In recent work, Fabjan et al. (2010) have included a sub-grid model for AGN feedback in hydrodynamical simulations. They found that the additional heating from AGN was insufficient to prevent overcooling in massive clusters, again leading to too high a star formation efficiency and sharply peaked temperature profiles. However, on the scale of galaxy groups, their AGN feedback scheme was able to successfully regulate the thermal structure of the ICM (see also McCarthy et al. 2010).

4.1.2 Entropy profiles

The entropy of intracluster gas increases when heat energy is introduced, and decreases when radiative cooling carries heat energy away. Entropy profiles thus preserve a record of the physical processes responsible for similarity breaking in clusters (e.g. Voit et al. 2002, 2003).

If shock heating were the only mechanism acting to raise the entropy of the gas, then analytical models based on spherical collapse

predict that entropy scales with radius as $K \propto r^{1.1}$ outside of central cluster regions (Tozzi & Norman 2001). Cosmological simulations that only include gravitational heating give rise to slightly steeper entropy profiles in cluster outskirts: $K \propto r^{1.2}$ (e.g. Voit et al. 2005; Nagai et al. 2007).

Observed profiles are also typically found to scale as $K \propto r^{1.1}$ at large cluster-centric radii, flattening in central regions (e.g. Ponman et al. 2003; Sun et al. 2009; Cavagnolo et al. 2009; Sanderson et al. 2009; PAP10). However, the precise radius at which this flattening occurs varies considerably, depending on such factors as the temperature (mass) of the system and whether it has a CC or an NCC. In particular, hotter, more massive objects have a higher mean core entropy (e.g. Cavagnolo et al. 2009), and the profiles of NCC clusters flatten off at significantly larger radii than those of CC clusters (e.g. Sanderson et al. 2009; PAP10).

Fig. 2 compares the entropy profiles obtained from each of our three simulations with observational data from REXCESS (PAP10). For illustrative purposes, we also show the power laws $K \propto r^{1.1}$ and $K \propto r^{1.2}$, assuming an arbitrary normalization in both cases. We have scaled all entropy profiles by the ‘virial’ entropy, K_{500} , defined as

$$K_{500} = \frac{k_B T_{500}}{n_{e,500}^{\gamma-1}}, \quad (8)$$

where $n_{e,500}$ is the average electron density within r_{500} , given by

$$n_{e,500} = \frac{500 f_b E(z)^2 \rho_{cr,0}}{\mu_e m_H}, \quad (9)$$

and $\mu_e = 1.14$ is the mean molecular weight per free electron. Note that K_{500} depends only on the total halo mass, so is independent of the thermodynamic state of the gas.

The entropy profiles of clusters extracted from the GO run are indeed well described by the power-law $K \propto r^{1.2}$ for $r \gtrsim 0.15r_{500}$, agreeing with the results of previous studies. There is also very little scatter about the mean, indicating self-similar scaling. For radii interior to $0.15r_{500}$ there is more diversity; some of the clusters have nearly isentropic cores while others show no signs of flattening. Compared to the observed entropy profiles of CC clusters, the profiles of objects in the GO run have a similar slope, at least for

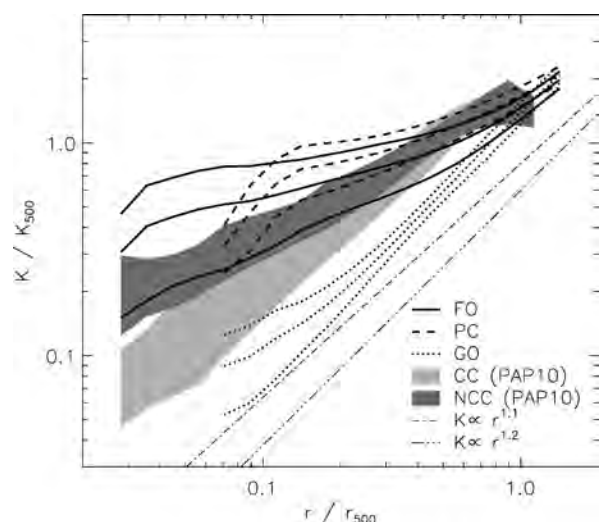


Figure 2. Mean entropy profiles, with 1σ scatter, obtained from the Millennium Gas simulations. The light and dark shaded regions enclose the mean profiles, plus 1σ scatter, of observed CC and NCC clusters from REXCESS (PAP10), respectively. We only consider clusters with a mass $M_{500} \geq 10^{14} h^{-1} M_{\odot}$.

$r \gtrsim 0.15r_{500}$, but the normalization is systematically too low. In the case of NCC clusters, it is evident that the GO model cannot explain the shallow profiles characteristic of these systems.

Clusters formed in the PC and FO simulations have entropy profiles that are broadly consistent with the theoretical scaling $K \propto r^{1.1}$ at large radii $r \gtrsim r_{500}$. This supports the idea that gravity dominates the ICM thermodynamics in the outer regions of clusters. As we move in towards the core from r_{500} , the slope decreases and the profiles flatten off, providing a fair match to the observed entropy profiles of NCC clusters. However, on average, both the PC and FO models predict entropy profiles with a shallower slope than those of NCC clusters in central regions, resulting in an overestimate of the core entropy. Note that the FO run yields entropy profiles that are slightly closer to the observed NCC cluster profiles than the PC run.

In both the PC and FO runs, we see a drop in the average scaled entropy profiles at small values of r/r_{500} , where we are averaging over the profiles of just the most massive systems. This is because the normalization of cluster entropy profiles decreases with mass in these simulations. To demonstrate this, in Fig. 3 we plot the scaled entropy at r_{500} as a function of M_{500} for each of our simulations, along with observational data from REXCESS (PAP10). For clarity, we do not plot individual points for the GO simulation, but instead show the best-fitting relation in log-log space, and the typical dispersion about this relation. The gradient of the best-fitting line is very close to zero, so the normalization of the scaled entropy profiles is independent of mass for GO clusters, as in the self-similar model. By contrast, our PC and FO models predict that the scaled entropy at r_{500} is a decreasing function of mass, implying that non-gravitational heating affects the entropy structure of the ICM out to larger radii in lower-mass systems. This is consistent with the expectation that non-gravitational processes are more influential at the low-mass end of the cluster population. Massive clusters in the PC and FO runs have a similar entropy at r_{500} to their GO counterparts. Note that the observational data points also appear to suggest

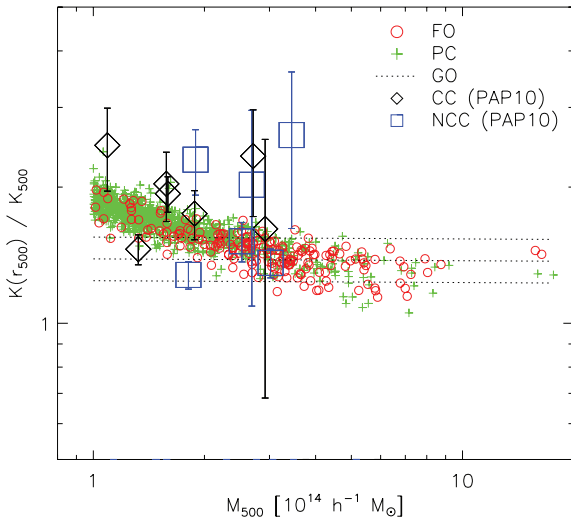


Figure 3. Scaled entropy at r_{500} as a function of total mass within r_{500} for clusters in the Millennium Gas simulations. For clarity, we do not display individual data points for the GO run, but instead show the best-fitting relation and the typical dispersion about this relation. Observational data for CC and NCC clusters in the REXCESS sample (PAP10) are also shown for comparison, along with 1σ error bars. Only clusters with $M_{500} \geq 10^{14} h^{-1} M_{\odot}$ are considered.

that the scaled entropy at r_{500} decreases with increasing mass, being scattered about the PC and FO model predictions.

The mass-dependence of the normalization of scaled cluster entropy profiles in the PC and FO runs explains why we see a larger scatter about the average profile than in the GO run. The scatter about the mean profile in the PC run is similar to that found in observed profiles of NCC systems, but the FO run generates clusters with a wider range of entropy profiles, leading to a larger scatter than is observed.

Neither the PC nor the FO models are capable of reproducing the steeply declining entropy profiles seen in CC clusters. In the case of the FO run, this problem could potentially be overcome by including radiative cooling in our model, since cooling acts to lower the entropy in dense central regions where the gas cooling time is short. As we have said, cooling is included in the PC run, but it is curtailed at high redshift by the preheating.

Self-consistent N -body/SPH simulations that incorporate cooling, star formation and associated feedback are able to produce entropy profiles that resemble those of CC clusters, with a normalization in the outer parts of clusters that is higher than predicted by pure gravitational heating, and a steep slope that remains roughly constant all the way into the core (e.g. Borgani et al. 2002, 2004; Kay et al. 2004; Kay 2004; Kay et al. 2007). However, this success is usually achieved at the expense of excessive star formation. Furthermore, such simulations fail to reproduce the observed entropy profiles of NCC systems.

4.2 X-ray scaling relations at $z = 0$

We now discuss whether our feedback model generates local X-ray scaling laws that are compatible with observations, focusing on the Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} relations. In each case, we compare with the corresponding relation derived from the low-redshift REXCESS data by PCA09. Wherever possible, we explain any differences that arise using the knowledge gleaned from our discussion of cluster profiles. The data of PCA09 are particularly suitable for a comparison with our simulated cluster samples because they tabulate spectral temperatures and luminosities within r_{500} (where r_{500} is defined as in this work), and their luminosities are bolometric. Note that we have rescaled the observational data to allow for the slightly different choice of cosmological parameters adopted by PCA09.

For each set of cluster properties, $(X, Y) = (M, Y_X)$, (M, T_{sl}) , (M, L_X) and (T_{sl}, L_X) , we fit a power-law scaling relation of the form

$$E(z)^n Y = C_0 \left(\frac{X}{X_0} \right)^\alpha \quad (10)$$

to our simulated data points by minimizing χ^2 in log space. Here $X_0 = 5 \times 10^{14} h^{-1} M_{\odot}$ if $X = M$ and $X_0 = 6 \text{ keV}$ if $X = T_{\text{sl}}$. The normalization C_0 has units of $10^{14} M_{\odot} \text{ keV}$, keV and $10^{44} h^{-2} \text{ erg s}^{-1}$ for $Y = Y_X$, T_{sl} and L_X , respectively. Best-fitting parameters α and C_0 for each relation are summarized in Table 2. The factor $E(z)^n$ is included to remove the self-similar evolution predicted by equations (1)–(4), where the index $n = -2/3$, $-2/3$, $-7/3$ and -1 for the Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} relations, respectively. We include this scaling factor simply to ‘adjust’ observational data to $z = 0$ for comparison with our $z = 0$ simulated clusters. This will only be a small effect for the redshift range ($z < 0.2$) probed by the REXCESS sample.

Table 2. Best-fitting parameters (with 1σ errors) for the $z = 0$ X-ray scaling relations obtained from the Millennium Gas simulations.

Relation	C_0	α	$\sigma_{\log_{10} Y}$
GO simulation			
Y_X-M	4.202 ± 0.070	1.547 ± 0.014	0.087
$T_{\text{sl}}-M$	3.931 ± 0.057	0.554 ± 0.012	0.076
L_X-M	18.58 ± 0.53	1.203 ± 0.024	0.148
L_X-T_{sl}	37.6 ± 1.5	2.004 ± 0.040	0.137
PC simulation			
Y_X-M	5.622 ± 0.052	1.7805 ± 0.0079	0.045
$T_{\text{sl}}-M$	6.310 ± 0.031	0.5512 ± 0.0042	0.024
L_X-M	5.549 ± 0.088	1.842 ± 0.013	0.076
L_X-T_{sl}	4.563 ± 0.055	3.297 ± 0.020	0.063
FO simulation			
Y_X-M	5.757 ± 0.069	1.692 ± 0.016	0.048
$T_{\text{sl}}-M$	6.333 ± 0.049	0.521 ± 0.010	0.031
L_X-M	6.17 ± 0.15	1.777 ± 0.033	0.098
L_X-T_{sl}	4.99 ± 0.12	3.296 ± 0.065	0.104

C_0 is the best-fitting normalization of the relations, and α is the best-fitting slope (see equation 10). $\sigma_{\log_{10} Y}$ is the scatter about the mean relation as defined by equation (11).

Scatter in the relations, $\sigma_{\log_{10} Y}$, is quantified via the rms deviation of $\log_{10} Y$ from the mean relation:

$$\sigma_{\log_{10} Y}^2 = \frac{1}{N-2} \sum_{i=1}^N \left[\log_{10} Y_i - \alpha \log_{10} \left(\frac{X}{X_0} \right) - \log_{10} C_0 \right]^2, \quad (11)$$

where N is the number of individual data points (X_i, Y_i). The scatter about each relation is also listed in Table 2.

4.2.1 The Y_X-M relation

The Y_X-M relation is particularly important as both simulations and observations indicate that Y_X is a low-scatter mass proxy, even in the presence of significant dynamical activity. Fig. 4 shows the local Y_X-M relation obtained from the Millennium Gas FO simulation, along with the relations derived from the GO and PC simulations and the observational data of PCA09. We define Y_X as the product of the gas mass inside r_{500} and the spectroscopic-like temperature in the $0.15r_{500} < r \leq r_{500}$ region, for consistency with the observations.

In the self-similar model we would expect the slope of the Y_X-M relation to be $\alpha = 5/3$ (equation 4). The Y_X-M relation obtained from the GO simulation is significantly shallower than both this and the observed relation. The slope of the PC Y_X-M relation is consistent with the observed slope $\alpha \approx 1.8$ from Arnaud et al. (2007) at the 1σ level. On the other hand, the FO run yields a Y_X-M relation that is shallower than observations suggest, with a slope closer to that expected from self-similar scaling. This is similar to the result $\alpha \approx 1.7$ obtained by Kravtsov et al. (2006) using simulations with radiative cooling, star formation and supernova feedback. The predicted scatter about the mean relation is similar in the PC and FO runs, being about a factor of 2 less than in the GO simulation. We note that Y_X does not appear to be as tightly correlated with cluster mass as T_{sl} in any of our simulations.

The fact that both the PC and FO Y_X-M relations lie close to the self-similar prediction implies that Y_X must be relatively unaffected by the non-gravitational heating in these models. In the case of the FO run, this is presumably because AGN feedback removes gas from the central regions of haloes, reducing the gas mass within r_{500} ,

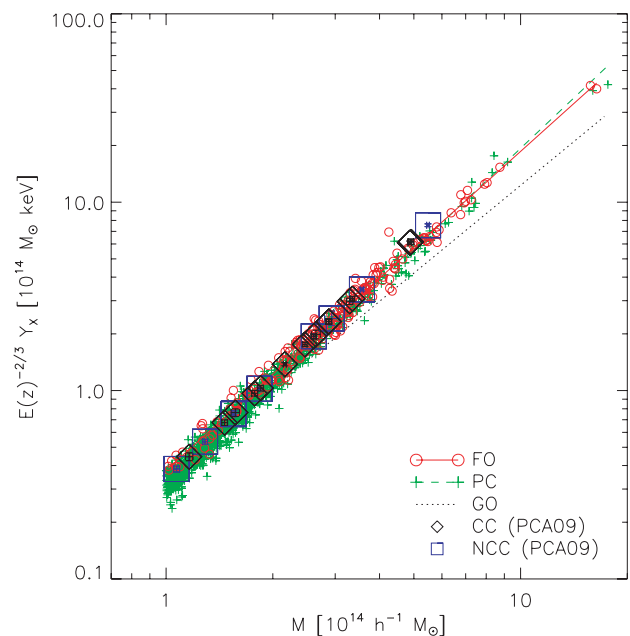


Figure 4. Y_X as a function of total mass within r_{500} for $z = 0$ clusters in the Millennium Gas simulations. We do not display data points from the GO run for clarity. Observational data for CC and NCC clusters from REXCESS (PCA09) are shown for comparison, along with 1σ error bars.

but this is offset by an increase in gas temperature caused by the continual injection of entropy from galaxy formation. Preheating evacuates haloes and increases the temperature of the intracluster gas at high redshift instead, but the eventual outcome is essentially the same.

It is important to note that the masses of the REXCESS clusters were not calculated from gas temperature and density profiles using the equation of hydrostatic equilibrium. This is because, by construction, REXCESS contains objects with a wide variety of dynamical states, so hydrostatic equilibrium may be a poor approximation in some cases. PCA09 estimate cluster masses using the Y_X-M relation of Arnaud et al. (2007) instead, so the observational data points shown in Fig. 4 all lie on this relation by construction.

The Y_X-M relation of Arnaud et al. (2007) was calibrated using clusters with hydrostatic mass estimates. Simulations have shown that the assumption of hydrostatic equilibrium can bias such mass estimates low by $\sim 10-20$ per cent (Rasia et al. 2006; Kay et al. 2007; Nagai et al. 2007; Burns et al. 2008; Piffaretti & Valdarnini 2008; Meneghetti et al. 2010). This is primarily because of additional pressure support provided by subsonic bulk motions in the ICM. Further bias may be introduced if there is significant pressure support from non-thermal components such as cosmic rays and magnetic fields (Laganá, de Souza & Keller 2010). Therefore, the masses of clusters in the REXCESS sample are also likely to be underestimated by the same amount.

If the total mass is indeed biased low by $\sim 10-20$ per cent, then r_{500} will be underestimated by $\sim 3-7$ per cent. Consequently, the gas mass within r_{500} will be biased low, because it is obtained by integrating the density profile out to r_{500} , and the temperature will be overestimated (Fig. 1). The former effect will dominate the latter, so we also expect Y_X to be underestimated. However, this is unlikely to fully compensate for the bias in the total mass estimate, so there may actually be a small offset between our PC and FO Y_X-M relations and the observed relation once any hydrostatic mass bias is accounted for.

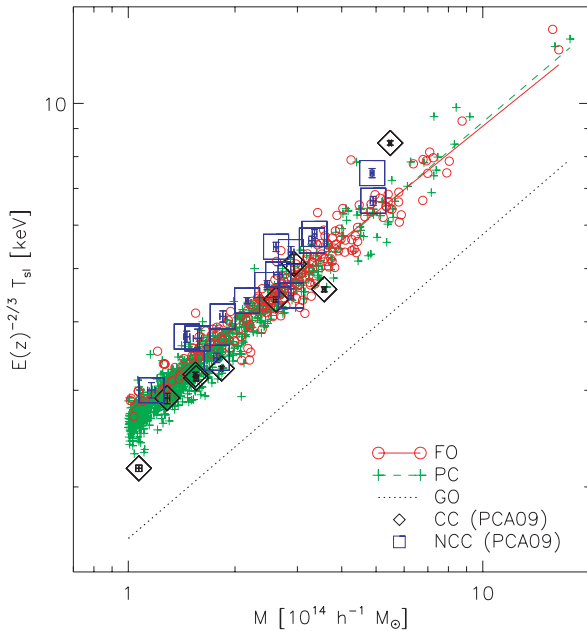


Figure 5. Spectroscopic-like temperature as a function of total mass within r_{500} for $z = 0$ clusters in the Millennium Gas simulations. We also display observational data for CC and NCC clusters in the REXCESS sample (PCA09).

4.2.2 The $T_{\text{sl}}-M$ relation

The $T_{\text{sl}}-M$ relations obtained from the GO, PC and FO runs at $z = 0$ are compared with observational data from REXCESS in Fig. 5.

For a given mass, clusters in the GO run are much cooler than observed, because the spectroscopic-like temperature estimate is dominated by the cool, dense cores of merging subhaloes. Differences in the distribution of this substructure drive fluctuations in T_{sl} , leading to a large scatter about the mean relation. The scatter is ~ 2.5 (3) times larger than in the FO (PC) run. The slope of the GO $T_{\text{sl}}-M$ relation is shallower than observed, and also significantly shallower than $\alpha = 2/3$ expected from the self-similar model (see equation 1). The reason for this is that concentration depends on cluster mass in our GO simulation: low-mass clusters are more concentrated, and thus hotter, than their high-mass counterparts, flattening the $T_{\text{sl}}-M$ relation relative to the self-similar prediction.

Non-gravitational heating in the PC and FO runs raises the mean temperature of the ICM above that expected from gravitational heating alone (Fig. 1). At a fixed mass, PC and FO clusters are thus hotter than their GO counterparts, with temperatures close to those of observed clusters. Both the PC and FO $T_{\text{sl}}-M$ relations have a similar normalization and slope, even though the manner in which entropy is injected into the intracluster gas is completely different in each case. The slope $\alpha \approx 0.55$ is close to that derived by Kay et al. (2007) from a simulation incorporating gas cooling and stellar feedback. However, the REXCESS relation has a significantly steeper slope: $\alpha = 0.633 \pm 0.032$ or $\alpha = 0.622 \pm 0.031$ (G. W. Pratt, private communication), depending on the fitting procedure adopted (see PCA09 for details). Note that the observed slope is consistent with the self-similar value, indicating that the $T_{\text{spec}}-M$ relation is relatively insensitive to baryonic physics.

Cooling processes are neglected in our FO model and inefficient in the PC model, so systems with a CC are not formed in either simulation. If we only consider the NCC clusters in REXCESS, the resulting $T_{\text{spec}}-M$ relation is shallower: $\alpha = 0.613 \pm 0.022$ or

$\alpha = 0.617 \pm 0.022$ (G. W. Pratt, private communication), which is slightly closer to, but still steeper than, the slope obtained from our PC and FO simulations. The intrinsic scatter (i.e. once measurement errors have been accounted for) about the REXCESS $T_{\text{spec}}-M$ relation for NCC clusters is $\sigma_{\log_{10} Y} = 0.025 \pm 0.015$ (G. W. Pratt, private communication), regardless of the regression method used, which is consistent with the scatter about the mean relation obtained from our PC and FO simulations. However, we note that the observational scatter will be an underestimate of the true dispersion since the masses of REXCESS clusters were derived from the Y_X-M relation of Arnaud et al. (2007) assuming no intrinsic scatter about that relation.

It appears that a better fit to the observed data could be obtained, at least for the NCC clusters, if the observational data points in Fig. 5 were shifted to the right by ~ 10 per cent in mass. This is consistent with the level of bias expected from hydrostatic estimates of cluster mass.

4.2.3 The L_X-M relation

In Fig. 6, we show the three local Millennium Gas L_X-M scaling relations, plus observational data from PCA09.

The peak of the X-ray emission in GO clusters is unresolved in our simulation, so the computed luminosities are not trustworthy. We present the GO L_X-M relation merely to illustrate how dramatically the model fails in reproducing the observational data.

The L_X-M relations obtained from the PC and FO simulations are both steeper than anticipated from pure gravitational heating. Both relations have a slope $\alpha \approx 1.8$, whereas the slope measured by PCA09 is $\alpha = 1.81 \pm 0.10$ or $\alpha = 1.96 \pm 0.11$. In the case of the FO run, this departure from self-similar scaling arises because AGN feedback expels gas from central cluster regions, reducing the gas density and thus X-ray emissivity. This effect is stronger in less massive systems, steepening the L_X-M relation as observed. By contrast, similarity breaking is accomplished in the PC model by boosting the entropy of the ICM before gravitational collapse

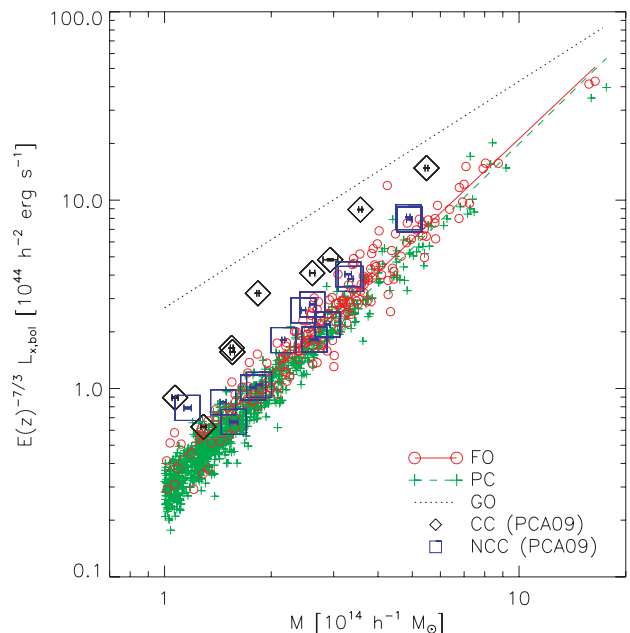


Figure 6. Bolometric X-ray luminosity as a function of total mass within r_{500} for $z = 0$ clusters in the Millennium Gas simulations. Observational data for CC and NCC clusters from REXCESS (PCA09) are also shown.

commences, preventing gas from reaching high densities in cluster cores and lowering the X-ray luminosity. Nevertheless, both the PC and FO models yield almost identical L_X – M relations at $z = 0$.

The large scatter towards the upper edge of the observed L_X – M relation is due to systems with a highly X-ray luminous CC. The PC and FO simulations cannot account for this scatter since neither model can reproduce the steeply declining entropy profiles of CC clusters (Fig. 2). Quantitatively, PCA09 measure the scatter about the mean L_X – M relation to be $\sigma_{\log_{10}(Y)} = 0.166 \pm 0.026$, which is about a factor of 2 greater than the dispersion about our mean PC and FO L_X – M relations, even without accounting for the intrinsic scatter about the Y_X – M relation underpinning the REXCESS cluster mass estimates.

Removing the CC clusters from the REXCESS sample leads to a shallower slope, $\alpha = 1.705 \pm 0.094$ or $\alpha = 1.766 \pm 0.093$, and a reduction in the measured scatter, $\sigma_{\log_{10}(Y)} = 0.094 \pm 0.017$, both of which agree very well with the predictions of our FO model. By contrast the PC L_X – M relation appears to be slightly too steep with too little scatter. The difference in scatter predicted by our two non-gravitational heating models is attributable to the greater diversity in the entropy profiles of objects formed in the FO simulation (Fig. 2).

There is an apparent offset between our PC and FO L_X – M relations and the observational data for NCC clusters. The magnitude of this offset is about ~ 10 per cent in mass, which could be accounted for by bias in the observational mass estimates due to the assumption of hydrostatic equilibrium.

4.2.4 The L_X – T_{sl} relation

The local GO, PC and FO L_X – T_{sl} scaling relations are displayed in Fig. 7, along with observational data from REXCESS. Again, the GO relation is only shown for illustrative purposes.

The PC and FO simulations produce almost identical L_X – T_{sl} relations, with a steep slope $\alpha \approx 3.3$ owing to the breaking of self-

similarity induced by non-gravitational heating. Kay et al. (2007) found a similar slope using a simulation with a self-consistent stellar feedback scheme. For comparison, PCA09 find $\alpha = 2.70 \pm 0.24$ or $\alpha = 3.35 \pm 0.32$ for the REXCESS sample.

The dispersion about the REXCESS L_X – T_{spec} relation is $\sigma_{\log_{10}(Y)} = 0.288 \pm 0.050$ or $\sigma_{\log_{10}(Y)} = 0.318 \pm 0.059$. This is roughly three (five) times larger than the scatter about the FO (PC) L_X – T_{sl} relation, because no X-ray cores are formed in either simulation. However, the PC and FO L_X – T_{sl} relations seem to provide a good fit to the NCC clusters in REXCESS. The observed relation for NCC clusters has a slope $\alpha = 2.89 \pm 0.21$ or $\alpha = 3.06 \pm 0.19$, with corresponding scatter $\sigma_{\log_{10}(Y)} = 0.116 \pm 0.025$ or $\sigma_{\log_{10}(Y)} = 0.124 \pm 0.030$. This is consistent with the scatter about our FO relation, but the PC relation is too tight, with a dispersion that is about of a factor of 2 less.

4.3 Evolution of cluster profiles from $z = 1.5$ to $z = 0$

We have demonstrated that our feedback model can reproduce the observed properties of massive low-redshift clusters reasonably well, apart from those with a CC. We have also seen that the $z = 0$ properties of clusters formed in the feedback run can be replicated almost exactly with a simplistic preheating model, where the entropy of the ICM is raised impulsively at $z = 4$, rather than by continual heating from SNe and AGN. Consequently, we cannot discriminate between these two models using data from local observations.

We now investigate whether feedback from galaxy formation leads to significantly different evolutionary behaviour than simple preheating. In this way we may be able to break the low-redshift degeneracy of the two models. We begin by examining the evolution of cluster profiles from $z = 1.5$ to $z = 0$; this will help us to understand the predicted evolution of X-ray scaling relations discussed in Section 4.4. No attempt is made to compare our results with observations since the available data are, as yet, very limited at high redshift.

4.3.1 Results for the PC simulation

In Fig. 8, we show the evolution of gas density, spectroscopic-like temperature and entropy profiles for clusters in the PC run. In the top row, we plot the profiles of the 10 hottest systems (i.e. the most massive objects) at each redshift and, in the bottom row, profiles for clusters in a narrow temperature range $3 \leq T_{\text{sl}} \leq 4$ keV. Again, we only keep profile data at radii greater than the gravitational softening length. We scale the density, temperature and entropy profiles by $n_{e,500}$, T_{500} and K_{500} , respectively (see equations 7–9). With this scaling we would expect to see no evolution of cluster profiles in the self-similar model, where the ICM is only heated by gravitational processes. We have confirmed that this is indeed the case in our GO run.

Focusing on the profiles of the hottest clusters, we see clear signs of evolution beyond the self-similar prediction, which can be understood as follows. Imposing a uniform entropy floor at $z = 4$ boosts the entropy of the ICM more in core regions than at large radii. Gas is driven out from central cluster regions, flattening the density profile and increasing the normalization of the temperature profile, relative to the prediction from gravitational heating alone. Note that the temperature must increase if the slope of the density profile decreases to maintain pressure support.

After preheating, ejected gas is gradually reincorporated into descendant haloes as hierarchical growth proceeds. Since the gas

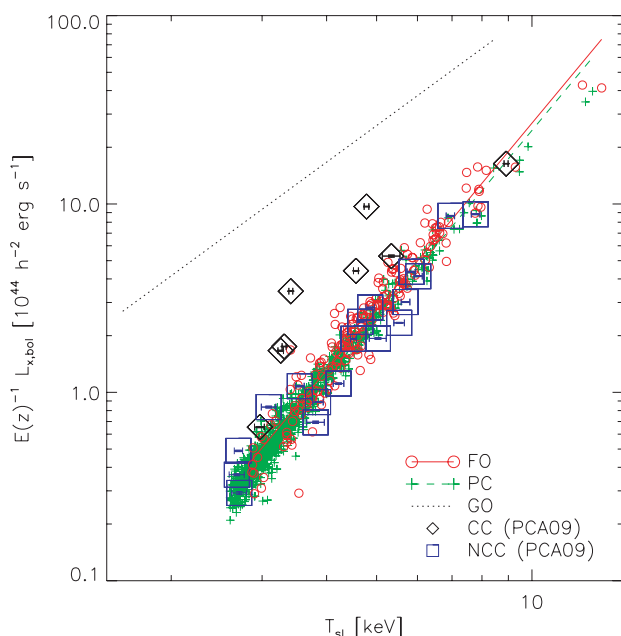


Figure 7. Bolometric X-ray luminosity as a function of spectroscopic-like temperature for $z = 0$ clusters in the Millennium Gas simulations. X-ray properties are calculated within r_{500} . For comparative purposes, we plot observational data for CC and NCC clusters in the REXCESS sample (PCA09).

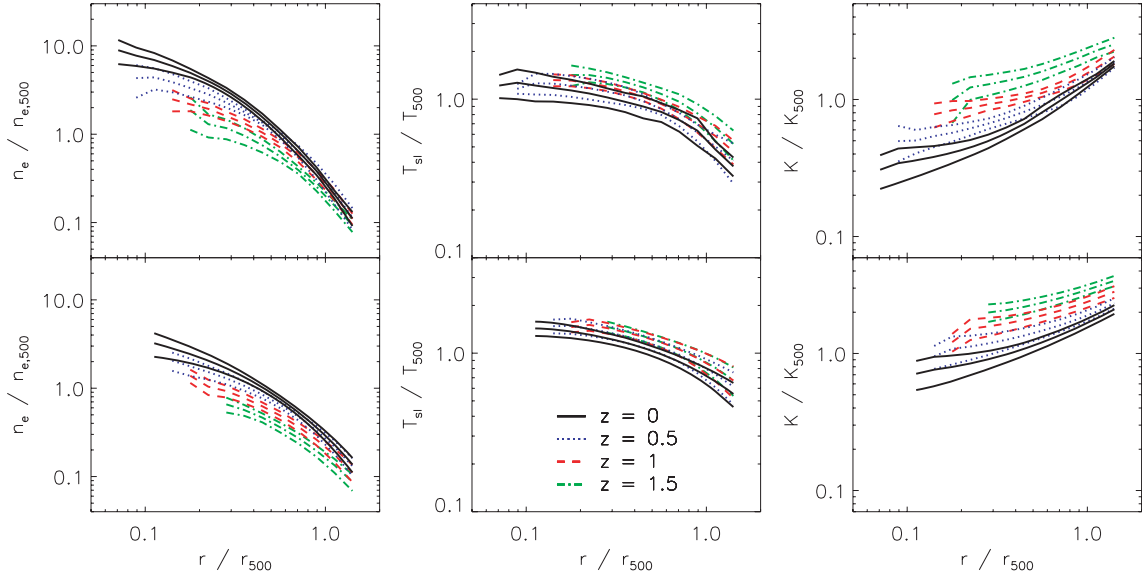


Figure 8. Evolution of gas density (first column), spectroscopic-like temperature (second column) and entropy (third column) profiles for clusters in the Millennium Gas PC run. The top row shows the evolution of the 10 hottest systems, while the bottom row shows the evolution of clusters with a temperature in the range $3 \text{ keV} \leq T_{\text{sl}} \leq 4 \text{ keV}$.

density has already been lowered by the preheating, it does not decrease as rapidly as in the gravitational heating scenario, so we see an increase relative to the average gas density $n_{e,500}$ as $z \rightarrow 0$. Likewise, the preheated gas has a higher temperature and entropy than if the only source of heating was gravity. Therefore, as gas is accreted back on to descendant haloes, compression and shock heating raise its temperature and entropy at a lesser rate than in the gravitational heating model. This explains why we see a drop in gas temperature and entropy with decreasing redshift relative to T_{500} and K_{500} , respectively. Given that there is no further non-gravitational heating of intracluster gas in the PC run, the high-redshift entropy injection will become increasingly ‘diluted’ with time, and cluster profiles will eventually resemble those obtained from a simulation with gravitational heating only.

At any given redshift, several of the 10 hottest objects are likely to have undergone a recent major merger, which could potentially affect the shape, dispersion and evolution of cluster profiles. To investigate this, we first compute the substructure statistic

$$S = \frac{|\mathbf{x}_{\text{com}} - \mathbf{x}_c|}{r_{500}} \quad (12)$$

for each of the 10 most massive clusters at each redshift of interest. Here, $\mathbf{x}_c$ is the location of the dark matter potential minimum, which we take to be the cluster centre, and $\mathbf{x}_{\text{com}}$ is the centre of mass of the cluster gas, defined by

$$\mathbf{x}_{\text{com}} = \mathbf{x}_c + \frac{\sum_i m_i (\mathbf{x}_i - \mathbf{x}_c)}{\sum_i m_i}, \quad (13)$$

where the sums are over all gas particles within r_{500} . Systems undergoing a major merger will be dynamically disturbed and will thus have a larger value of S . Following Kay et al. (2007), we say that a cluster is disturbed if $S > 0.1$, and relaxed otherwise. At each redshift, we have found that the shape and dispersion of the radial profiles shown in the top row of Fig. 8 remain almost unchanged if we only consider relaxed clusters in the sample of the 10 hottest systems. This signifies that our results are not affected by cluster mergers.

The scaled profiles of clusters with $3 \leq T_{\text{sl}} \leq 4 \text{ keV}$ evolve in a similar way to those of the most massive objects, but their shape is different at each redshift. In particular, their density and entropy profiles are flatter. The reason for these differences is that we are now considering lower-mass clusters. Consequently, preheating is more effective at removing gas from their shallower potential wells, modifying their thermodynamic properties out to larger radii.

4.3.2 Results for the FO simulation

The evolution of the scaled gas density, spectroscopic-like temperature and entropy profiles of clusters in the FO run is illustrated in Fig. 9.

The main point to note from the scaled profiles of the 10 hottest clusters is that they do not evolve with redshift. This means that the gas density, temperature and entropy scale in the same way as predicted by the self-similar model: $n_e \propto E(z)^2$, $T_{\text{sl}} \propto E(z)^{2/3} M^{2/3}$ and $K \propto M^{2/3} / E(z)^{2/3}$. Recall that the PC model predicts substantial evolution of scaled cluster profiles over the same redshift range, essentially because haloes are simply ‘recovering’ from the extreme preheating at $z = 4$. By contrast, energy feedback from galaxies is a continual process in the FO run, acting to reduce the gas density and increase the entropy in central regions. The fact that entropy is injected in such a way that the shape of the scaled cluster profiles does not change with redshift is presumably attributable to the self-regulatory nature of the feedback loop in the galaxy formation model underpinning our simulation. This behaviour is not peculiar to the most massive objects; we find that the scaled profiles of lower-mass systems evolve in a self-similar fashion too. We have also checked that cluster mergers have a negligible effect on the shape, dispersion and evolution of radial profiles by following the procedure outlined in the previous section.

Turning our attention to clusters with a temperature $3 \text{ keV} \leq T_{\text{sl}} \leq 4 \text{ keV}$, we find that their scaled profiles do evolve, in the opposite sense to that predicted by the PC model. The explanation for this behaviour lies in the fact that we are considering a different

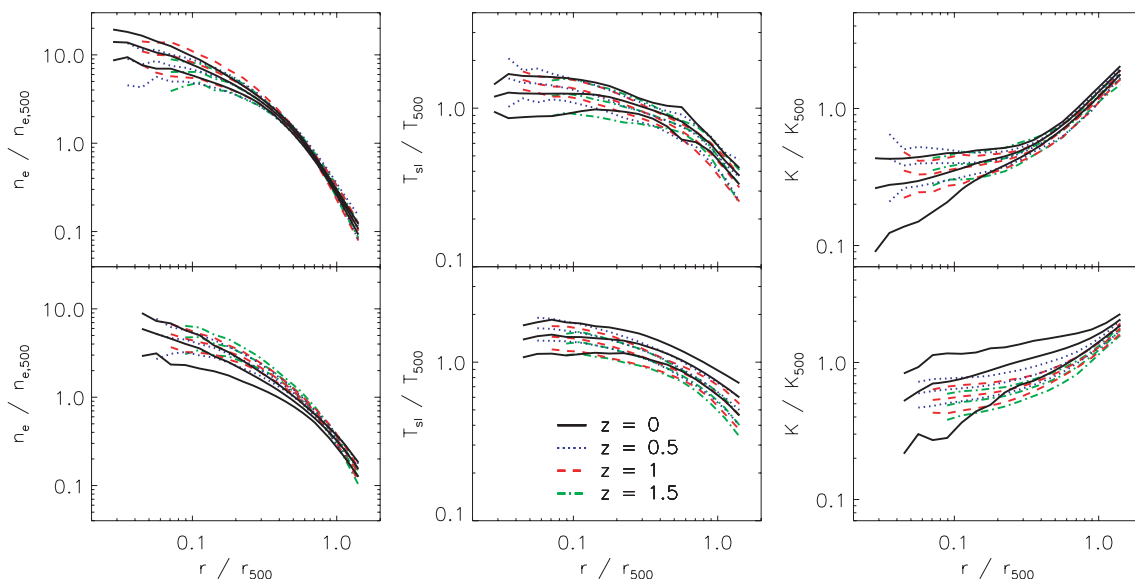


Figure 9. Evolution of gas density, spectroscopic-like temperature and entropy profiles for clusters in the Millennium Gas FO run. The layout of the plots is identical to Fig. 8.

set of clusters at each redshift. Consider the $z = 1.5$ progenitors of clusters with a temperature $3 \text{ keV} \leq T_{\text{sl}} \leq 4 \text{ keV}$ at $z = 0$. These objects are less massive than clusters with a temperature in the same range at $z = 1.5$. Accordingly, they will have been more affected by the non-gravitational heating from AGN, so the gas density will be lower and the entropy higher in central regions. Since the scaled profiles of individual clusters do not evolve in the FO run, these differences are preserved until $z = 0$, so we see apparent signs of evolution when comparing the profiles of clusters with $3 \text{ keV} \leq T_{\text{sl}} \leq 4 \text{ keV}$ at $z = 0$ with clusters of the same temperature at higher redshift.

4.4 Evolution of X-ray scaling relations from $z = 1.5$ to $z = 0$

We have seen that feedback from galaxy formation leads to dramatically different evolution of cluster profiles than high-redshift preheating. It follows that we should see differences in the evolution of X-ray scaling laws too. We now examine whether the evolution of the Y_X - M , T_{sl} - M , L_X - M and L_X - T_{sl} relations predicted by our FO simulation is compatible with observational data, and whether the data prefer this model over simple preheating. The data sets we use are the low-redshift REXCESS sample of PCA09, and the high-redshift sample of Maughan et al. (2008b, hereafter MJF08). We choose to compare with the data of MJF08 for several reasons. First, this data set is one of the largest high-redshift X-ray-selected cluster samples currently available, consisting of 115 clusters observed with *Chandra*. Secondly, it covers a broader redshift range ($0.1 < z < 1.3$) than any other existing large sample. Thirdly, temperatures and bolometric luminosities were derived in the aperture $0 < r \leq r_{500}$, using the same definition of r_{500} as in this work. This agrees with the way in which these properties were calculated for our simulated clusters. Nevertheless, we must be careful not to overinterpret any comparison of our simulated data with observations since strong selection biases limit our ability to perform a statistically meaningful comparison. We discuss this further in Section 4.4.5.

To account for the evolution of X-ray observables, we define scaling relations by

$$E(z)^n Y = C(z) \left(\frac{X}{X_0} \right)^\alpha, \quad (14)$$

where all quantities are as in equation (10), except that the normalization is now a function of redshift. For each relation, we fix the slope α to the $z = 0$ value found previously (see Table 2), and compute the normalization at each redshift by minimizing χ^2 in log space. The self-similar model predicts that the slope of each relation will be independent of redshift. In our simulations, we see small fluctuations in the slope with redshift, but there is no systematic variation, justifying our assumption of a fixed slope.

A power law of the form

$$C(z) = C_0(1+z)^\beta \quad (15)$$

is then fit to the normalization data to determine the parameters C_0 and β (note that this may cause C_0 to change slightly from the $z = 0$ value given in Table 2). Best-fitting parameters for each relation are listed in Table 3. Since we have included the $E(z)^n$ factor in equation (14), then we would expect the slope β to be zero if clusters do indeed evolve self-similarly. If $\beta < 0$ or $\beta > 0$, then we say there is negative or positive evolution, respectively. Note that some authors do not scale out the expected self-similar behaviour first, so their definition of negative/positive evolution has a different meaning to ours. This is one reason why care must be taken when comparing the results of different studies.

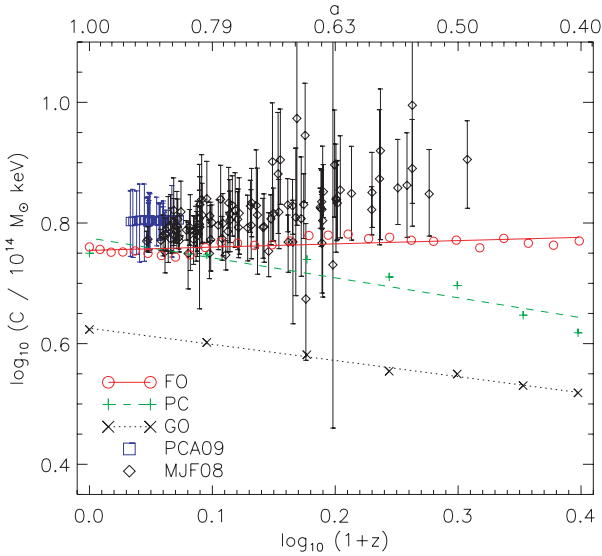
4.4.1 The Y_X - M relation

Fig. 10 illustrates how the normalization of the Y_X - M relation evolves in each of the Millennium Gas simulations. The observational data of PCA09 and MJF08 shown in the figure were plotted as follows. For each cluster in the two data sets, we computed $C(z)$ using equation (14), assuming α was fixed to the slope of the local Y_X - M relation of Arnaud et al. (2007): $\alpha = 1.825 \pm 0.090$. Note that MJF08 adopt the same definition of Y_X as used in both this work and REXCESS.

Table 3. Best-fitting parameters (with 1σ errors) for the evolution of the normalization of the X-ray scaling relations predicted by each Millennium Gas simulation.

Relation	C_0	β
GO simulation		
Y_X-M	4.222 ± 0.028	-0.267 ± 0.011
$T_{\text{sl}}-M$	3.941 ± 0.031	-0.335 ± 0.013
L_X-M	19.53 ± 0.65	-0.243 ± 0.055
L_X-T_{sl}	39.4 ± 1.4	0.370 ± 0.058
PC simulation		
Y_X-M	5.96 ± 0.23	-0.330 ± 0.066
$T_{\text{sl}}-M$	6.317 ± 0.025	0.0423 ± 0.0065
L_X-M	6.18 ± 0.42	-0.90 ± 0.11
L_X-T_{sl}	5.34 ± 0.52	-1.77 ± 0.16
FO simulation		
Y_X-M	5.683 ± 0.038	0.054 ± 0.014
$T_{\text{sl}}-M$	6.180 ± 0.042	-0.249 ± 0.014
L_X-M	6.334 ± 0.046	0.748 ± 0.015
L_X-T_{sl}	5.85 ± 0.14	0.760 ± 0.050

C_0 is the best-fitting normalization, and β is the best-fitting slope. β characterizes the evolution of the normalization (see equations 14 and 15).

**Figure 10.** Normalization of the Y_X-M scaling relation as a function of redshift for each of the Millennium Gas simulations. Low-redshift observational data from REXCESS (PCA09) and the high-redshift data of MJF08 are shown for comparison. 1σ error bars are also plotted for the observational data.

The normalization of the Y_X-M relation evolves in a negative sense in the PC run, which can be understood as follows. Preheating drives significant amounts of gas beyond r_{500} at high redshift, even in the most massive of haloes. Given some cluster at $z = 0$, its gas mass at high redshift will thus be less in the PC run than expected from the pure gravitational heating scenario. On the other hand, Fig. 8 shows that the spectroscopic-like temperature increases with redshift relative to the self-similar prediction. Since Y_X is the product of these two quantities, these opposing evolutionary trends will cancel each other out to some degree. However, the net effect is a more rapid decrease in Y_X with redshift than anticipated from the self-similar model. Since the total mass of a preheated cluster will

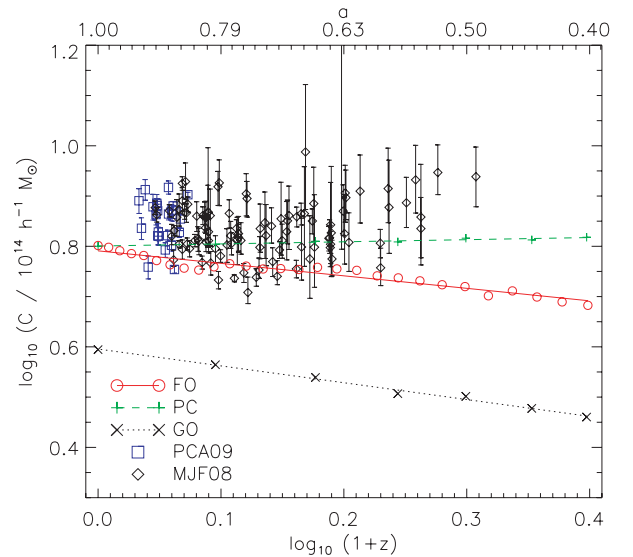
decrease with redshift at a rate akin to the self-similar prediction, this implies that any cluster on the PC Y_X-M relation at $z = 0$ will follow a steeper trajectory towards the bottom-left of the Y_X-M plane than expected. The drop in normalization with redshift will then be larger than in the self-similar model, so we see negative evolution.

Unlike preheating at high redshift, our model for feedback from galaxies produces a cluster population whose properties scale in a self-similar manner (see the top row of Fig. 9). We would therefore expect to see no evolution of the normalization of the FO Y_X-M relation, relative to the prediction of the self-similar model. From Fig. 10 we see that this is almost the case; the value of β obtained from fitting the normalization data is close to zero. There is slight positive evolution which arises because the slope of the relation, $\alpha \approx 1.7$, is marginally steeper than the self-similar value. This effect is explained in full in Appendix A. We note that the significant negative evolution seen in the GO model can be explained in the same way.

4.4.2 The $T_{\text{sl}}-M$ relation

The normalization of the $T_{\text{sl}}-M$ relations obtained from the GO, PC and FO runs is shown as a function of redshift in Fig. 11. Also shown is the observational data of PCA09 and MJF08, where we have assumed a fixed slope equal to that of the local REXCESS $T_{\text{spec}}-M$ relation: $\alpha = 0.633 \pm 0.032$ (G. W. Pratt, private communication).

The PC model predicts slightly positive evolution of the normalization. If we take a particular object that lies on the $T_{\text{sl}}-M$ relation at $z = 0$, then we know from Fig. 8 that its temperature will decrease less rapidly with redshift than in the gravitational heating scenario. However, its total mass will decrease at a similar rate with redshift as it is dominated by the dark matter. Therefore, the cluster will move towards the bottom left of the $T_{\text{sl}}-M$ plane, following a shallower trajectory than expected from self-similar scaling arguments. It follows that, at some $z > 0$, the normalization will be higher than expected, i.e. positive evolution. Although the degree of evolution is small, recall that the slope of the PC $T_{\text{sl}}-M$ relation is substantially shallower than the self-similar value (see Table 2). In Appendix A,

**Figure 11.** Normalization of the $T_{\text{sl}}-M$ scaling relation as a function of redshift for each of the Millennium Gas simulations. We also display observational data from PCA09 and MJF08.

we show how this can induce negative evolution, implying that the positive evolution predicted by the PC model is actually stronger than it appears.

The normalization of the $T_{\text{sl}}-M$ relation obtained from the FO run evolves in the opposite sense, being significantly negative. *A priori* we would expect to find $\beta \approx 0$ in this model since entropy is injected in such a way that the profiles of individual clusters scale self-similarly (Fig. 9). The cause of the apparent evolution is that the slope is considerably shallower than the self-similar prediction. Given this difference in slope, the argument presented in Appendix A implies that individual clusters must decrease in mass by about a factor of 3 between $z = 0$ and $z = 1$ to account for the ~ 20 per cent drop in normalization seen in Fig. 11. We have checked that this is indeed the case in the FO simulation.

4.4.3 The L_X-M relation

In Fig. 12, we show how the normalization of the L_X-M relation evolves in each of our three simulations. The observational data of PCA09 and MJF08 are also plotted, assuming a fixed slope $\alpha = 1.96 \pm 0.11$, which is the slope of the low-redshift REXCESS L_X-M relation.

The normalization of the L_X-M relation evolves in a negative manner in the PC run. To explain this, consider some preheated cluster that lies on the $z = 0$ relation. Recall from Fig. 8 that the PC model predicts a drop in gas density, relative to the self-similar prediction, as redshift increases. Since the dominant contribution to the X-ray luminosity is the gas density in the bremsstrahlung regime, then the luminosity at some higher redshift will be lower than predicted by the self-similar model. Given that the total mass of the cluster at this redshift will be close to the value expected from self-similar evolution, then we will see an apparent decrease in normalization of the L_X-M relation relative to the self-similar prediction. This corresponds to negative evolution. We would expect the evolution to appear stronger if the slope of the PC L_X-M relation matched the self-similar value, rather than being considerably steeper.

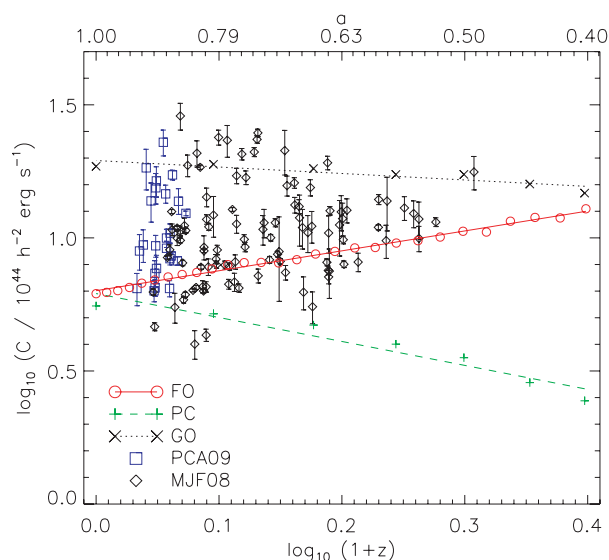


Figure 12. Normalization of the L_X-M scaling relation as a function of redshift for each of the Millennium Gas simulations. For comparative purposes, we plot low- and high-redshift observational data from PCA09 and MJF08, respectively.

The density and temperature profiles of clusters formed in the FO run evolve in a self-similar fashion, so the X-ray luminosity will also scale self-similarly. Since the growth rate of a cluster is governed primarily by the dark matter dynamics, we would thus expect the normalization of the L_X-M relation not to evolve once the predicted self-similar behaviour has been factored out. However, this will only be the case if the slope of the relation matches the self-similar value. In reality, feedback from SNe and AGN establishes a steeper slope, $\alpha \approx 1.8$. As discussed in Appendix A, this departure from self-similarity leads to apparent positive evolution. From Fig. 12, we see that the normalization of the FO L_X-M relation does indeed evolve positively, with a ~ 40 per cent increase in normalization relative to the self-similar model between $z = 0$ and $z = 1$. This is consistent with the fact that the masses of clusters in the FO run decline by roughly a factor of 3 over this redshift range.

4.4.4 The L_X-T_{sl} relation

We show the normalization of the three Millennium Gas L_X-T_{sl} relations as a function of redshift in Fig. 13. To plot the observational data of PCA09 and MJF08, we have fixed the slope to that of the local REXCESS relation: $\alpha = 3.35 \pm 0.32$.

The PC run predicts negative evolution of the L_X-T_{sl} relation as well, which is more pronounced than for the L_X-M relation. This is because the temperature increases relative to the self-similar prediction with redshift (Fig. 8), whereas the total mass decreases at a similar rate. Over a given redshift interval, the normalization of the L_X-T_{sl} relation decreases more than that of the L_X-M relation, so we see a larger drop in normalization relative to the self-similar model, implying stronger negative evolution. As before, the evolution of the PC L_X-T_{sl} relation will have been tempered somewhat, because the slope is steeper than the self-similar value.

On the other hand, our model for feedback from galaxies leads to an L_X-T_{sl} relation with a positively evolving normalization. Given that the X-ray luminosity and spectroscopic-like temperature both scale self-similarly in this model, we should see no evolution relative to that expected from self-similar theory. However, it is evident from Fig. 13 that, between $z = 0$ and $z = 1$, the normalization of the

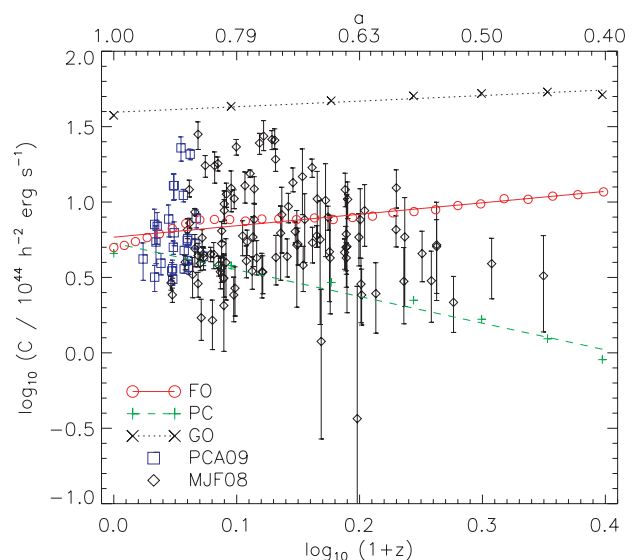


Figure 13. Normalization of the L_X-T_{sl} scaling relation as a function of redshift for each of the Millennium Gas simulations. Data from the observational studies of PCA09 and MJF08 are also shown.

L_X-T_{sl} relation increases by ~ 50 per cent compared to the self-similar prediction. Again, this evolution arises because the slope of the L_X-T_{sl} relation obtained from the FO simulation, $\alpha \approx 3.3$, is much steeper than the self-similar prediction $\alpha = 2$. With this difference in slope, the magnitude of the positive evolution can be readily explained by following the argument outlined in Appendix A, using the fact that the temperatures of individual clusters in the FO run drop by about a factor of 2 between $z = 0$ and $z = 1$.

We note that Kay et al. (2007) find negative evolution of the L_X-T_{sl} relation using a fully self-consistent simulation with radiative cooling, star formation and supernova feedback. Their work is directly comparable to ours (same choice of overdensity, same temperature definition, no core excision, etc.), so this indicates that including AGN feedback changes the way in which the L_X-T_{sl} relation evolves, possibly because of the different redshift-dependence of the two feedback mechanisms.

4.4.5 Comparison with observations

Energy feedback from galaxies leads to substantially different evolution of the Y_X-M , $T_{\text{sl}}-M$, L_X-M and L_X-T_{sl} relations than uniform preheating. We now discuss which of the PC and FO models, if either, is preferred by the high-redshift data of MJF08.

We begin by noting that, as in REXCESS, the masses of clusters in the sample of MJF08 were estimated from a Y_X-M relation. Since this relation was calibrated using clusters with hydrostatic mass estimates, the masses of their high-redshift clusters are also likely to be biased low by ~ 10 – 20 per cent. Therefore, the observational data points shown in Figs 11 and 12 should all be shifted down by ~ 5 – 10 per cent and ~ 20 – 30 per cent, respectively.

Once we have applied this correction, we find that all four scaling relations obtained from the FO run evolve in a manner broadly consistent with the observational data at low to moderate redshifts, $z \lesssim 0.5$. In the case of the L_X-M and L_X-T_{sl} relations, there are hints that the positive evolution predicted by our feedback model provides a better match to the data at these redshifts than the PC model, although the observed scatter is large. Both the PC and FO runs predict similar results for the Y_X-M and $T_{\text{sl}}-M$ relations at $z \lesssim 0.5$, and it is not possible to distinguish between the two models with the observational data.

At higher redshift, $z \gtrsim 0.5$, the observational data for the Y_X-M and L_X-M relations seem to follow an upward trend, consistent with the positive evolution expected from our feedback model. The data also suggest that the $T_{\text{spec}}-M$ relation evolves in a positive sense at these redshifts, but in this case the PC model provides a better description of the observed evolution than the FO model. The PC model also predicts negative evolution of the L_X-T_{sl} relation for $z \gtrsim 0.5$, consistent with the observational data.

It is clear from this discussion that it is difficult to deduce whether the data of MJF08 favour our feedback model over simple preheating. For each relation, it seems as if the observed normalization data cannot be well fitted by a single power law. For example, Fig. 13 suggests that the evolution of the L_X-T_{spec} relation is approximately self-similar (or possibly slightly positive) up until $z \sim 0.5$, then negative thereafter. This could be a signature of a change in the evolutionary behaviour of clusters that is not reproduced by any of our models or, more probably, it may simply be an artefact of selection effects instead.

At low to moderate redshifts, most clusters in the heterogeneous sample of MJF08 come from samples based on the *ROSAT All-Sky Survey* (RASS), which are wide and shallow. Their relatively high

flux limit corresponds to an intermediate mass limit at low redshift, but a much higher mass limit at moderate redshift, thus falling on a steeper part of the mass function. Given the large scatter in the L_X-M relation, this means that the number of objects scattered from the left to the right of the mass limit will grow relative to the number scattered in the other direction. This increasing bias towards luminous systems as we transition from low to moderate redshift may explain the ‘hump’ in the observational data at $z \sim 0.3$ apparent in Figs 12 and 13. Unfortunately, it is hard to quantify this effect since the sample of MJF08 is not cleanly selected, so the selection function is unknown.

At high redshift, we expect the data of MJF08 to be less affected by selection biases for two reasons. First, their high-redshift clusters come from narrow and deep samples, such as the *Wide Angle ROSAT Pointed Survey* (Burenin et al. 2007) and the *400 Square Degree ROSAT PSPC Survey* (Horner et al. 2008), whose lower flux limit corresponds to a high-redshift mass limit that falls on a flatter part of the mass function than the mass limit of RASS-based surveys at moderate redshift. This implies smaller bias given the same scatter in the L_X-M relation as at lower redshift. Secondly, there should be less scatter about the mean L_X-M relation at high redshift due to the absence of CCs (e.g. Vikhlinin et al. 2007), which would further reduce any bias. However, given the remaining uncertainties on the selection biases and the limited number of high-redshift clusters in the sample of MJF08, we cannot draw firm conclusions about the nature of the evolution at $z \gtrsim 0.5$.

To summarize, it is fair to say that the quality of current X-ray data is insufficient to place robust constraints on theoretical models. In addition to small numbers of high-redshift clusters and large measurement errors, existing heterogeneous samples are plagued by strong selection biases which can imitate genuine evolution. As demonstrated by Pacaud et al. (2007), correctly modelling the full source-selection process is crucial for measuring the evolution of scaling laws. In the near future, the XCS will provide a large sample of X-ray-selected clusters (~ 500 objects) with $0 < z \lesssim 1.5$ that have been analysed in a consistent manner across the full redshift baseline. The survey selection function will be well monitored, allowing selection effects to be properly included when analysing the evolution of the X-ray scaling relations. With such a data set it will hopefully become possible to discriminate between theoretical models such as our PC and FO models, providing us with a valuable insight into cluster astrophysics.

5 SUMMARY AND CONCLUSIONS

In this paper, we set out to investigate the evolution of galaxy cluster X-ray scaling relations using numerical simulations. The evolution of scaling laws is crucial for constraining cosmological parameters with clusters surveys, and also offers a potentially powerful probe of the cooling and heating processes operating in clusters. Our main objective was to determine how including additional feedback from AGN in simulations affects the predicted evolution, and whether this is consistent with observations. Given that there is a substantial body of observational and theoretical evidence indicating that AGN are key in shaping the properties of galaxy clusters, it is clearly important to address this issue. However, all evolution studies to date have been based on simulations that only incorporate feedback from star formation.

The simulation we have used for our study – the FO run – is a new member of the Millennium Gas suite, presented for the first time here. The basic objective of the Millennium Gas Project is to add gas to the structures found in the original Millennium Simulation. The

Millennium Gas simulations are ideal for studying the evolution of cluster properties, because their large volume ($500^3 h^{-3} \text{Mpc}^3$) means that we can resolve statistically significant numbers of massive clusters at all relevant redshifts. Furthermore, we can follow the formation of the richest clusters, which are the objects actually observed at high redshift.

Feedback is implemented in our simulation using the hybrid scheme of Short & Thomas (2009), where the energy input into the ICM by SNe and AGN is calculated from a SAM of galaxy formation. This guarantees that feedback originates from a realistic galaxy population, whereas fully self-consistent simulations often predict excessive star formation on cluster scales.

Our main conclusions can be summarized as follows.

(i) Non-gravitational heating from SNe and AGN in the FO run produces a $z = 0$ cluster population whose radial temperature and entropy profiles broadly agree with those of NCC clusters in the REXCESS sample (PAP10). In particular, the temperature profiles are close to isothermal in the core, and the entropy profiles are significantly flatter in central regions than the theoretical $K \propto r^{1.1}$ scaling observed in cluster outskirts. However, it seems that the entropy of the gas has been raised too much in the core, compared to the observational data. None of our clusters exhibits a gentle drop in temperature at small cluster-centric radii or a steadily declining entropy profile, both of which are characteristic of CC systems. This is because gas cannot lose entropy via radiative cooling in our simulation. We note that fully self-consistent hydrodynamical simulations tend to suffer from the opposite problem, in the sense that radiative cooling leads to the overproduction of CCs.

(ii) The Y_X-M , $T_{\text{sl}}-M$, L_X-M and L_X-T_{sl} scaling relations obtained from the FO run at $z = 0$ generally match the local REXCESS relations (PCA09), once we have accounted for the fact that the observed masses are likely to be biased low by ~ 10 – 20 per cent due to the assumption of hydrostatic equilibrium. The exception is that we cannot explain the large scatter above the mean L_X-M and L_X-T_{spec} relations seen in the observational data. This is because the source of this scatter is highly X-ray luminous CC systems which are not formed in our simulation.

(iii) A crude model of non-gravitational heating from astrophysical sources in which the ICM is preheated at $z = 4$, rather than in response to galaxy formation, can produce a population of clusters whose $z = 0$ properties closely resemble those of objects formed in the FO run. In fact, the two model predictions are so similar that they cannot be distinguished using high-quality local observations.

(iv) Density, temperature and entropy profiles of individual clusters in the FO run all evolve in a self-similar fashion from $z = 1.5$ to $z = 0$, although feedback from galaxies has modified their shape compared to that expected from pure gravitational heating. We suspect this is linked to the self-regulation of cooling and heating in the underlying model of galaxy formation.

(v) The profiles of preheated clusters do not scale self-similarly. This is because the injection of entropy at high redshift acts to remove gas from central cluster regions, lowering the gas density and increasing its temperature. Following preheating, the properties of the ICM can only be modified by gravitational processes, so the effect of the preheating is gradually erased and cluster profiles will eventually resemble those of clusters that have been subject to gravitational heating only. This ‘recovery’ from preheating is what drives the apparent evolution of cluster profiles relative to the self-similar model.

(vi) Feedback from galaxy formation in our FO model leads to positive evolution of the Y_X-M , L_X-M and L_X-T_{sl} relations, and

negative evolution of the $T_{\text{sl}}-M$ relation. By contrast, preheating leads to scaling relations that evolve in the opposite sense. Kay et al. (2007) also reported negative evolution of the L_X-T_{sl} relation using a simulation with a self-consistent stellar feedback scheme. This suggests that additional heating from AGN changes the way in which scaling laws evolve, possibly because AGN heating is still important in cluster cores at low-redshift, long after the peak of star formation. We have investigated whether the evolution predicted by our feedback model is consistent with X-ray observations of high-redshift clusters. Unfortunately, the large samples of high-redshift clusters currently available are not cleanly selected, which is problematic since it may generate spurious evolution (e.g. Pacaud et al. 2007). This is possibly why different observational studies give contradictory results. Consequently, we have not been able to decide whether our FO model provides a better description of reality than simple preheating. However, it is encouraging that the evolutionary behaviour predicted by the two models is distinct, particularly in the case of the L_X-M and L_X-T_{sl} relations, so that we could potentially distinguish between them, and also other models (such as that of Kay et al. 2007), when higher-quality data become available. As an example, the XCS will soon provide the largest ever sample of X-ray clusters selected with well-defined criteria, extending out to $z \approx 1.5$. Likewise, large high-redshift cluster samples are expected from SZ surveys currently underway. With such data sets, a rigorous comparison between theory and observation will become possible, so that we will be able to use the evolution of cluster scaling laws as an additional constraint on models of non-gravitational heating in clusters.

The Millennium Gas FO simulation introduced here is the only existing simulation that is large enough to follow the evolution of significant numbers of massive clusters at reasonable resolution, while also attempting to include some of the main physical processes involved in cluster formation: star formation and feedback from both SNe and AGN. Although our feedback model can generally reproduce several key observational properties of clusters, at least for those without a CC, it does have its limitations. In the future, we plan to enhance the hybrid model of Short & Thomas (2009) in two major ways.

First, we will adapt the model to follow the metal enrichment of intracluster gas by Type II and Type Ia SNe. This is important since radial abundance profiles derived from X-ray observations provide valuable constraints on the feedback mechanisms responsible for injecting metals into the diffuse phase (e.g. De Grandi & Molendi 2001; Tamura et al. 2004; Vikhlinin et al. 2005). Cora (2006) has already used a similar approach to tackle this problem (see also Cora et al. 2008). However, they neglected energy feedback from SNe and AGN in their hybrid model, which will have a significant impact on the way metals are distributed throughout the ICM.

Secondly, we aim to self-consistently incorporate radiative cooling into the model as well, rather than relying on the simple cooling recipes employed in SAMs. These recipes usually assume that haloes have a spherically-symmetric isothermal gas distribution but, in general, neither of these assumptions will hold in hydrodynamical simulations. To circumvent this problem, we intend to fully couple SAMs to radiative simulations, so that the gas distribution in the simulation governs star formation, black hole growth and associated feedback in the SAM. This is a non-trivial task, requiring the simulation and SAM to be run simultaneously. With this modification we hope to be able to reproduce the roughly bimodal distribution of core entropies found in real clusters.

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APPENDIX A: MOCK EVOLUTION OF X-RAY SCALING RELATIONS

In this Appendix, we demonstrate how evolution of the scaling relations can arise if the slope is different to the self-similar prediction, even if cluster properties scale self-similarly themselves, as in our FO simulation. We present our argument in terms of the evolution of a general scaling relation of the form (14). A diagram of the situation under consideration is shown in Fig. A1.

Consider a cluster at $z_1 = 0$ that is located at the point (X_1, Y_1) on a Y - X relation with a self-similar slope α_{ss} and normalization C_0^{ss} , so

$$Y_1 = C_0^{ss} \left(\frac{X_1}{X_0} \right)^{\alpha_{ss}}. \quad (A1)$$

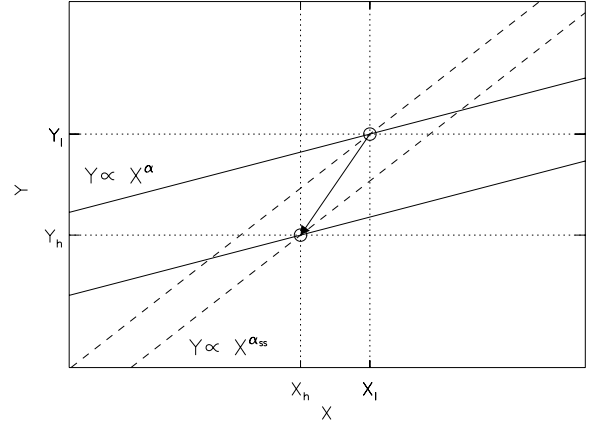


Figure A1. Diagram to illustrate how evolution of a general X-ray scaling relation can be induced if the slope, α , differs from the self-similar value α_{ss} . The arrow shows how the cluster highlighted by an open circle evolves with increasing redshift (see text for mathematical details).

Suppose the cluster evolves self-similarly until, at some redshift $z_h > 0$, it is located at the point (X_h, Y_h) , then

$$E(z_h)^n Y_h = C_0^{ss} \left(\frac{X_h}{X_0} \right)^{\alpha_{ss}}. \quad (A2)$$

In reality, we expect non-gravitational cooling and heating processes to alter the slope of the Y - X relation from the self-similar prediction. Now suppose that our cluster was located at the same point, (X_1, Y_1) , at z_1 , but lay on a Y - X relation with a slope α where, without loss of generality, we take $\alpha < \alpha_{ss}$. If we assume self-similar scaling of cluster properties, as predicted by our feedback model, then the position of the cluster at z_h will again be (X_h, Y_h) . We can then write

$$Y_1 = C_1 \left(\frac{X_1}{X_0} \right)^{\alpha}, \quad (A3)$$

and

$$E(z_h)^n Y_h = C_h \left(\frac{X_h}{X_0} \right)^{\alpha}, \quad (A4)$$

where C_1 and C_h are the normalizations of the Y - X relation at z_1 and z_h , respectively. In the self-similar model we would have $C_h/C_1 = 1$. From equations (A3) and (A4) it follows that

$$\frac{C_h}{C_1} = E(z_h)^n \frac{Y_h}{Y_1} \left(\frac{X_h}{X_1} \right)^{-\alpha}, \quad (A5)$$

but equations (A1) and (A2) imply

$$E(z_h)^n \frac{Y_h}{Y_1} = \left(\frac{X_h}{X_1} \right)^{\alpha_{ss}}, \quad (A6)$$

so

$$\frac{C_h}{C_1} = \left(\frac{X_h}{X_1} \right)^{\alpha_{ss} - \alpha}. \quad (A7)$$

Since $X_h < X_1$ and $\alpha_{ss} > \alpha$, then $C_h/C_1 < 1$, so we see a decrease in normalization relative to the self-similar prediction with redshift, i.e. negative evolution. If the slope had been steeper than the self-similar value, $\alpha > \alpha_{ss}$, then we would have seen apparent positive evolution.

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